

Design of Experiments for Reverse Engineering Formulations

Predicting Chemical Composition from Fewer Test Blends
by Modeling Spectra using Functional Data Analysis

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Short Course
April 22
IDA



Outline

- Why use? & What is Design of Experiments (DOE)?
- What is Functional Data Analysis (FDA)?
- Reverse Engineering Case #1 – Mixture of alcohol blends
- Reverse Engineering Case #2 – Mineral formulations

Review of DOE – Why use it?

*There's no better way
to get the most information
from the least amount of testing*

- Identify important factors when faced with many
- Do sensitivity and trade-space analysis
- Optimize across multiple responses
- Characterize the operating region

Let's go to JMP...

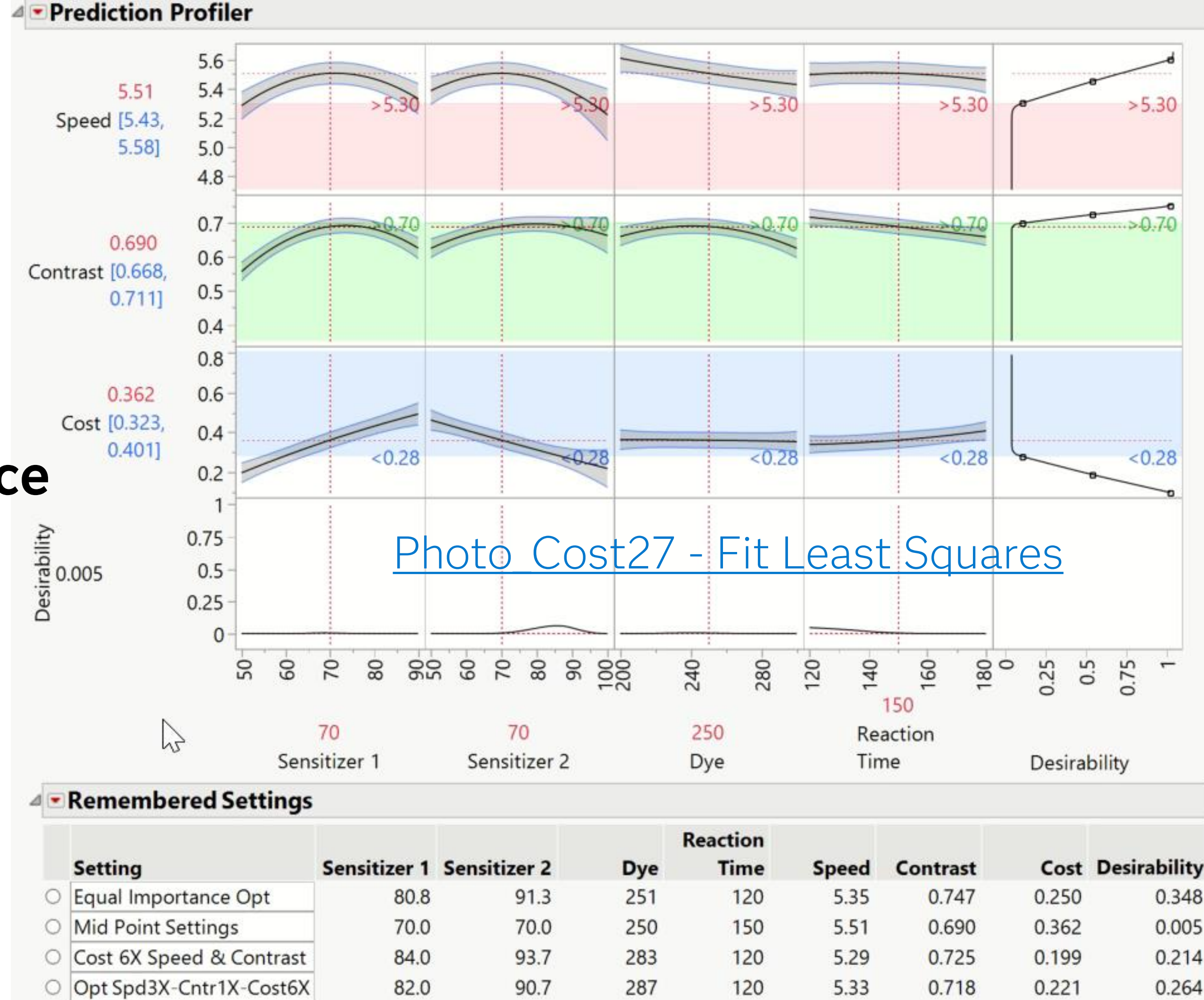
**Use Prediction Profiler to Answer Questions
about the DOE-Characterized/Modeled Process**

Back from JMP...

How do you discuss trading off performance and cost with your decision makers?

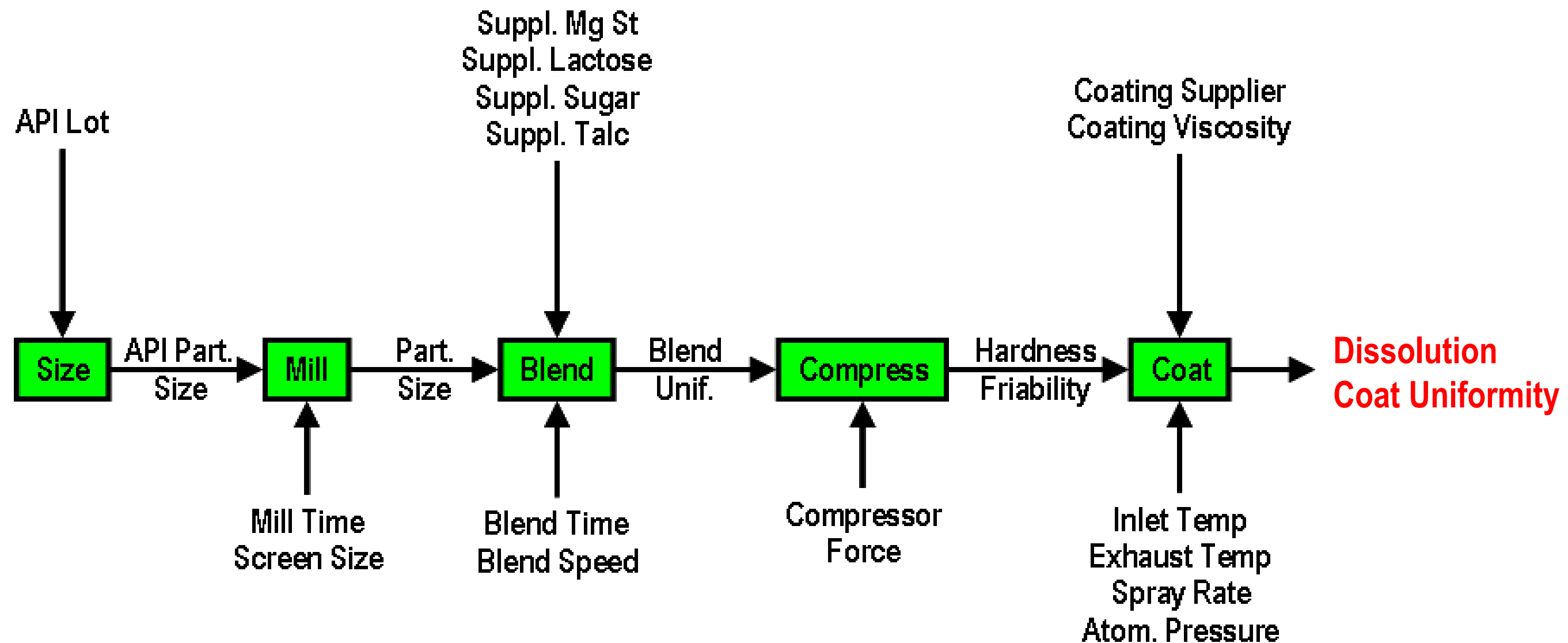
1. Use JMP
2. Record in PPT
3. Interactive HTML
(CI & PI - new in JMP 18)

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Review of DOE - Classic Definition

Purposeful control of the inputs (factors) in such a way as to deduce their relationships (if any) with the outputs (**responses**).



Alternative Definition of DOE

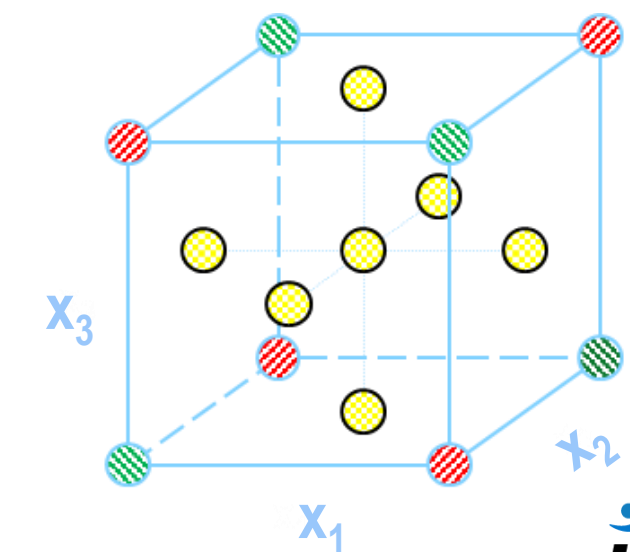
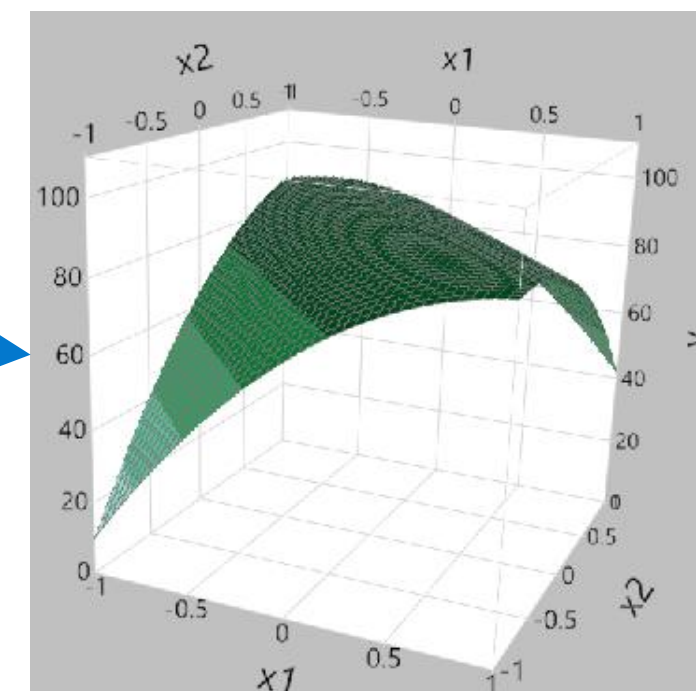
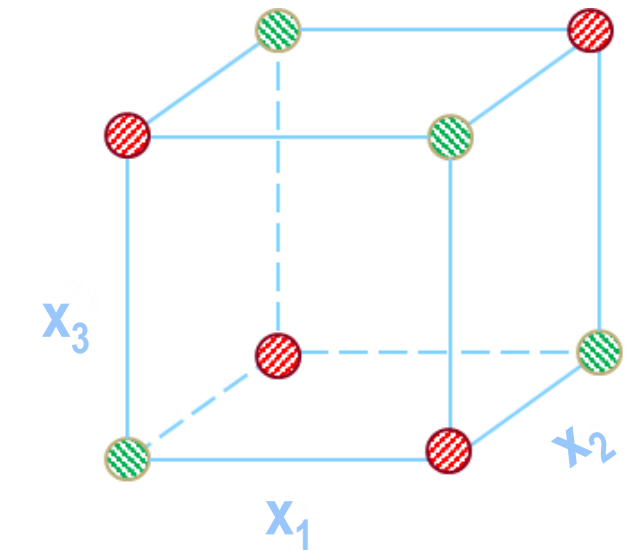
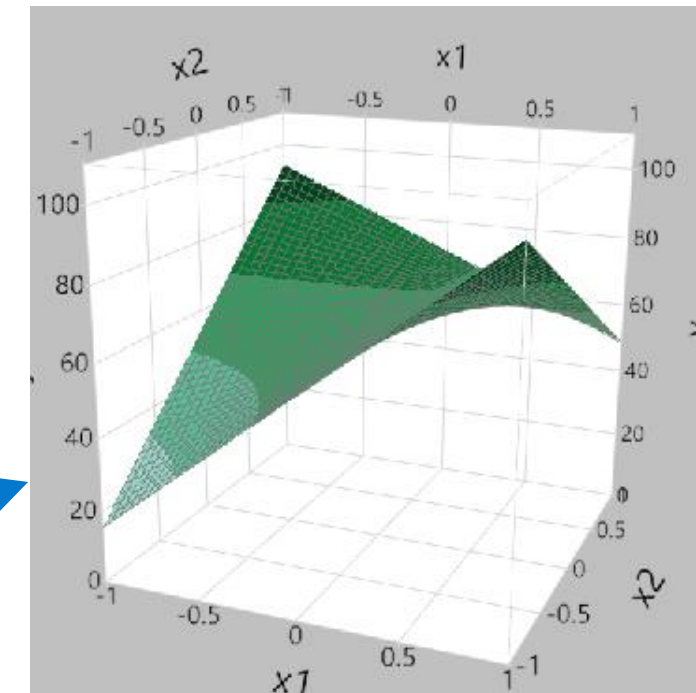
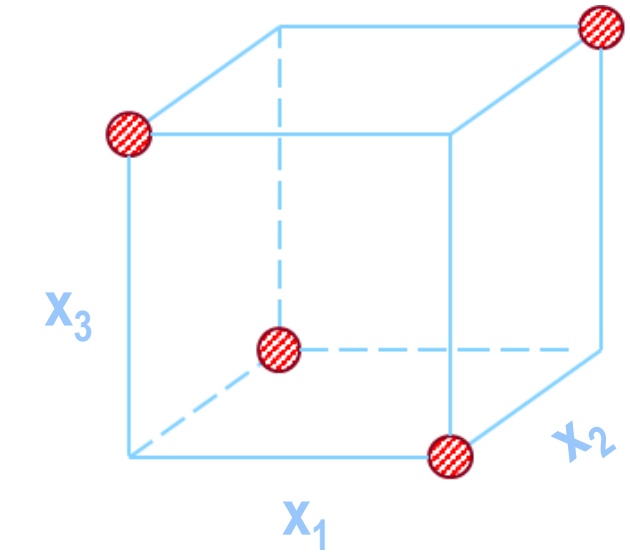
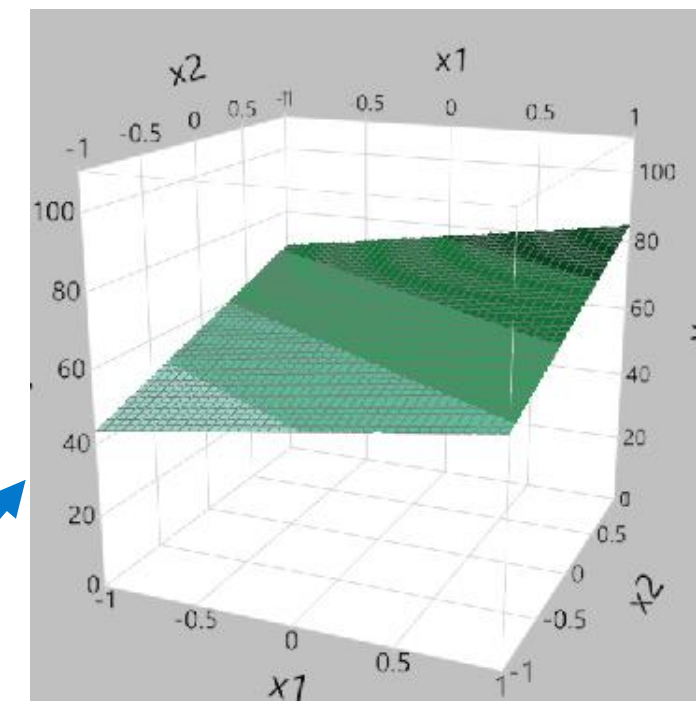
A DOE is a specific collection of trials run to support a *proposed* model.

☒ Guided Mode ☐ Flexible Mode

Define Model Design Data Entry Analyze Predict Report

Model type

<input type="radio"/> Main Effects ▶ Show Hint	12
<input type="radio"/> Main Effects (Uncorrelated with Two-Factor Interactions) ▶ Show Hint	12
<input type="radio"/> Main Effects (Including All Two-Factor Interactions) ▶ Show Hint	16
<input checked="" type="radio"/> Response Surface Design ▶ Show Hint	21

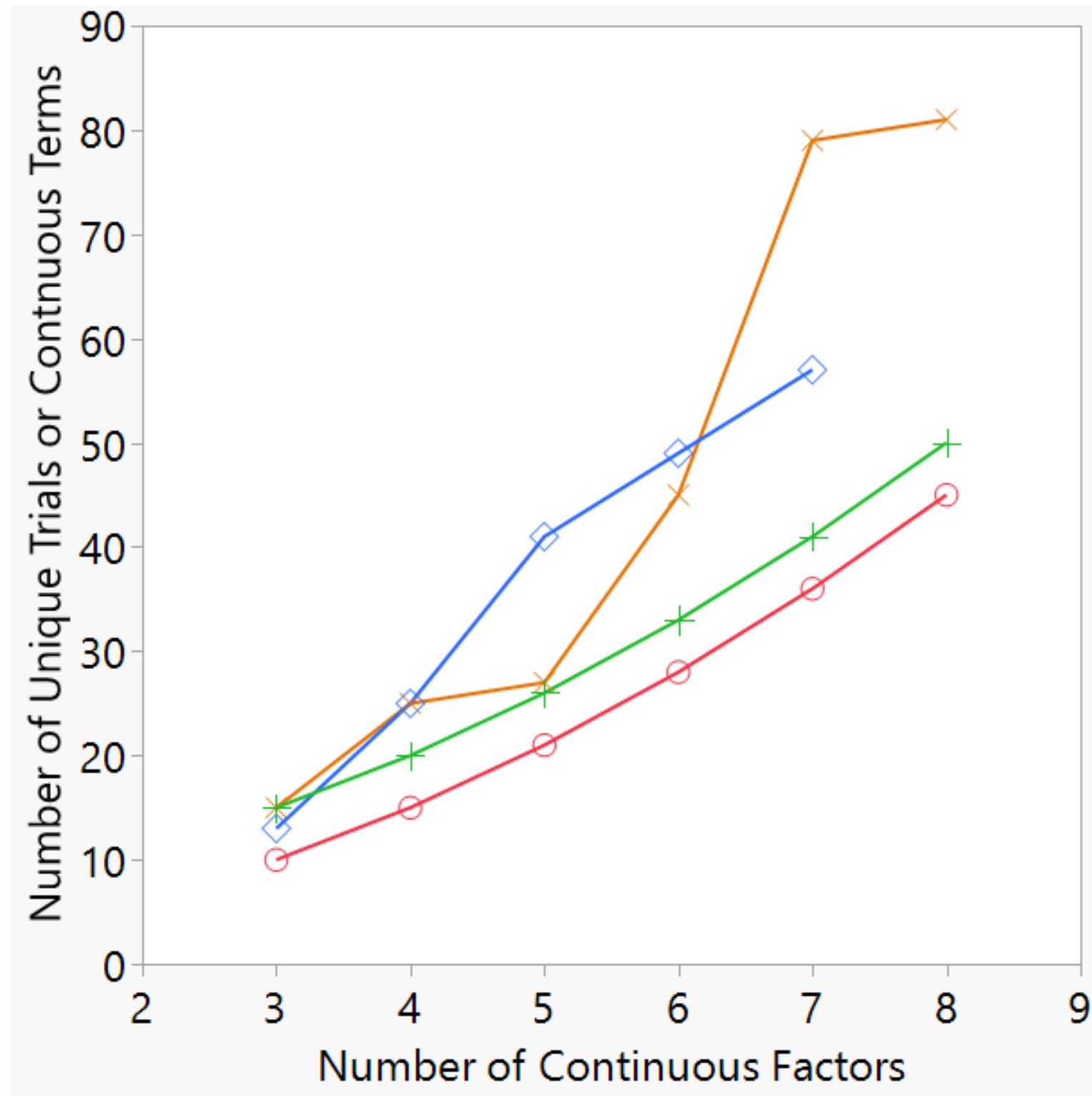


Real-World Design Issues

Model-Driven Custom DOE
Makes Design Fit your Problem –
NOT your Problem Fit the Design!

- Work with different kinds of control variables/factors:
 - Continuous/quantitative
 - Categorical/qualitative
 - Mixture/formulation
 - Blocking
- Work with combinations of these four kinds of variables
- Certain factors are hard-to-change
- Certain factor combinations cannot be run
- Want to add onto existing trials
- Need to repair broken design

Number Unique Trials & Number Quadratic Model Terms vs. Number Continuous Factors

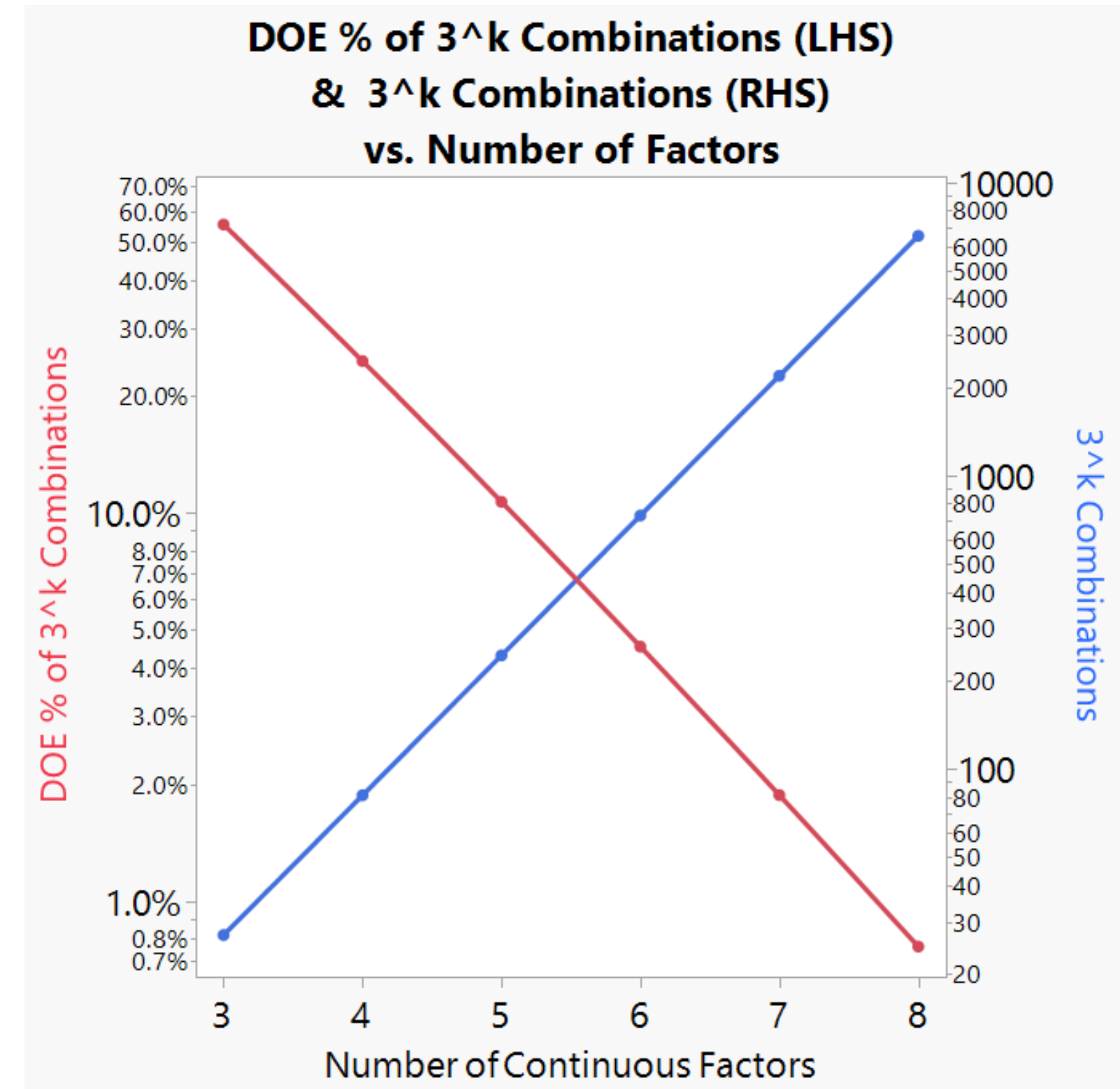
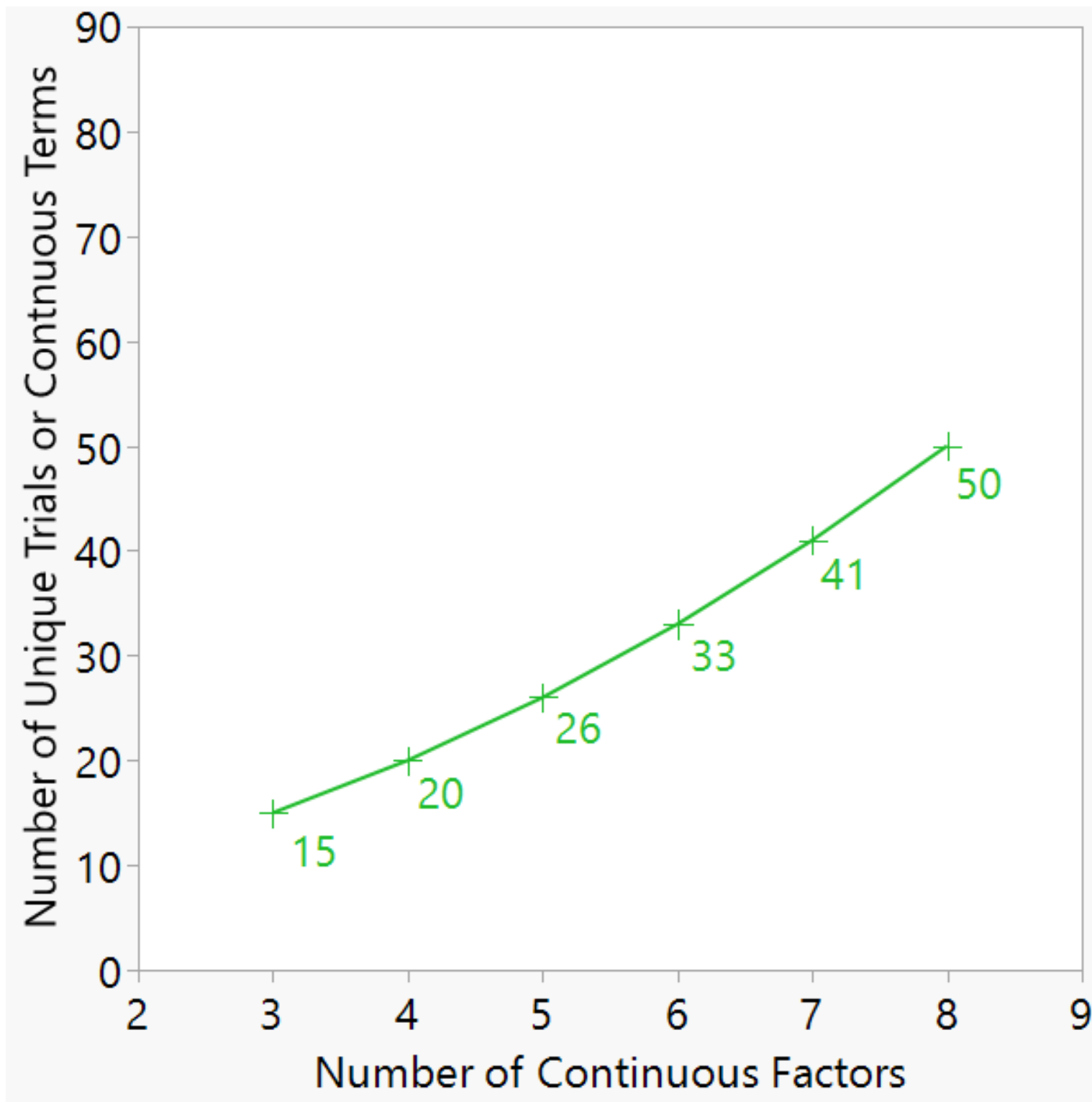


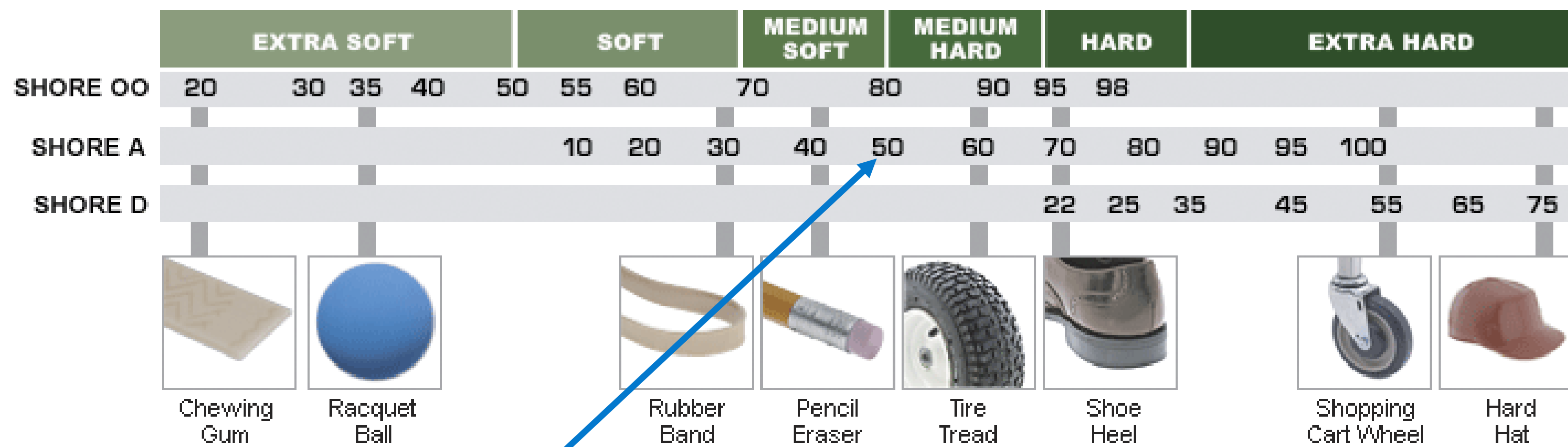
- × — Unique Trials in Central Composite Design
- ◇ — Unique Trials in Box-Behnken Design
- + — Unique Trials in Custom Design with 6 df for Model Error
- — Terms in Quadratic Model

Number of Custom DOE Trials Rises Slowly

Number of Possible Trial Combinations Rises Rapidly (3^k)

DOE Trials as a Percentage of All Combinations Falls Rapidly

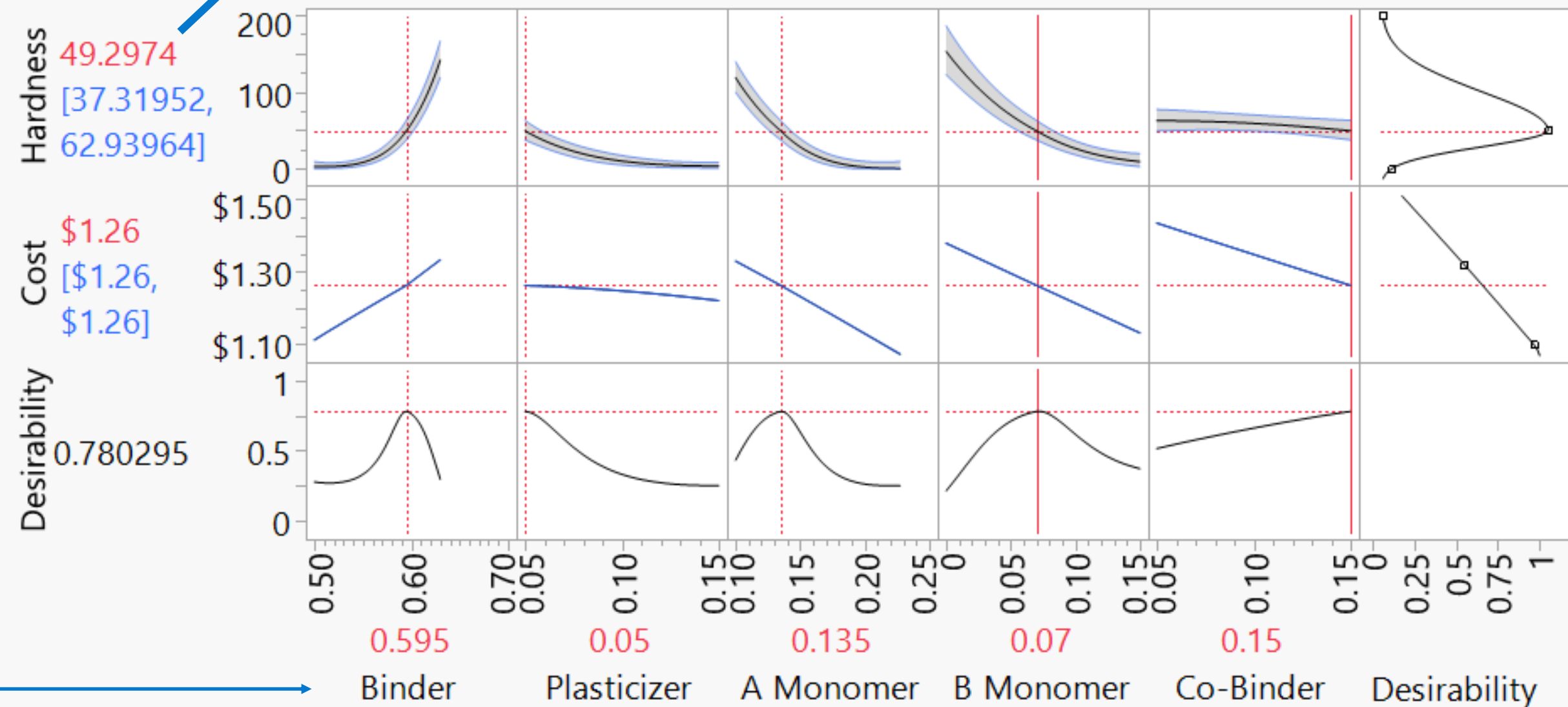




Mixture DOE

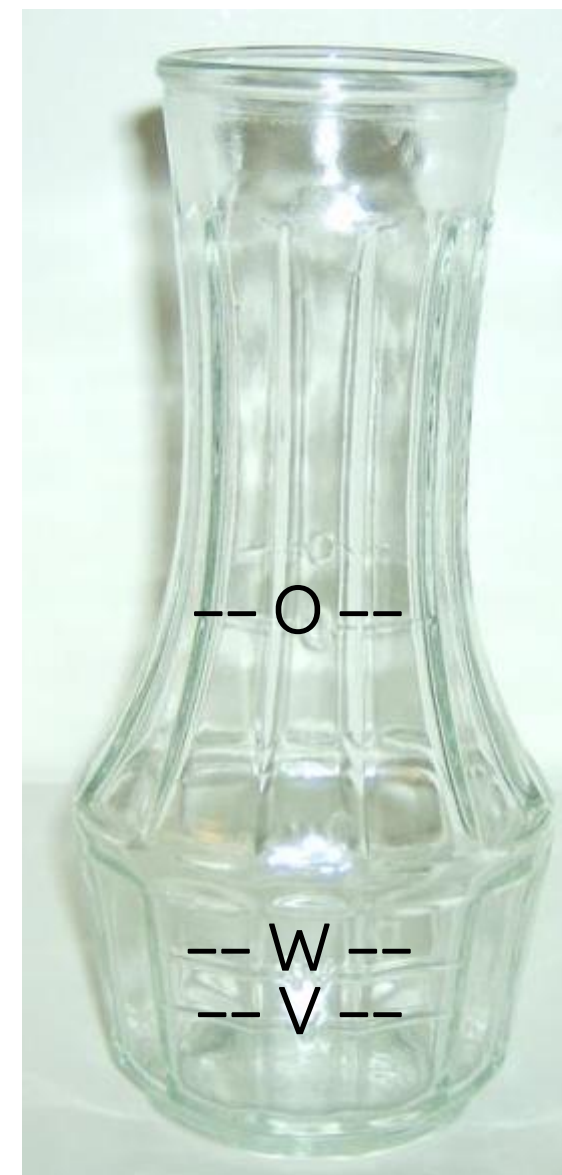
2 Responses & 5 Formulation Components

Prediction Profiler



Mixture or Formulation DOE

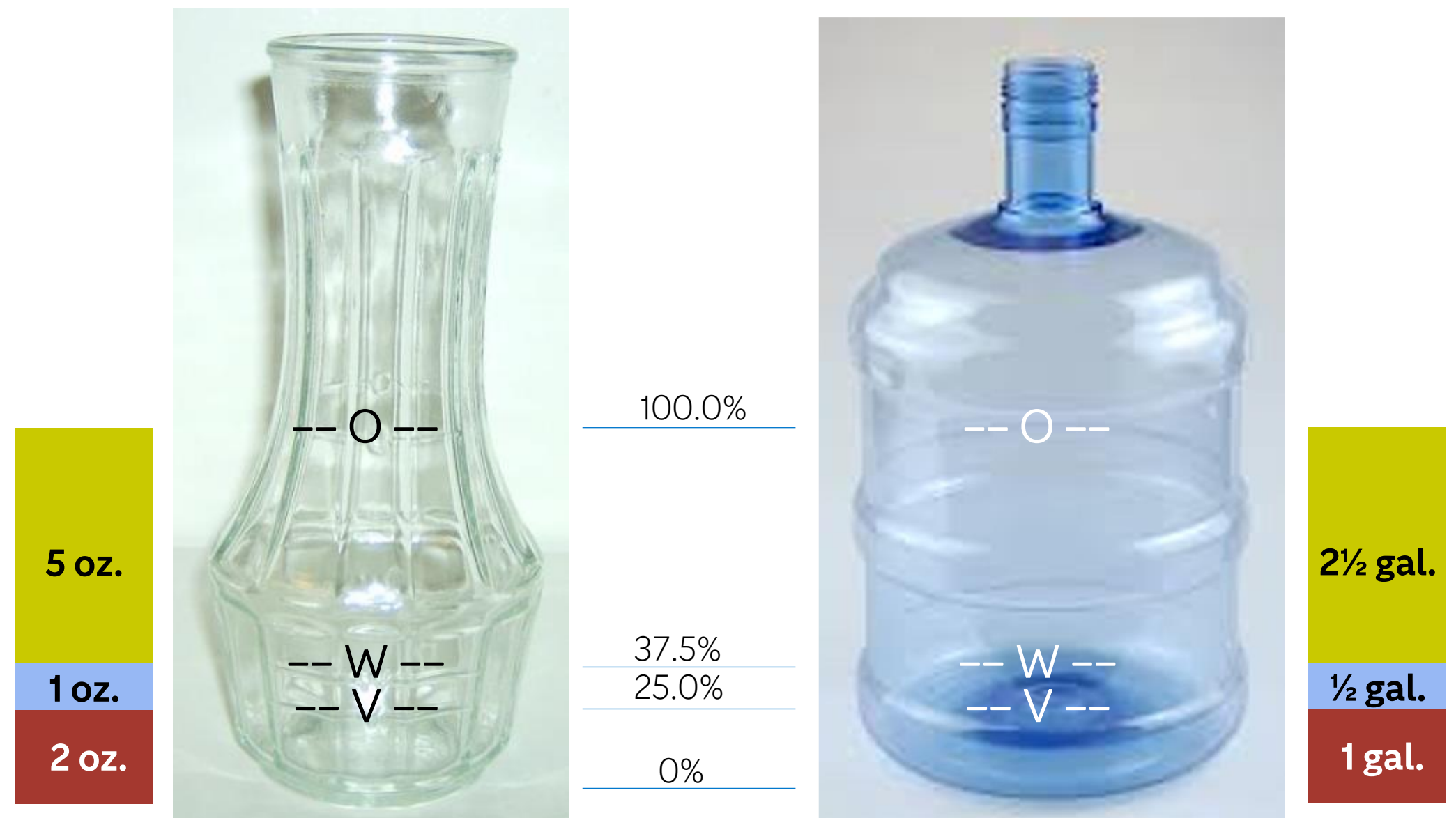
Making salad dressing is a simple 3-component blend of *Oil*, *Water*, & *Vinegar*



- Response depends on **proportions** not quantity.
- **Sum of proportions equals 1.** This *constraint* is what makes mixture DOE different.

Mixture or Formulation DOE

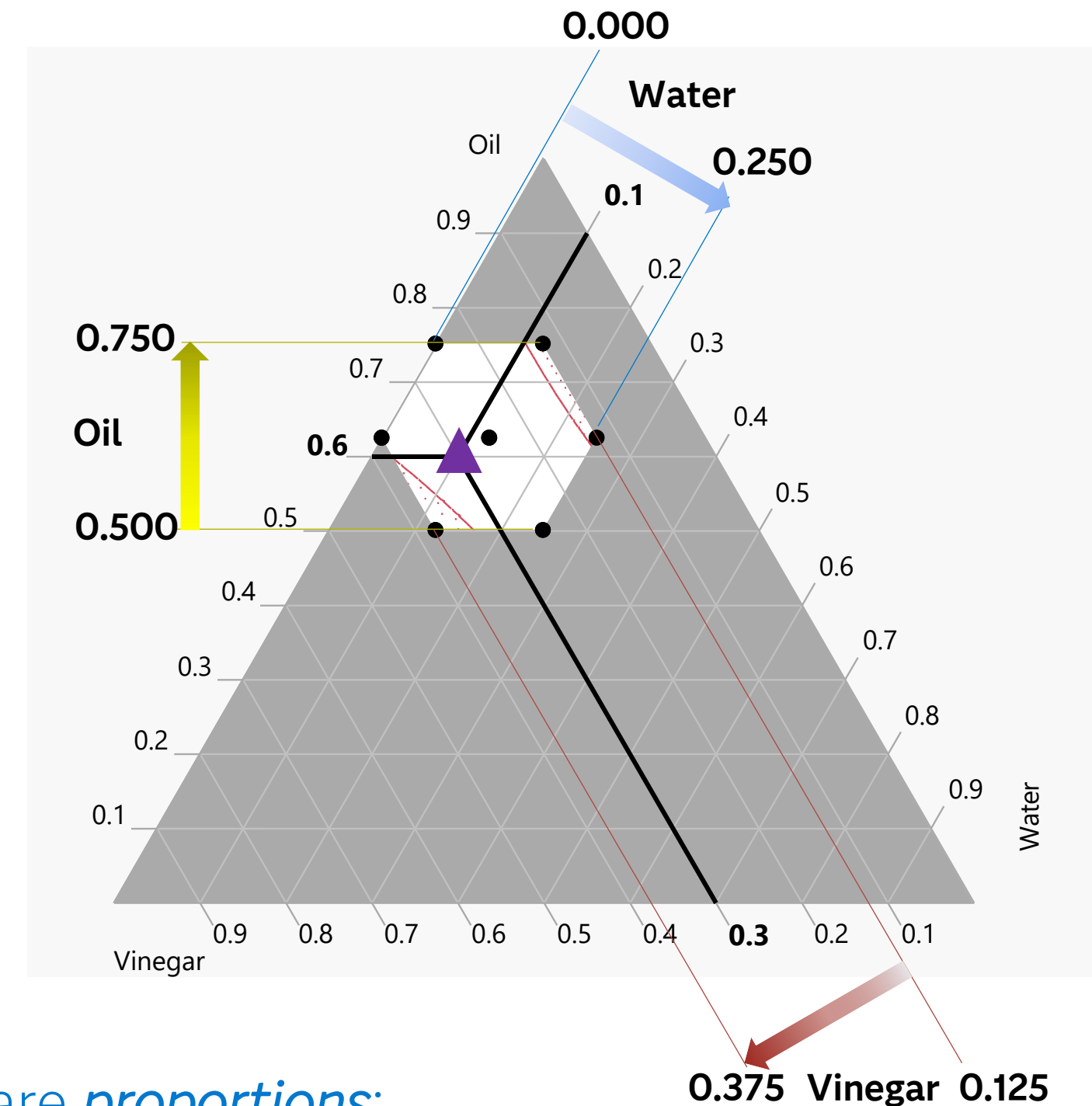
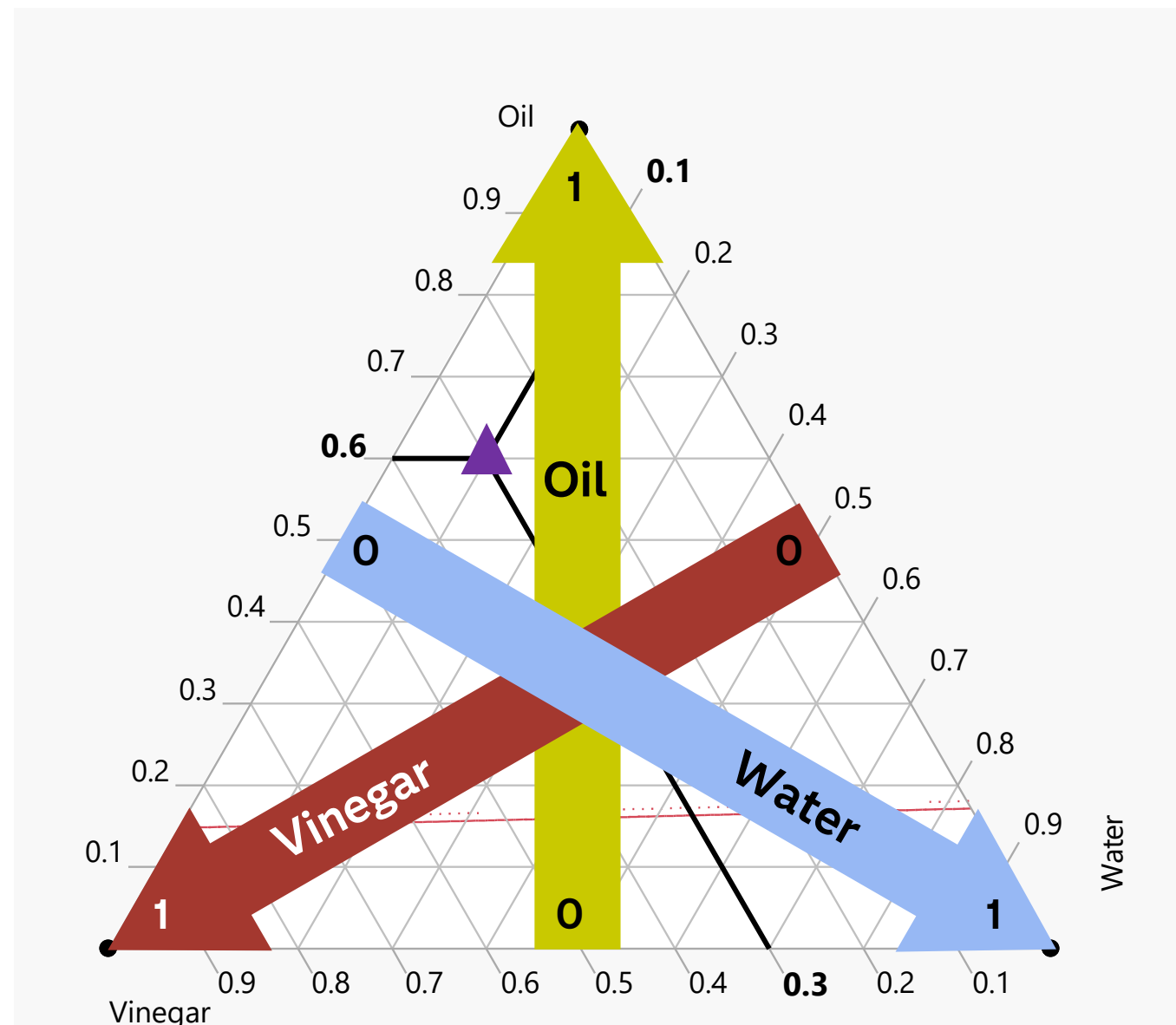
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- Response depends on **proportions** not quantity.
- **Sum of proportions equals 1.** This *constraint* is what makes mixture DOE different.

Use Ternary Plots to Visualize the Mixture Constraint

$$O + W + V = 1$$



Mixture components in a DOE use ranges that are *proportions*:

O: 0.500 to 0.750
W: 0.000 to 0.250
V: 0.125 to 0.375

If Oil = 0.6 and Vinegar = 0.3, then
Water = $1 - (0.6 + 0.3) = 0.1$ (See ▲)

Want to see something more complex than salad dressing?

2024

DISCOVERY SUMMIT

October 21-24
Cary, NC



Design of Experiments for Complex Biochemical Systems

Cell-free expression (CFE) systems are a suite of methods that reconstitute complex cellular functions like transcription, translation, and metabolism outside the confines of a living cell. CFE systems have numerous biotechnological uses in sensing, biomanufacturing, medicine, basic research, and education. Most CFE systems are made from combining cellular lysates with a complex blend of excipients that improve activity. While the number of excipients makes exploring the combinatorial spaces challenging, high-throughput experimentation with acoustic liquid handling makes it feasible to optimize formulations if paired with an appropriate statistical framework.

Here we describe our use of design of experiments (DOE) to optimize excipient combinations for specific use cases of CFE. **We pair our DOE with functional data analysis (FDA)** to collapse activity over time measurements to metrics readily used for analysis. Initial formulation DOE examples range from five to 14 components. We further describe our efforts to push to higher scales, attempting **mixture-process DOE designs with as many as 42 components** using an experimental set-up that allows for 1,536 formulations to be tested at once.

Presenters



Matthew Lux



John Davies



David Garcia

8 of 45 Provided Video Links on Functional Data Analysis (FDA)

[Modeling Spectral Data with JMP Pro 17](#) Presentation to the Statistics in Defense & National Security (SDNS) section of the American Statistical Association (ASA) by **Chris Gotwalt**, Chief Data Scientist – 1-hour, 2023

[An Introduction to Spectral Data Analysis with Functional Data Explorer in JMP Pro 17](#)

Ryan Parker & Clay Barker Research Statistician Developers – 25-min, 2023

[Developer Tutorial: Modeling Spectral Data with JMP Pro 17](#) **Chris Gotwalt & Ryan Parker**,

– 1 & 1/4-hour, 2024

Case Study Applications of Functional Data Analysis by **Tom Donnelly**, Principal Systems Engineer

- [Modeling Streamed Sensor Data with Functional Data Analysis](#) – 1-hour, JMP Discovered 2019
- [Using Sensor Stream Data as Both an Input and Output in a Functional Data Analysis](#) – 24-min, DATAWorks 2022
- [Design of Experiments for Reverse Engineering Formulations](#) – 45-min, Technically Speaking 2024

[A Preview of Functional Data Analysis for Modeling and Simulation Validation](#) **Curtis Miller, Research Staff, Institute for Defense Analyses (IDA)** – 34-min, DATAWorks 2024

[Design of Experiments for Complex Biochemical Systems](#) **Matthew Lux, John Davies, & David Garcia, Research Scientists, US Army DEVCOM Chemical Biological Center (CBC)** – 10-min, Discovery 2024





Review of Functional Data Analysis (FDA)

Functional Data Analysis (FDA) is a branch of statistics that analyzes data providing information about curves, surfaces, or anything else varying over a continuum.

Traditional Rectangular Data

		Batch	X1	X2	Y
1		001	1.00	1.00	2.17
2		002	0.94	1.01	0.00
3		003	1.06	1.01	2.70
4		004	0.94	0.99	0.26
5		005	1.06	0.99	2.87
6		006	1.00	1.00	1.97

Functional Data

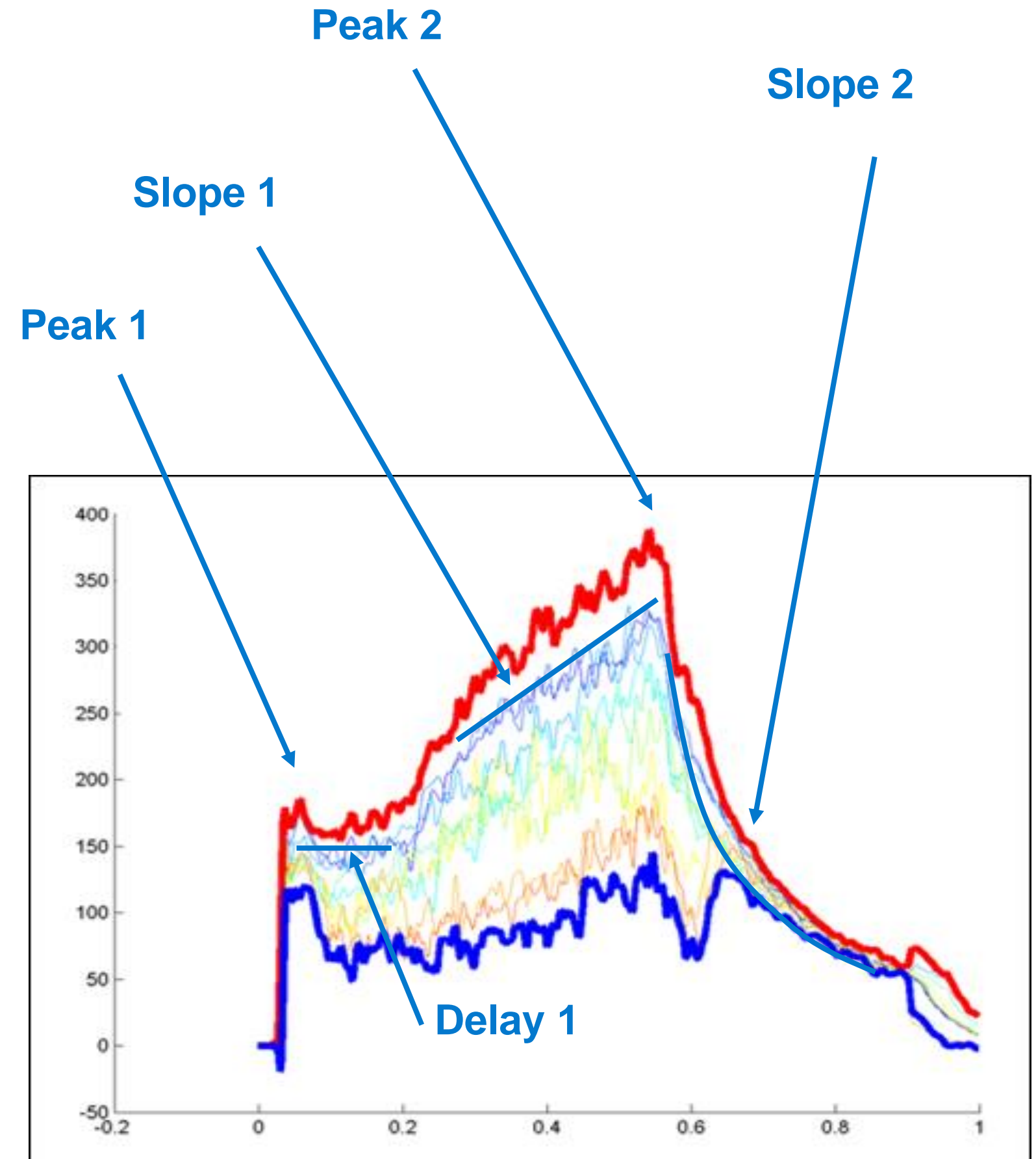
	Batch	X1	X2	Y
1	001	5.6	6.5	
2	002	5.3	8.15	
3	003	8.3	6.85	
4	004	6.9	7.6	

The *curve* is the fundamental unit of observation

Landmark Analysis

Moderately effective non-FDA option,
but NOT as good as using FDA

Does not use information from the
whole curve



Based on slide from David Harrison of Lockheed Martin Corporation

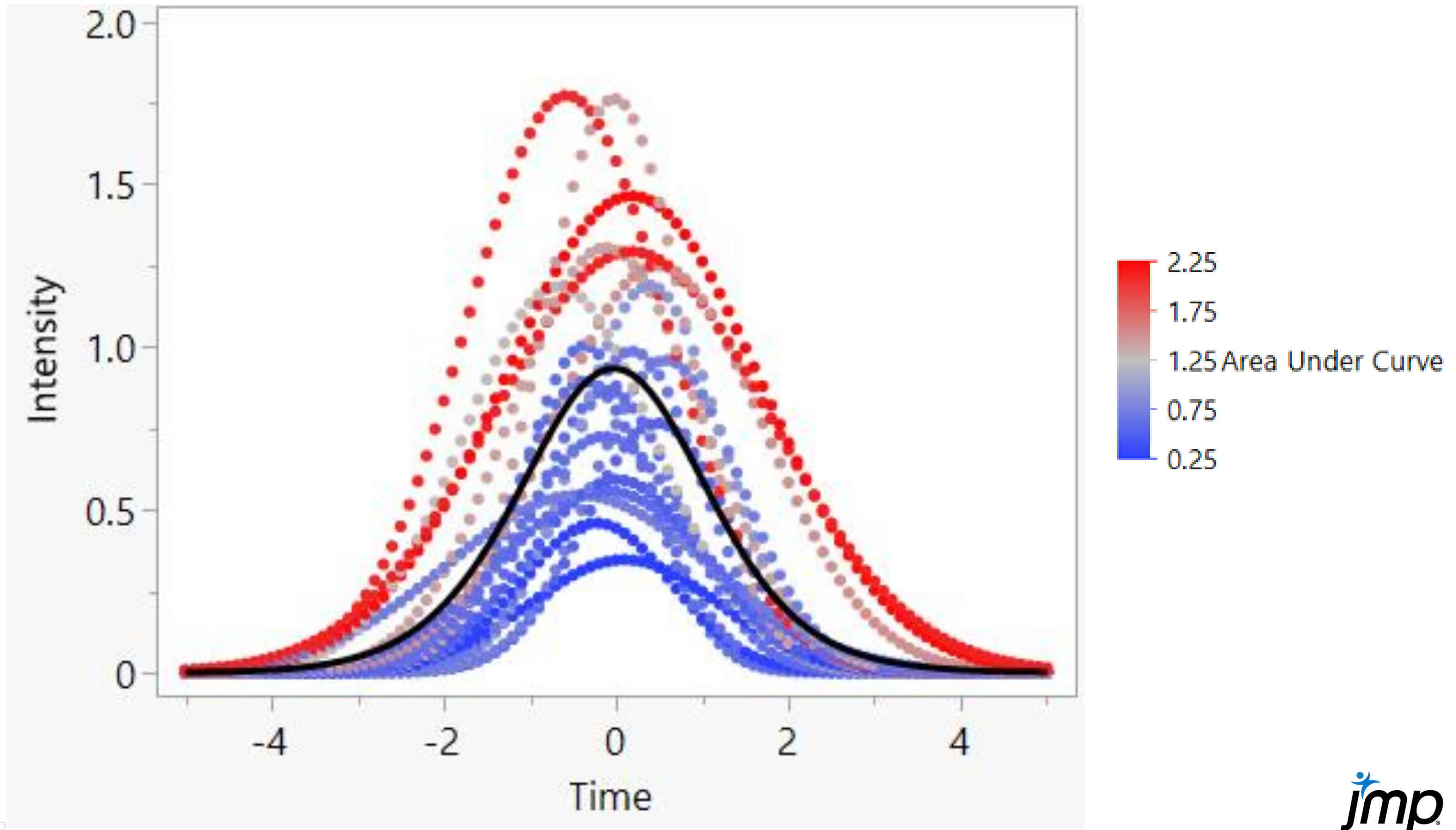
FDA Examples

- Sensor streams
- Measurements taken over a range
- Vibration signals
- **Spectral data**
- Radar/sonar signatures
- Trajectories of flights between cities
- Electrocardiograms (EKGs)
 - *...and more!*
- *Almost any response in a longitudinal order*

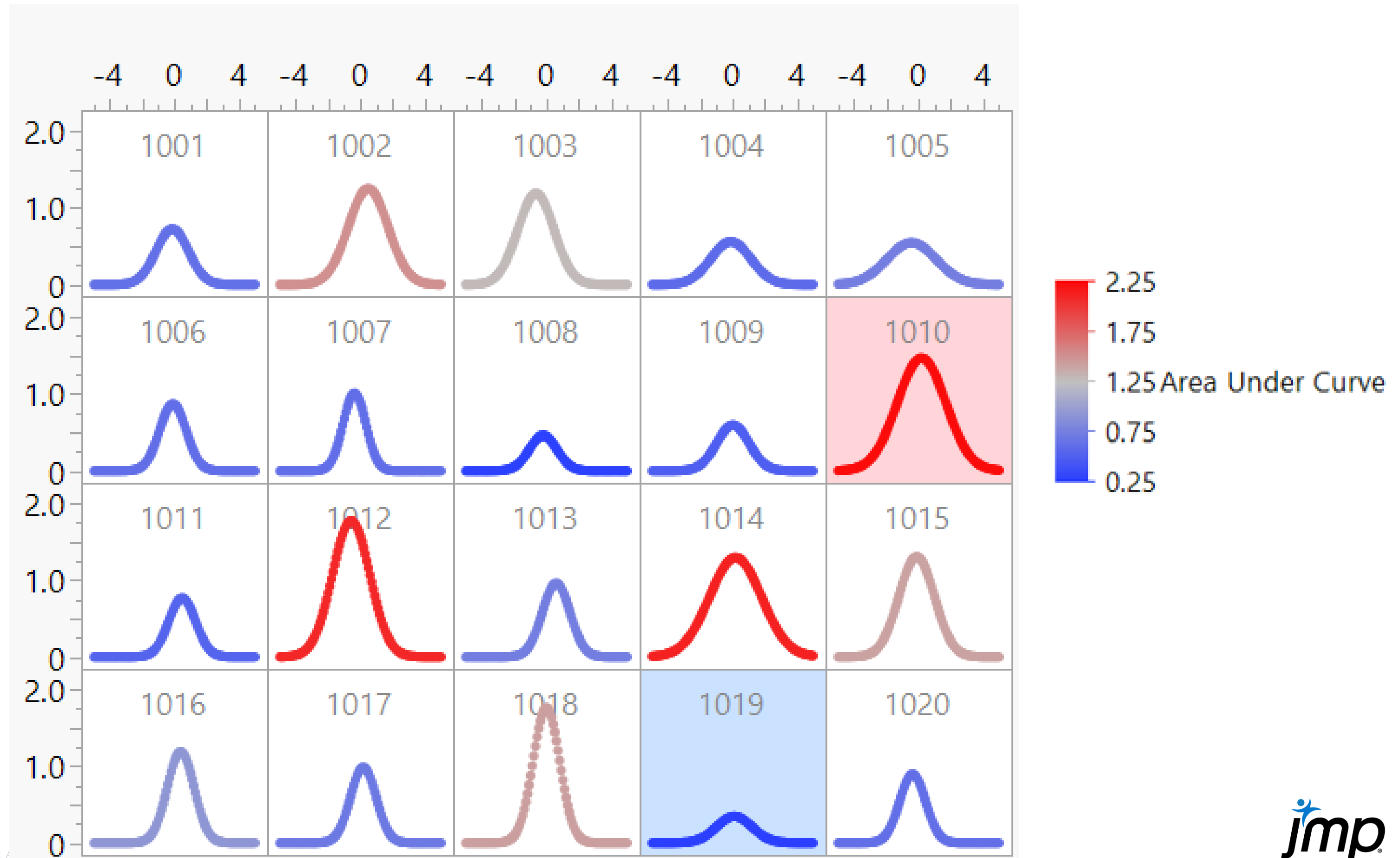
FUNCTIONAL DATA ANALYSIS

- Use Functional Principal Components Analysis (FPCA) to do dimension reduction and break “curve” data into *FPC Scores* & *Shape Components*
 - FPC Scores explain *function-to-function variation*
 - Shape Components explain the *longitudinal variation* (e.g., *time*, *distance*, *frequency*, or *wavelength*)
- Fit models with FPC scores, cluster and graph them - *just like any other continuous data*
- *Model the FPC scores as functions of the DOE factors*

FUNCTIONAL DATA ANALYSIS

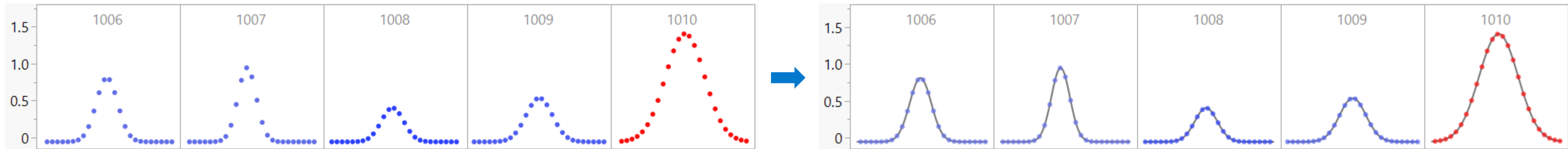


FUNCTIONAL DATA ANALYSIS

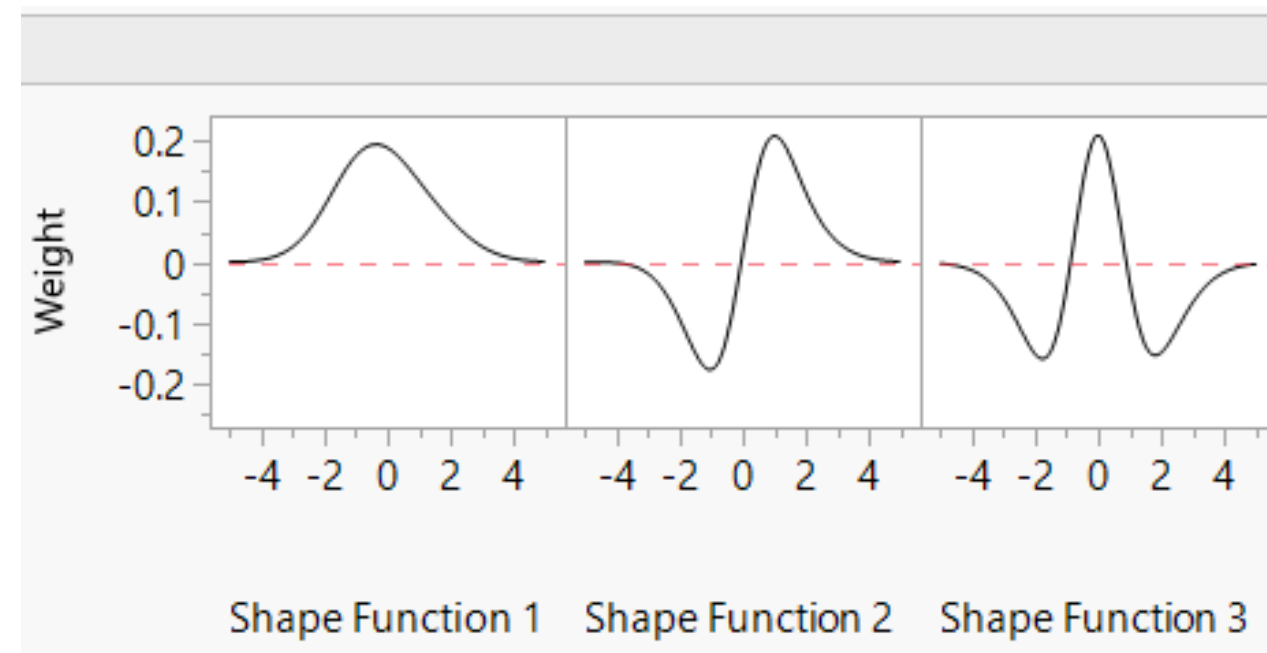


FUNCTIONAL DATA ANALYSIS

1. Convert streams of data into functions - “smoothly connect the dots.”



2. Do FPCA to create
 - a) **Shape Functions** to explain the longitudinal variation.
 - b) **FPC scores** to explain function-to-function variation.

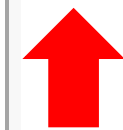
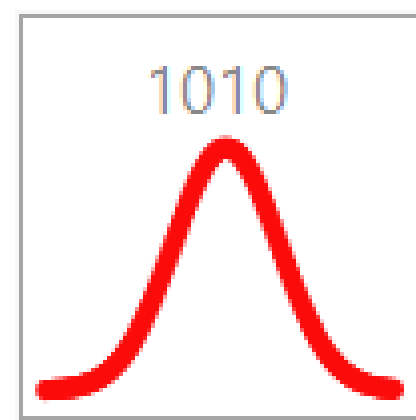


Function Summaries			
Batch	FPC 1	FPC 2	FPC 3
1006	-0.97	-0.30	0.48
1007	-0.86	-1.13	0.54
1008	-2.33	-0.48	-0.22
1009	-1.61	-0.07	-0.15
1010	3.42	1.05	-0.76

FUNCTIONAL DATA ANALYSIS

3. Products of FPC scores multiplying their corresponding shape functions, when added to the Mean shape closely reproduce the original (batch) raw function curves.

Batch	FPC 1	FPC 2	FPC 3
1001	-1.08	-0.32	0.01
1002	1.39	1.77	-0.29
1003	1.02	-1.86	-0.44
1004	-1.42	-0.24	-0.48
1005	-1.20	-0.56	-0.91
1006	-0.97	-0.30	0.48
1007	-0.86	-1.13	0.54
1008	-2.33	-0.48	-0.22
1009	-1.61	-0.07	-0.15
1010	3.42	1.05	-0.76
1011	-1.53	0.99	-0.00
1012	3.78	-2.15	-0.10
1013	-0.91	1.57	-0.01
1014	2.80	0.88	-1.07
1015	1.63	-0.21	0.40
1016	-0.07	1.45	0.64
1017	-0.75	0.55	0.67
1018	2.14	0.15	1.90
1019	-2.53	-0.08	-0.51
1020	-0.91	-1.03	0.29

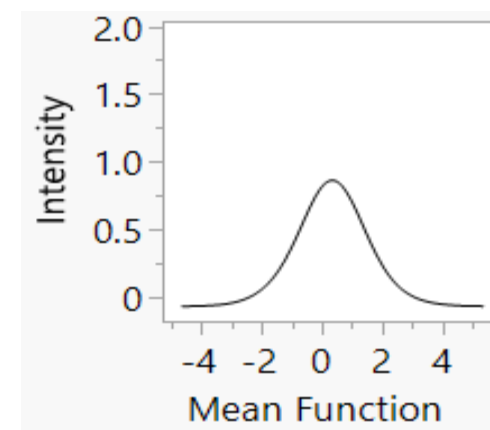


+3.42 ·

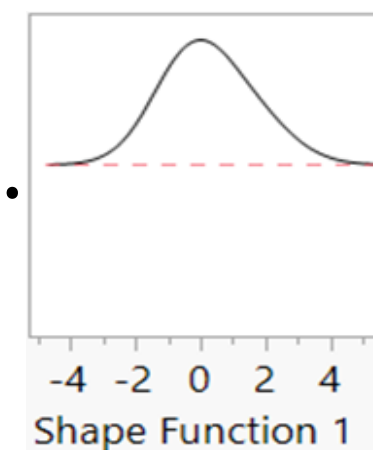
+1.05 ·

−0.76 ·

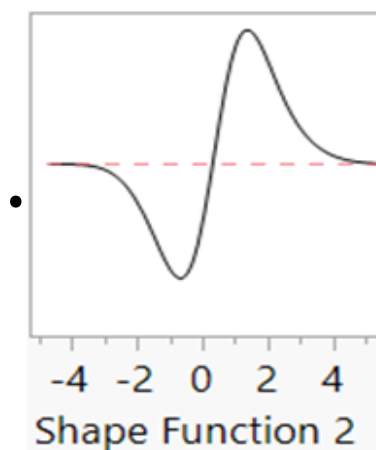
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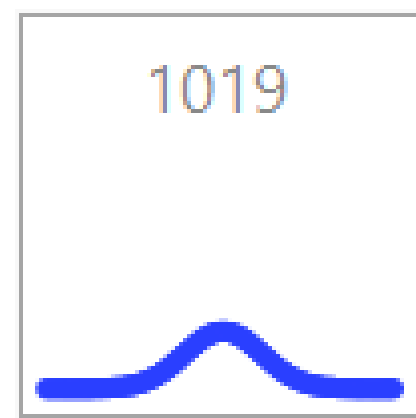
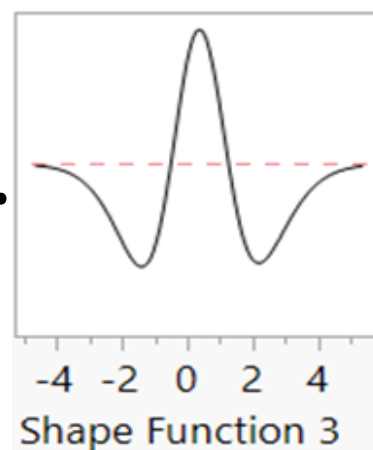
+FPC1 ·



+FPC2 ·



+FPC3 ·

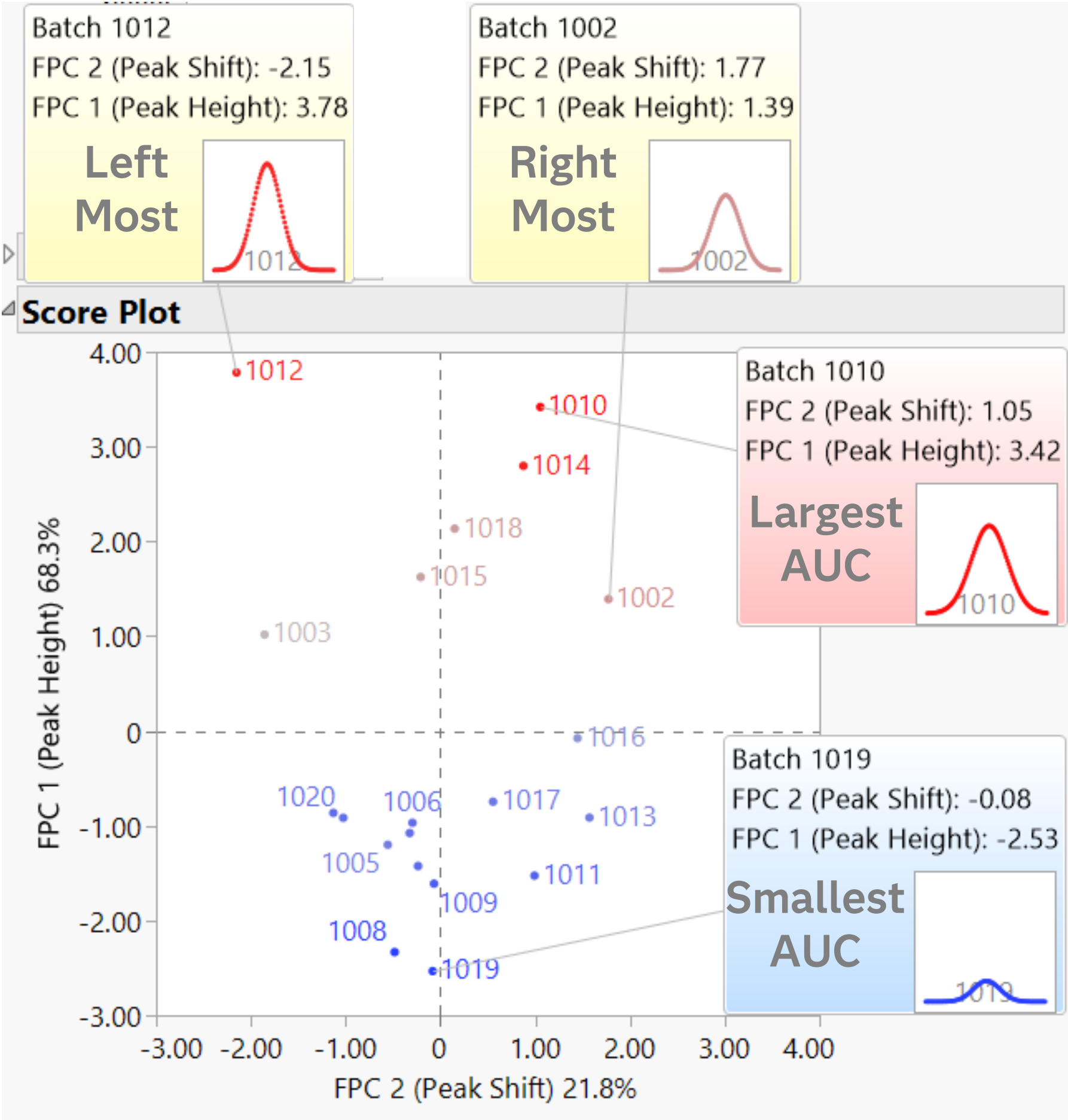
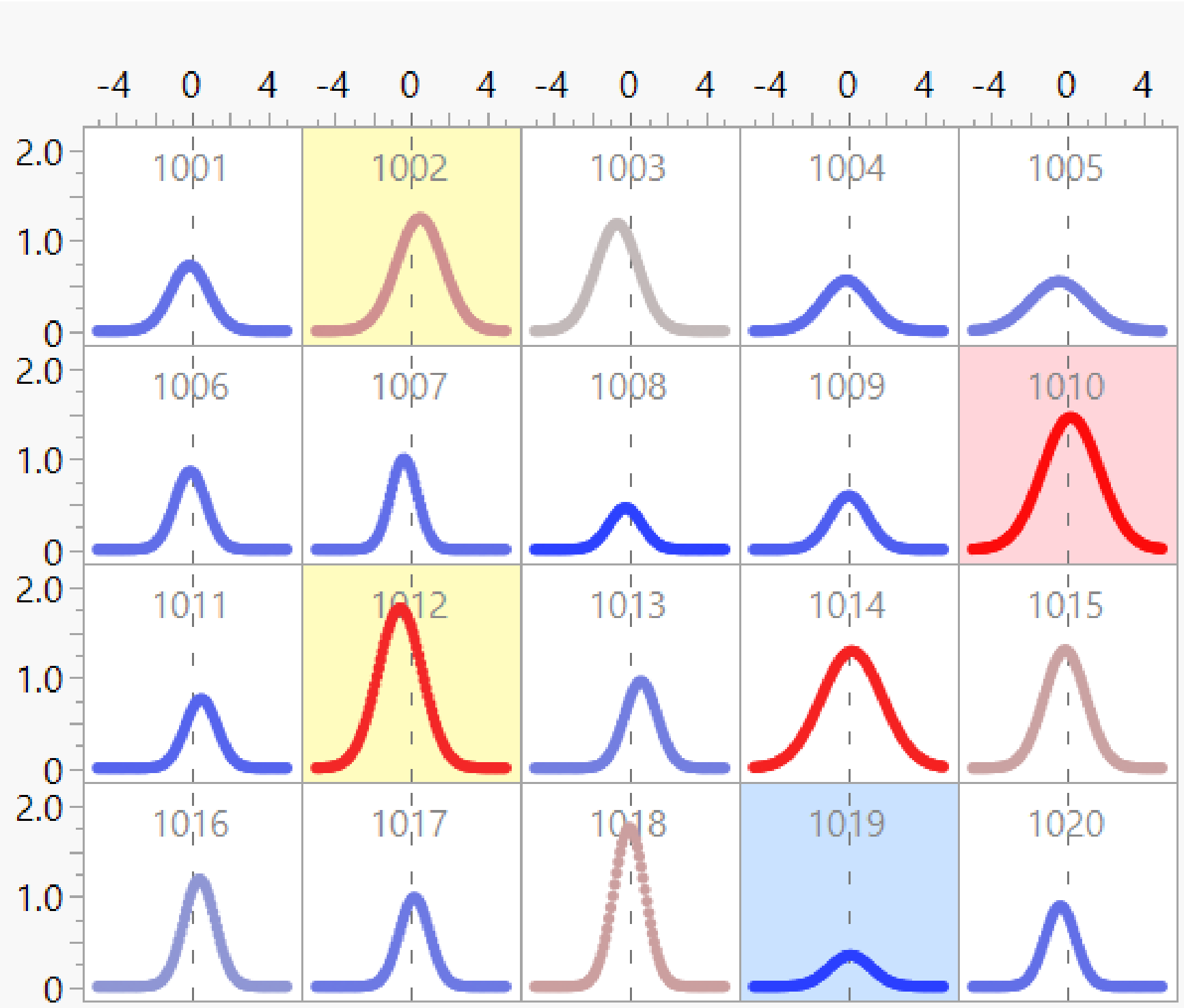


−2.53 ·

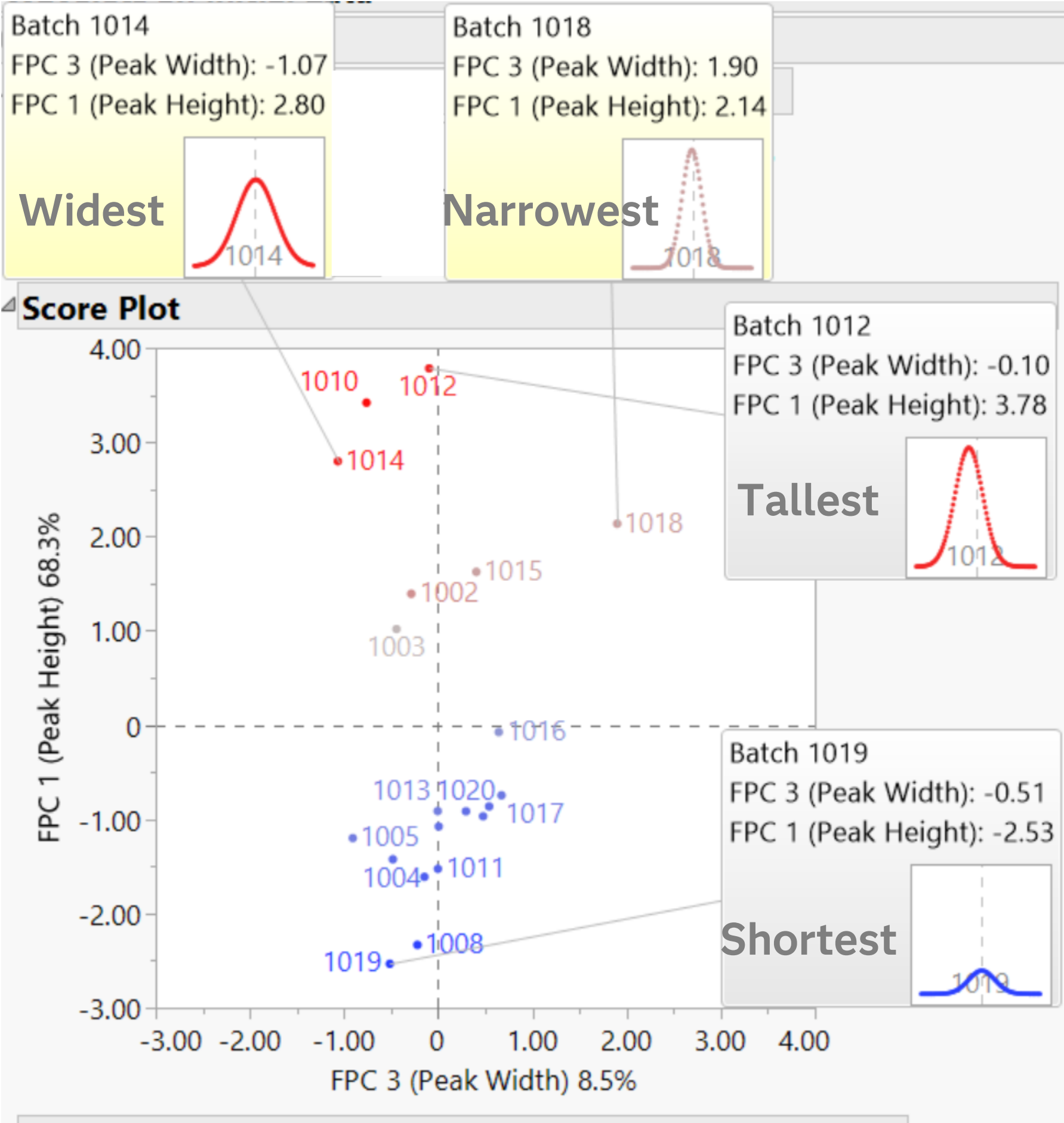
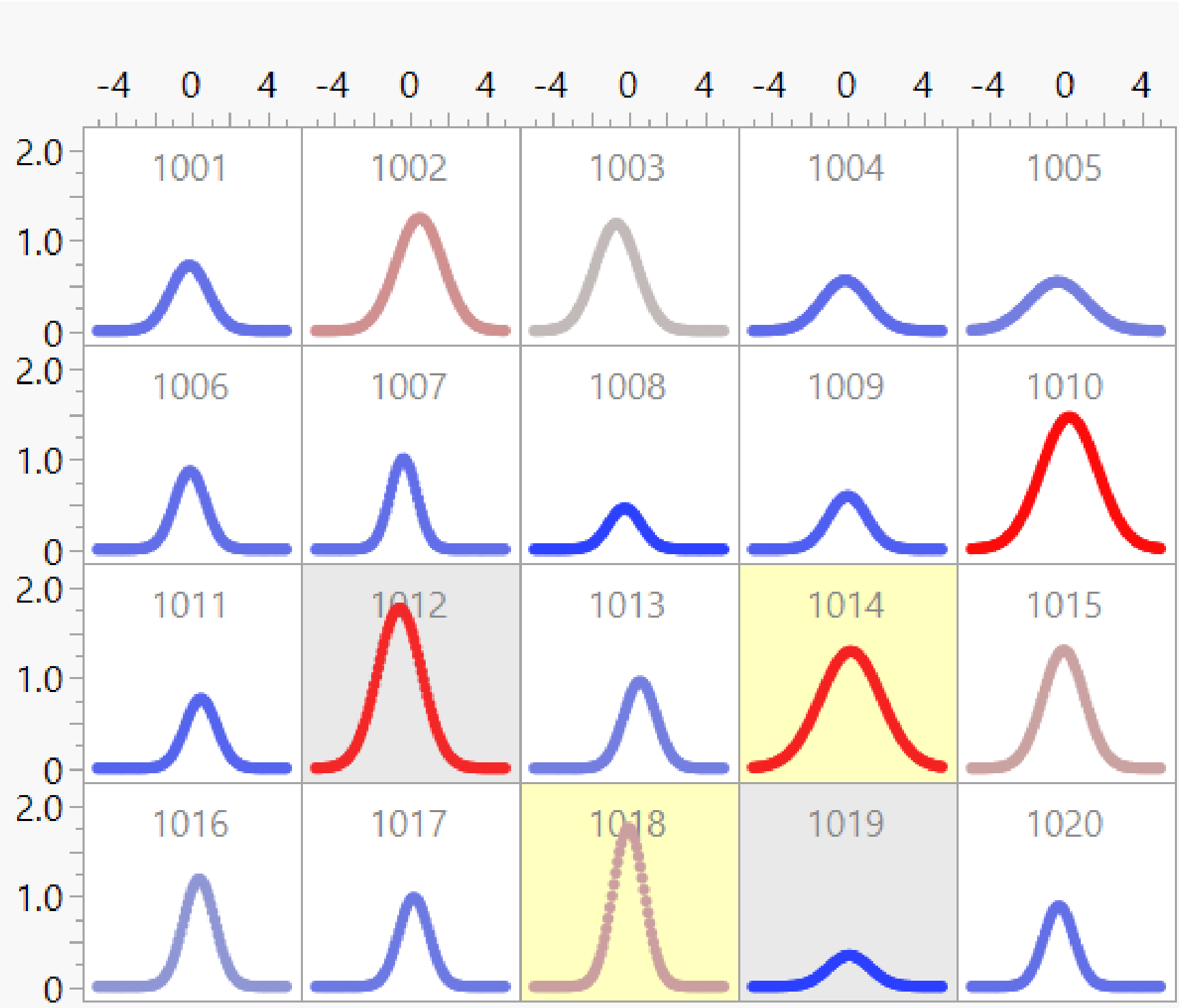
−0.08 ·

−0.51 ·

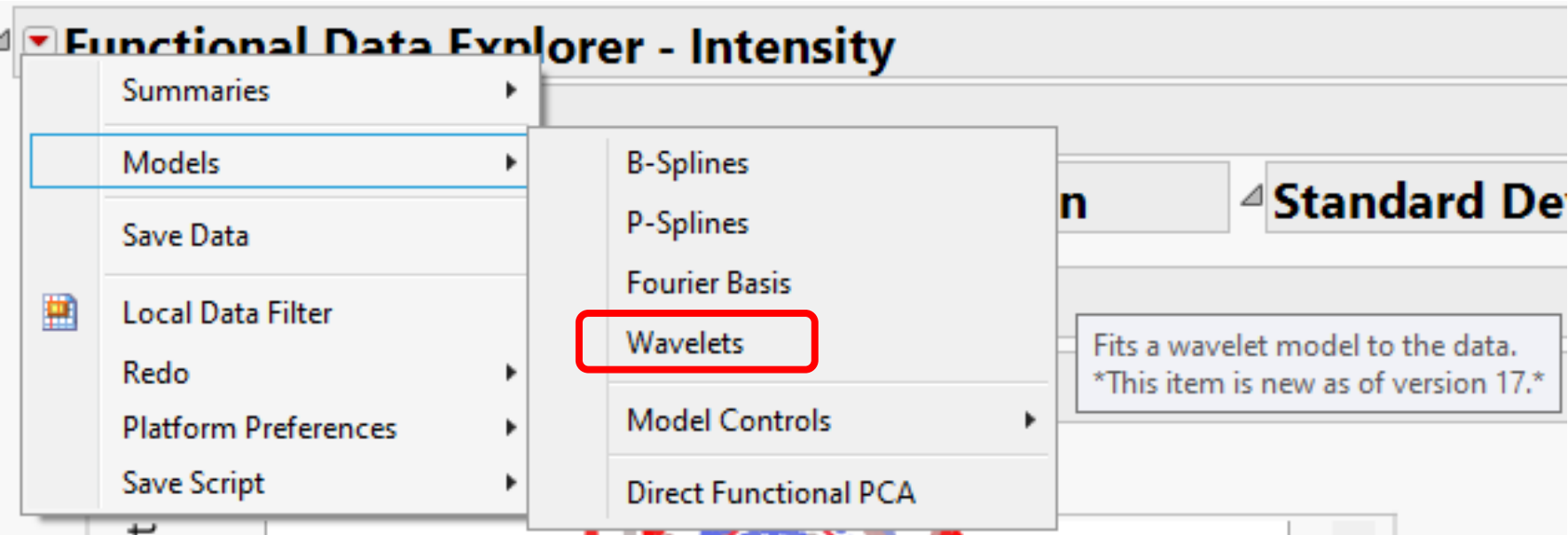
FUNCTIONAL DATA ANALYSIS



FUNCTIONAL DATA ANALYSIS



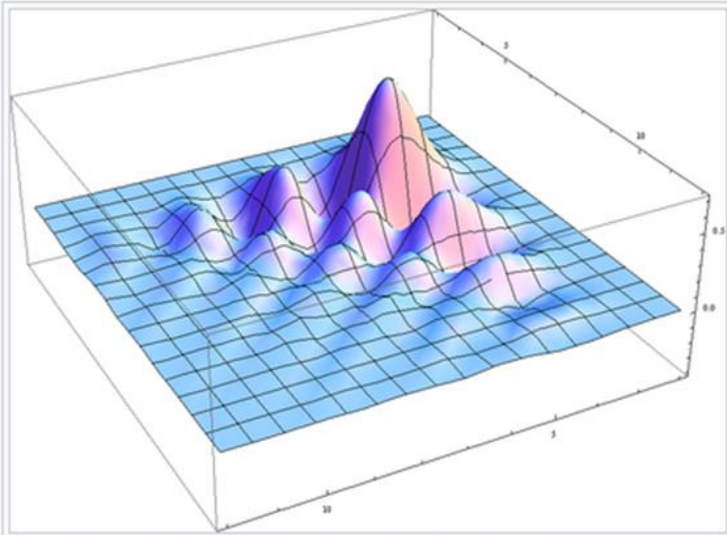
Wavelets often Outperform Splines & Fourier Basis Functions



The **Daubechies wavelets**, based on the work of Ingrid Daubechies, are a family of **orthogonal wavelets** defining a **discrete wavelet transform** and characterized by a maximal number of vanishing **moments** for some given **support**. With each wavelet type of this class, there is a scaling function (called the *father wavelet*) which generates an orthogonal **multiresolution analysis**.

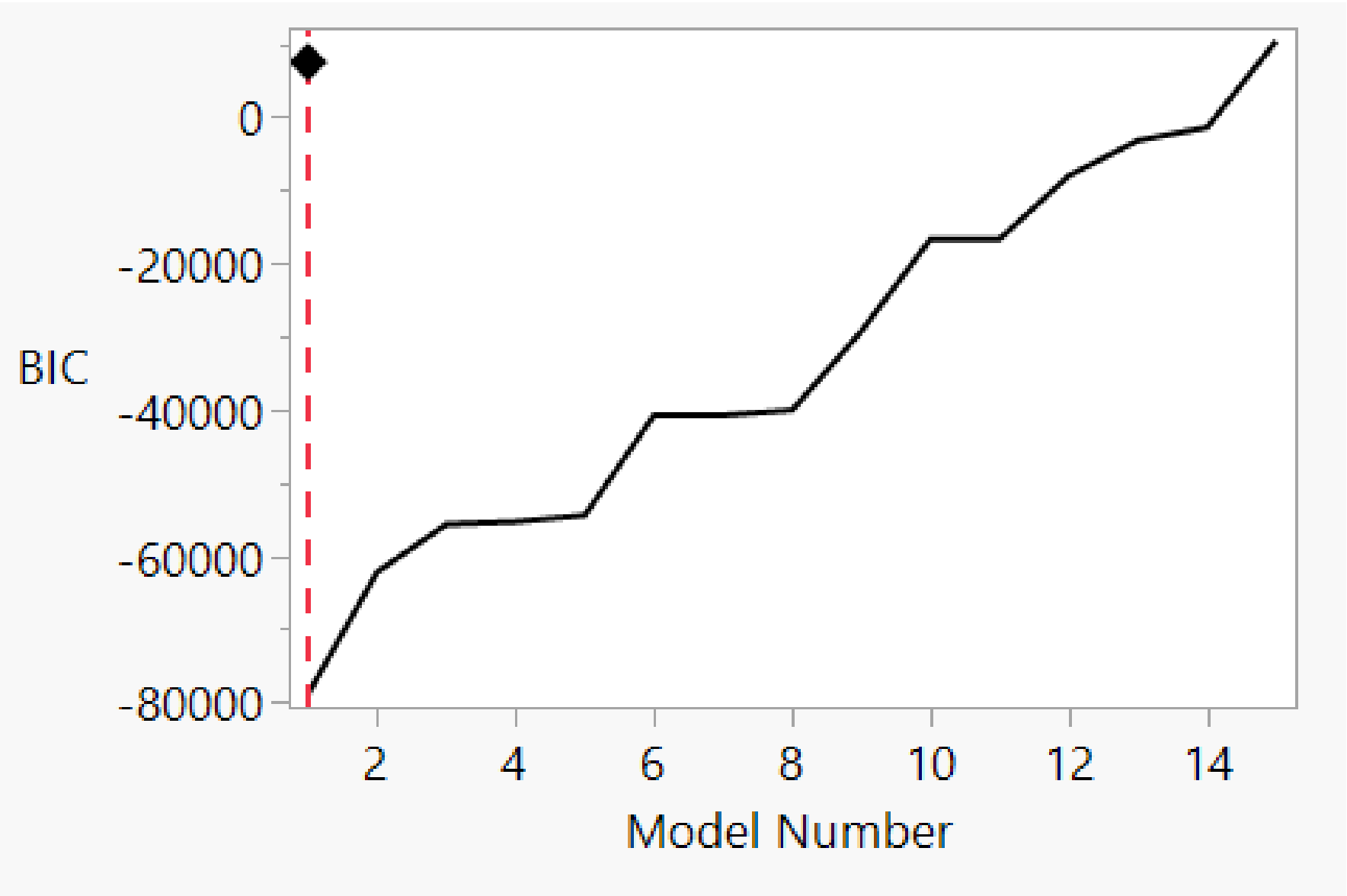
Properties [\[edit \]](#)

In general the Daubechies wavelets are chosen to have the highest number *A* of vanishing moments, (this does not imply the best smoothness) for given support width (number of coefficients) $2A$.^[1] There are two naming schemes in use, *DN* using the length or number of taps, and *dbA* referring to the number of vanishing moments. So *D4* and *db2* are the same wavelet transform.



Daubechies 20 2-d wavelet (Wavelet Fn X Scaling Fn)


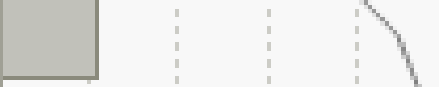

A **wavelet** is a wave like oscillation with an amplitude that begins at zero, increases or decreases, and then returns to zero one or more times. They are used to approximate more complex functions.



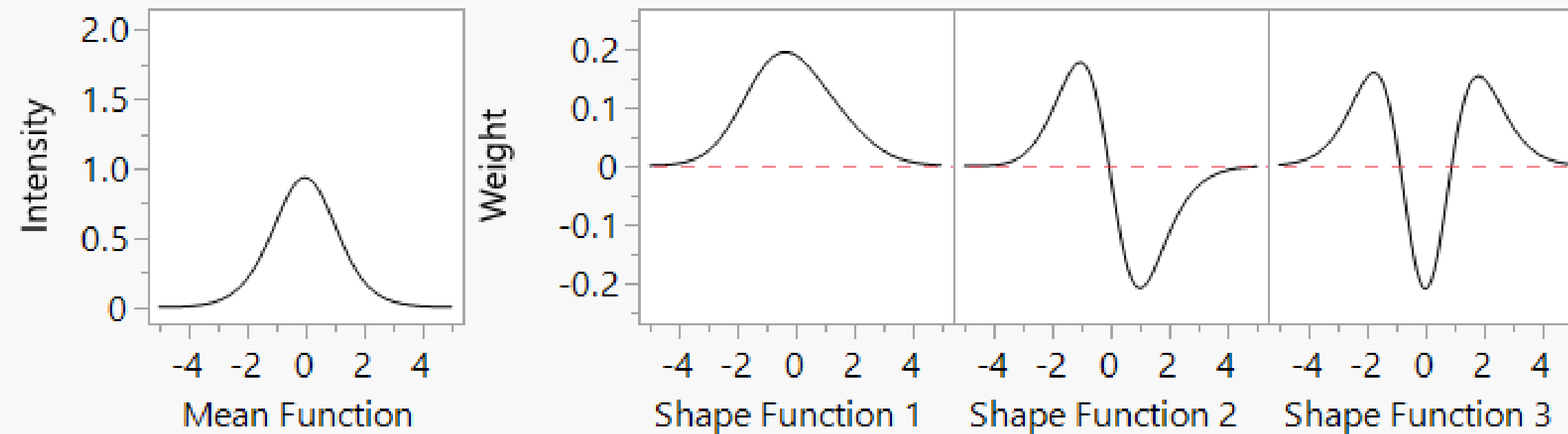
Model	Wavelet	AICc	BIC	GCV
1	Daubechies 20	-59532.1	-78876.4	3.44e-15
2	Symlet 20	-44379.4	-62187.8	1.35e-11
3	Symlet 10	-52644.6	-55665.3	5.25e-10
4	Daubechies 10	-52369.7	-55315.7	6.27e-10
5	Coiflet 5	-48479.4	-54470.6	8.06e-10
6	Daubechies 6	-39144.6	-40758.9	9.397e-7
7	Symlet 6	-39174.2	-40758.8	9.423e-7
8	Coiflet 3	-39355	-40067.7	1.448e-6
9	Symlet 4	-30273.7	-29262.9	0.000388
10	Coiflet 1	-19733.8	-16681.6	0.363082
11	Daubechies 2	-19678.2	-16665.7	0.358012
12	Haar	-11619.8	-8022.99	45.13531
13	Biorthogonal 1.3	-5971.84	-3170.2	257.5009
14	Biorthogonal 4.4	-2245.76	-1401.35	368.4419
15	Biorthogonal 2.6	11632.9	10392.76	96774.19

FUNCTIONAL DATA ANALYSIS

Component Strength

FPC	Eigenvalue	20 40 60 80	Percent	Cumulative
1	3.6484		68.3%	68.3%
2	1.1660		21.8%	90.1%
3	0.4546		8.51%	98.6%

Shape Functions



longitudinal variation


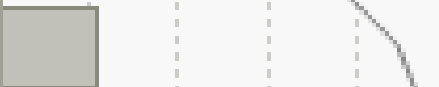
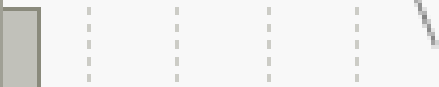
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11	1011	-1.53	0.99	-0.00
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13	1013	-0.91	1.57	-0.01
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15	1015	1.63	-0.21	0.40
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17	1017	-0.75	0.55	0.67
18	1018	2.14	0.15	1.90
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*function-to-function
variation*

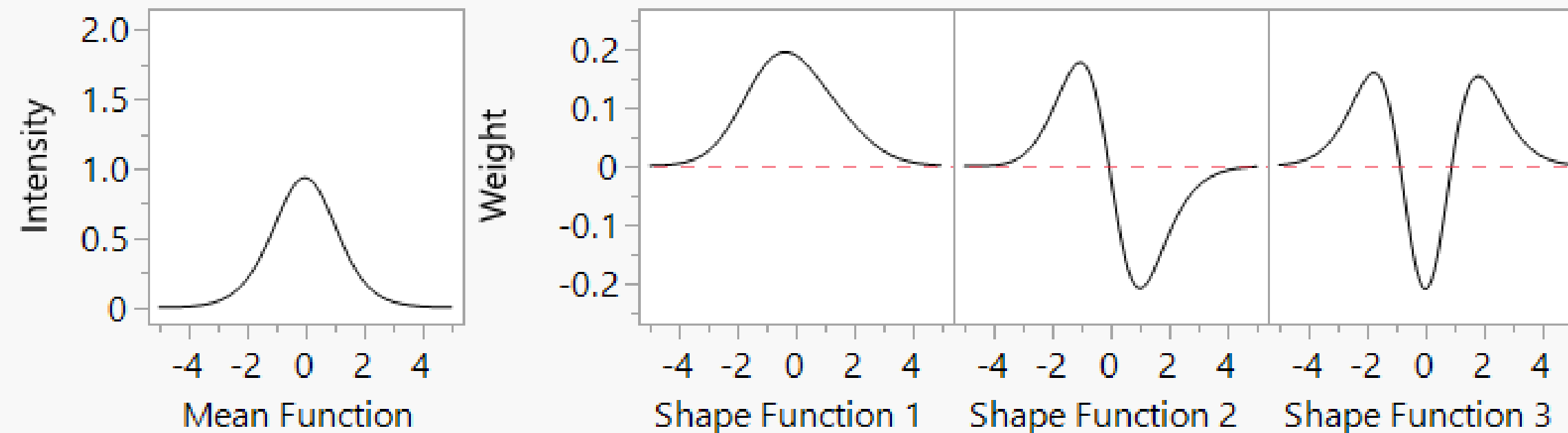


FUNCTIONAL DATA ANALYSIS

Component Strength

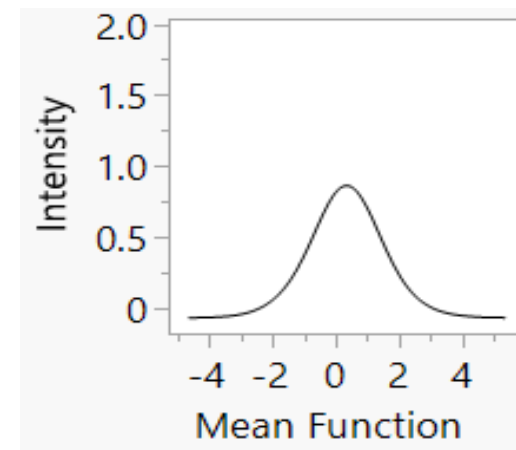
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Shape Functions

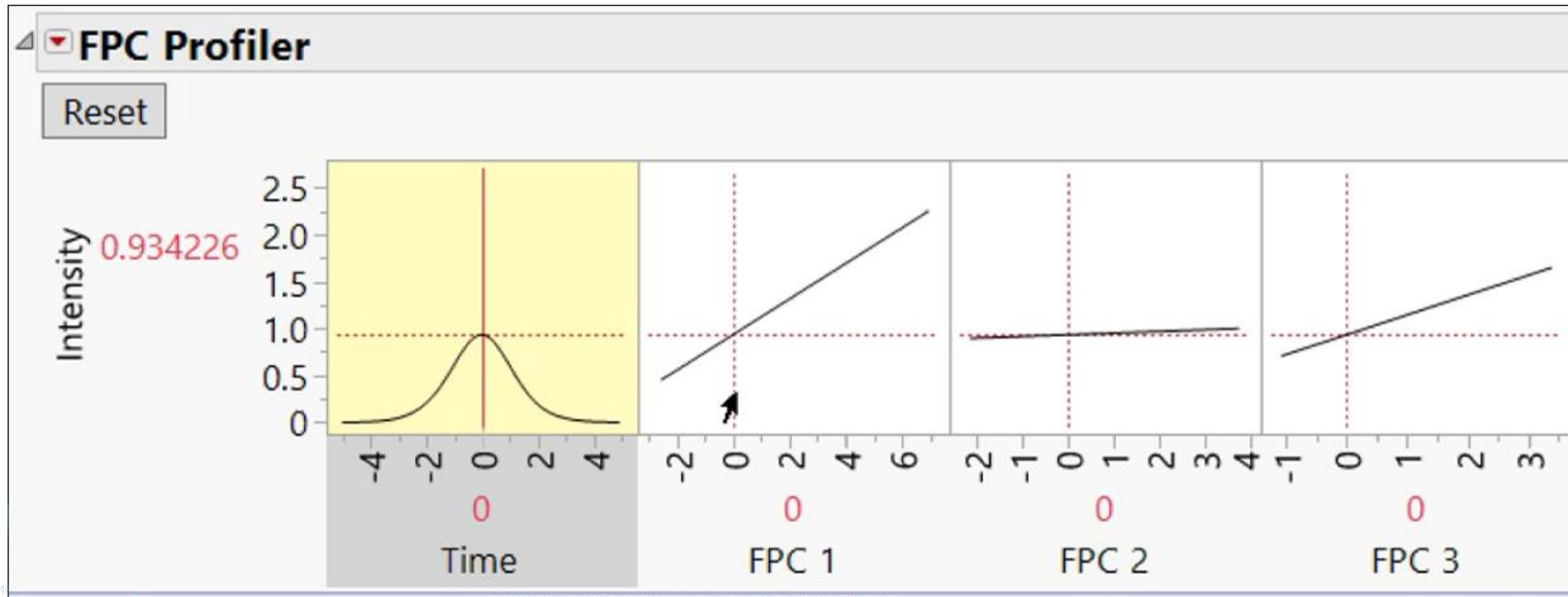


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19	1019	-2.53	-0.08	-0.51
20	1020	-0.91	-1.03	0.29

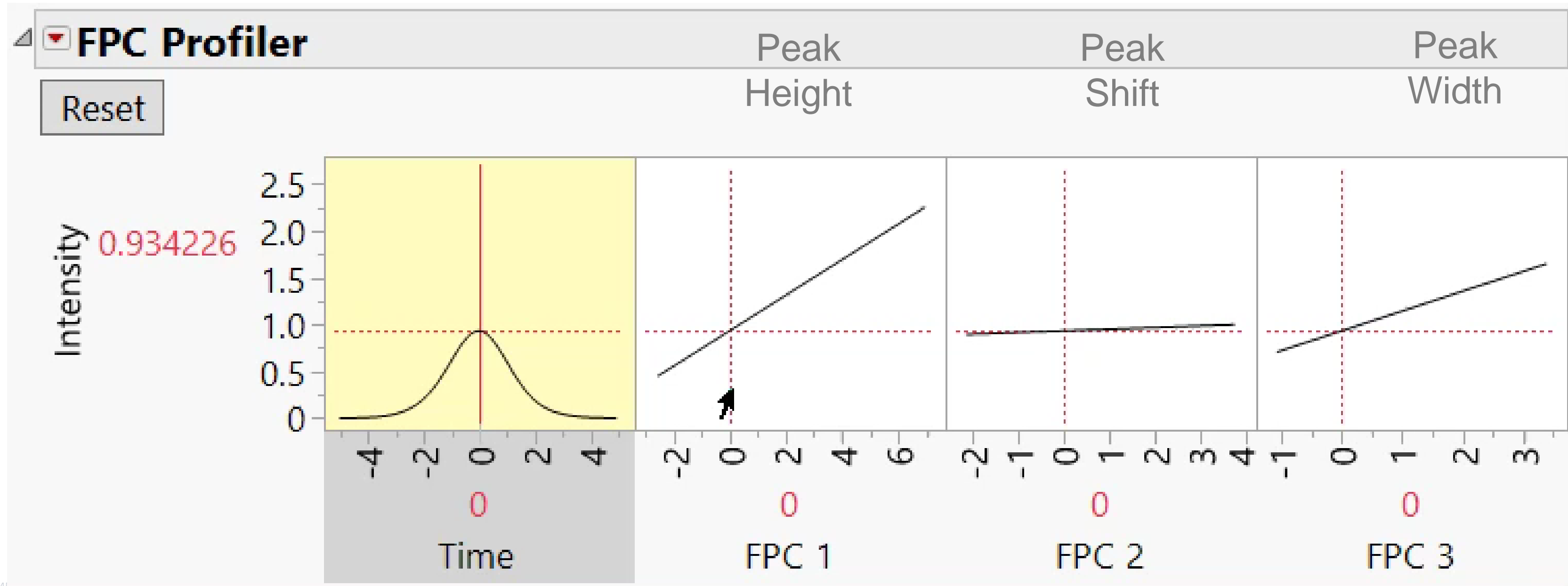
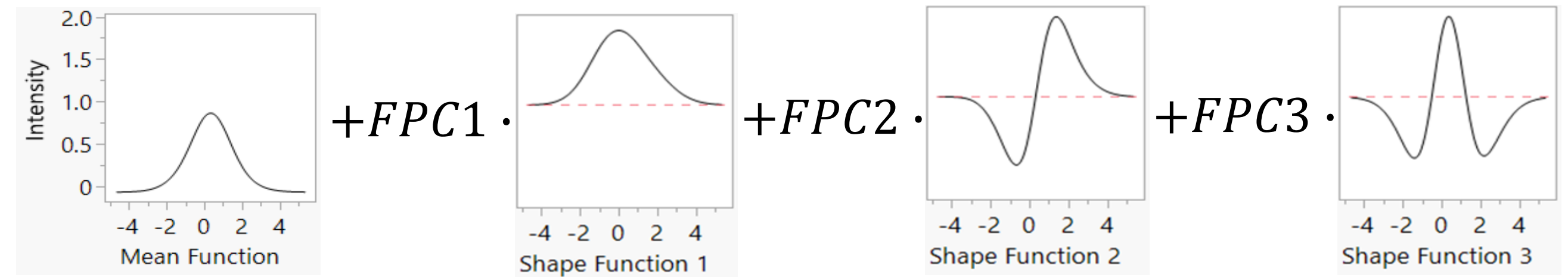
FUNCTIONAL DATA ANALYSIS



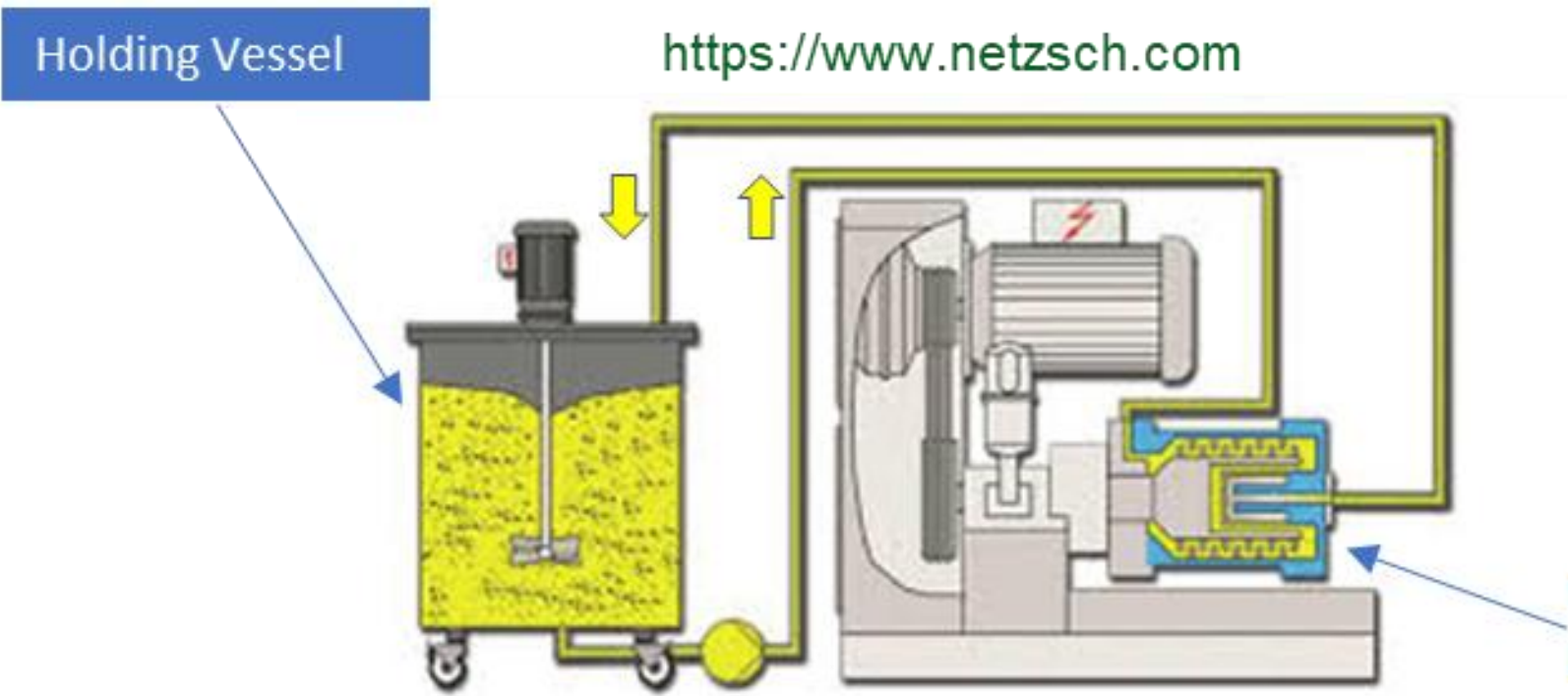
When
FPC Scores \rightarrow Mean Curve
all zero



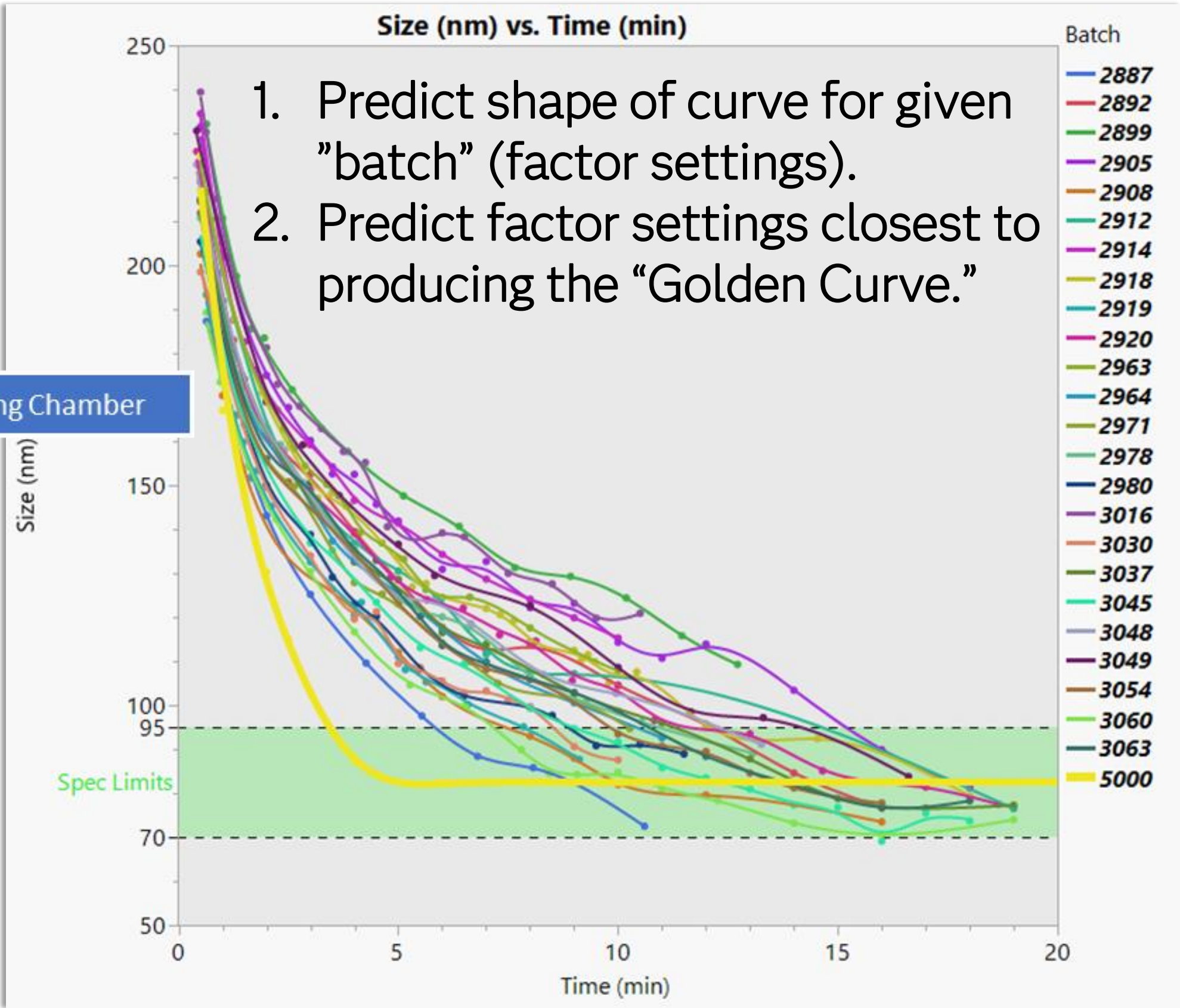
FUNCTIONAL DATA ANALYSIS



FDA-DOE Example



Batch	Run Order	%Beads	%Active	Flow	Temperature	Trial Type
2887	1	90	25	150	45	Design
2892	2	80	25	350	15	Design
2899	3	80	15	550	15	Design
2905	4	80	15	150	45	Design
2908	5	90	25	150	15	Design
2912	6	90	15	150	30	Design
2914	7	85	15	150	15	Design
2918	8	90	15	550	15	Design
2919	9	90	25	550	15	Design
2920	10	90	15	350	45	Design
2963	11	80	20	150	15	Design
2964	12	85	20	350	30	Design
2971	13	80	25	150	45	Design
2978	14	80	25	550	30	Design
2980	15	85	25	550	45	Design
3016	16	80	15	550	45	Design
3030	17	90	20	550	45	Design



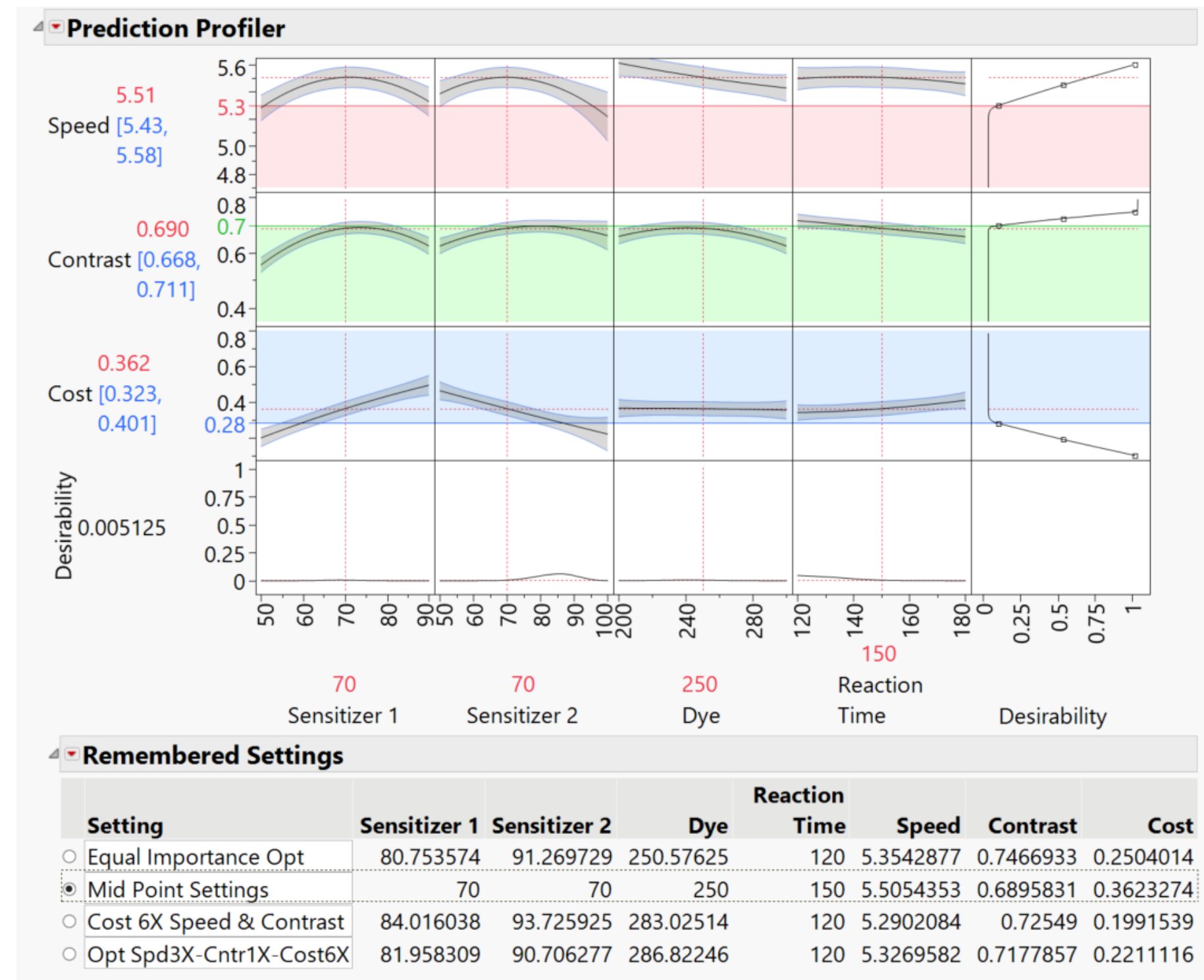
Outline

- Why / What DOE?
- What is Functional Data Analysis (FDA)?
- Reverse Engineering Case #1 – Modeling alcohol blends
- Reverse Engineer Case #2 – Mineral formulations

Takeaway #1

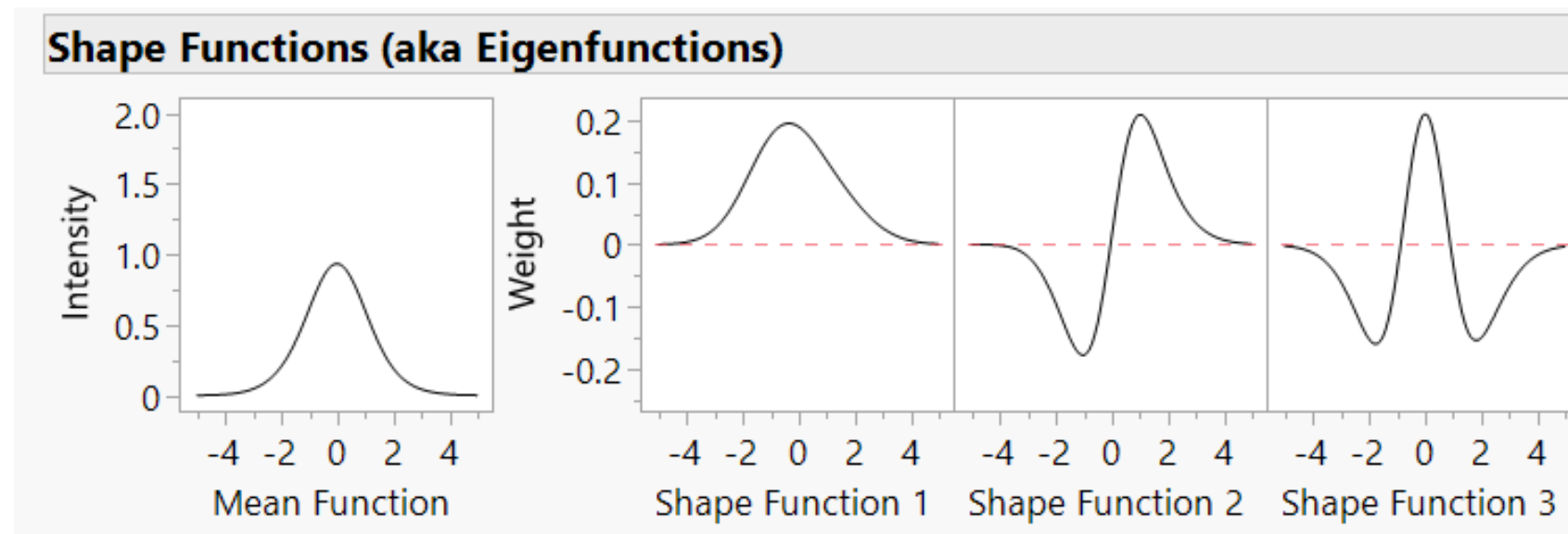
There's no better way to get the most information from the least amount of data than to use Design of Experiments methods

	Sensitizer 1	Sensitizer 2	Dye	Reaction Time	Speed	Contrast	Cost
7/4	90	90	300	180	5.59	0.73	0.73
27/0	50	50	200	120	4.79	0.36	0.17
1	50	50	250	120	5.36	0.616	0.198
2	50	50	200	180	5.39	0.537	0.175
3	90	70	200	120	5.31	0.623	0.447
4	50	90	200	150	5.13	0.431	0.177
5	70	70	250	180	5.37	0.643	0.445
6	50	90	300	120	4.79	0.375	0.231
7	90	90	200	180	5.45	0.626	0.471
8	90	50	250	150	5.00	0.470	0.670
9	50	50	300	150	5.22	0.478	0.283
10	70	90	200	120	5.41	0.668	0.226
11	90	90	250	120	5.33	0.734	0.310
12	50	50	250	120	5.32	0.574	0.257
13	70	50	200	150	5.49	0.596	0.456
14	50	70	250	180	5.22	0.558	0.166
15	70	70	250	150	5.57	0.689	0.390
16	90	90	300	150	5.26	0.653	0.226
17	70	70	250	150	5.47	0.688	0.356
18	70	70	300	120	5.42	0.657	0.337
19	50	70	200	120	5.43	0.518	0.222
20	50	50	300	150	5.15	0.505	0.287
21	90	70	200	120	5.33	0.661	0.457
22	50	90	300	120	4.97	0.411	0.191
23	90	50	300	120	5.09	0.492	0.588
24	90	50	300	180	5.03	0.358	0.733
25	70	70	250	150	5.59	0.707	0.318
26	70	90	300	180	5.25	0.605	0.290
27	50	90	200	150	5.24	0.476	0.177



Takeaway #2

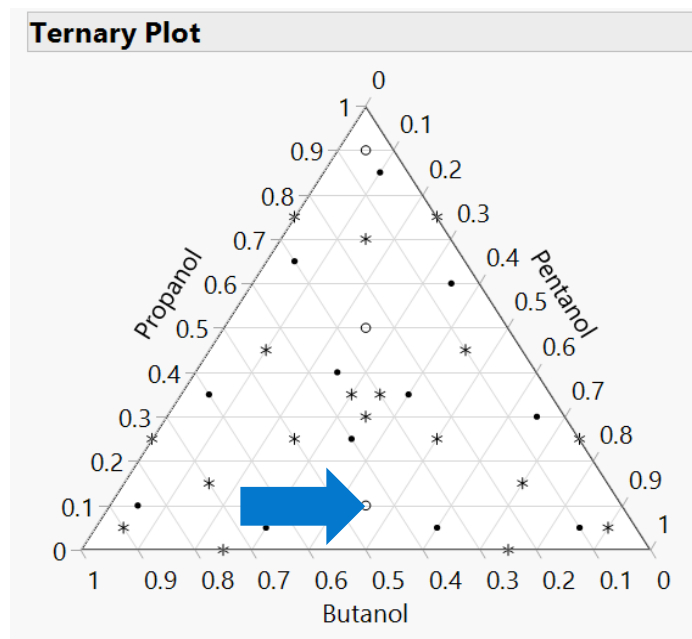
- FDA breaks apart highly correlated longitudinal data like spectra into two parts:
 - 1. **Shape functions** – explaining the **longitudinal variation**
 - 2. **FPC Scores** – explaining the **function-to-function variation**



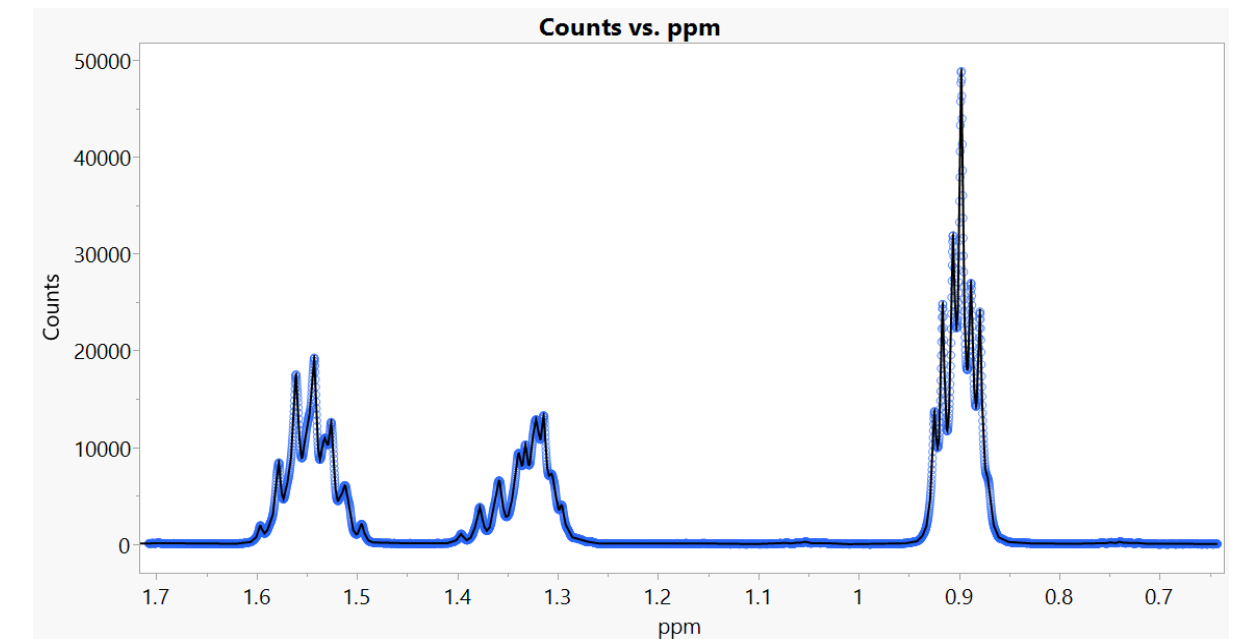
	Batch	FPC 1	FPC 2	FPC 3
1	1001	-1.08	-0.32	0.01
2	1002	1.39	1.77	-0.29
3	1003	1.02	-1.86	-0.44
4	1004	-1.42	-0.24	-0.48
5	1005	-1.20	-0.56	-0.91
6	1006	-0.97	-0.30	0.48

Takeaway #3

- FDA using wavelets can be combined with mixture DOE analysis to build models that **predict spectra as a function of formulation component proportions.**

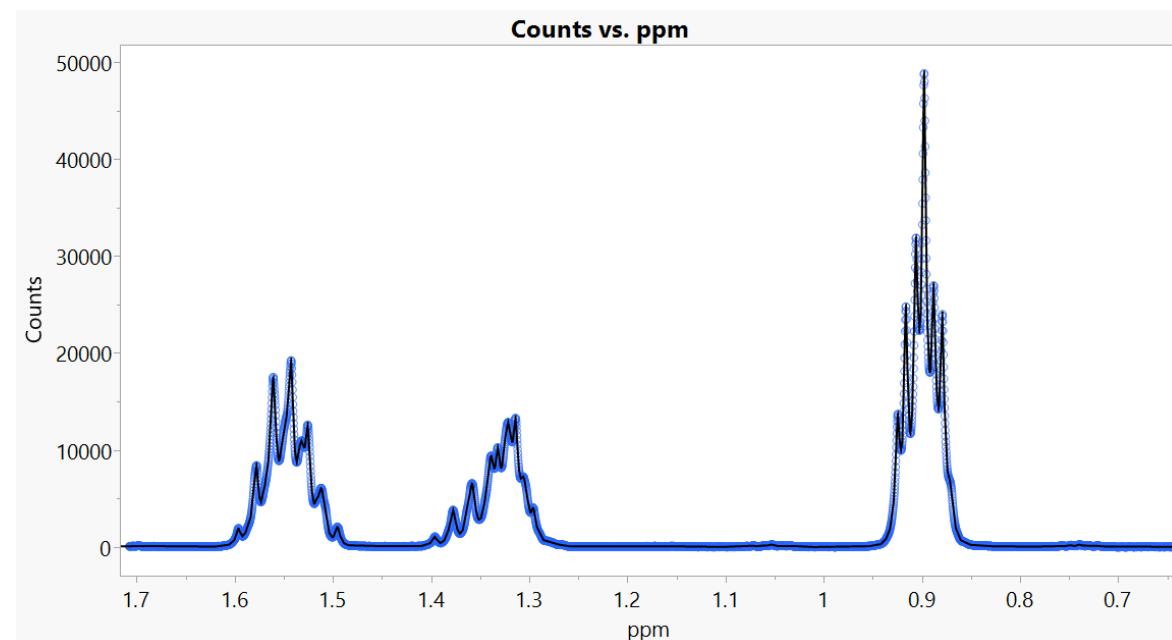


**FDA-DOE
Model**

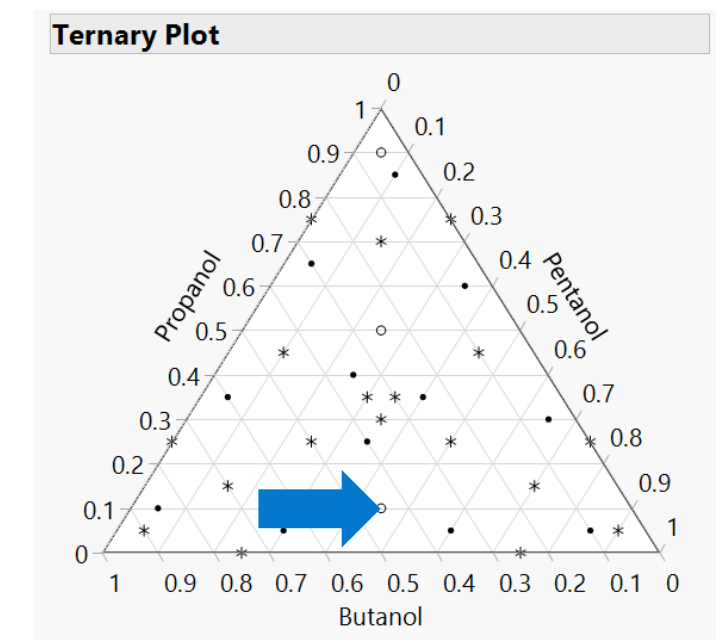


Takeaway #4

- Using spectra for an unknown blend as a “target” and an FDA-DOE mixture model, one can **predict formulation component proportions**.
Reverse Engineer it!



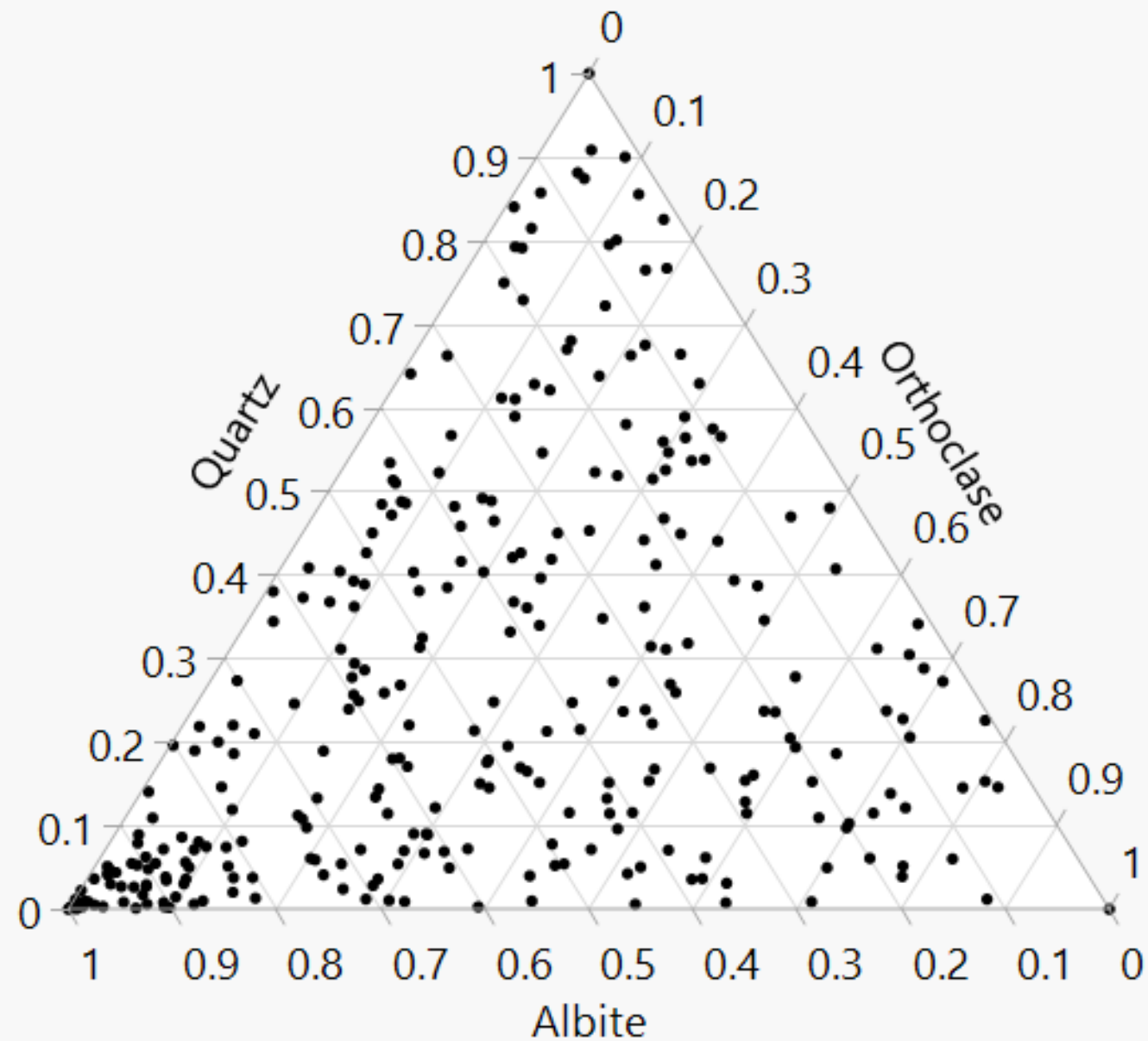
**FDA-DOE
Model**



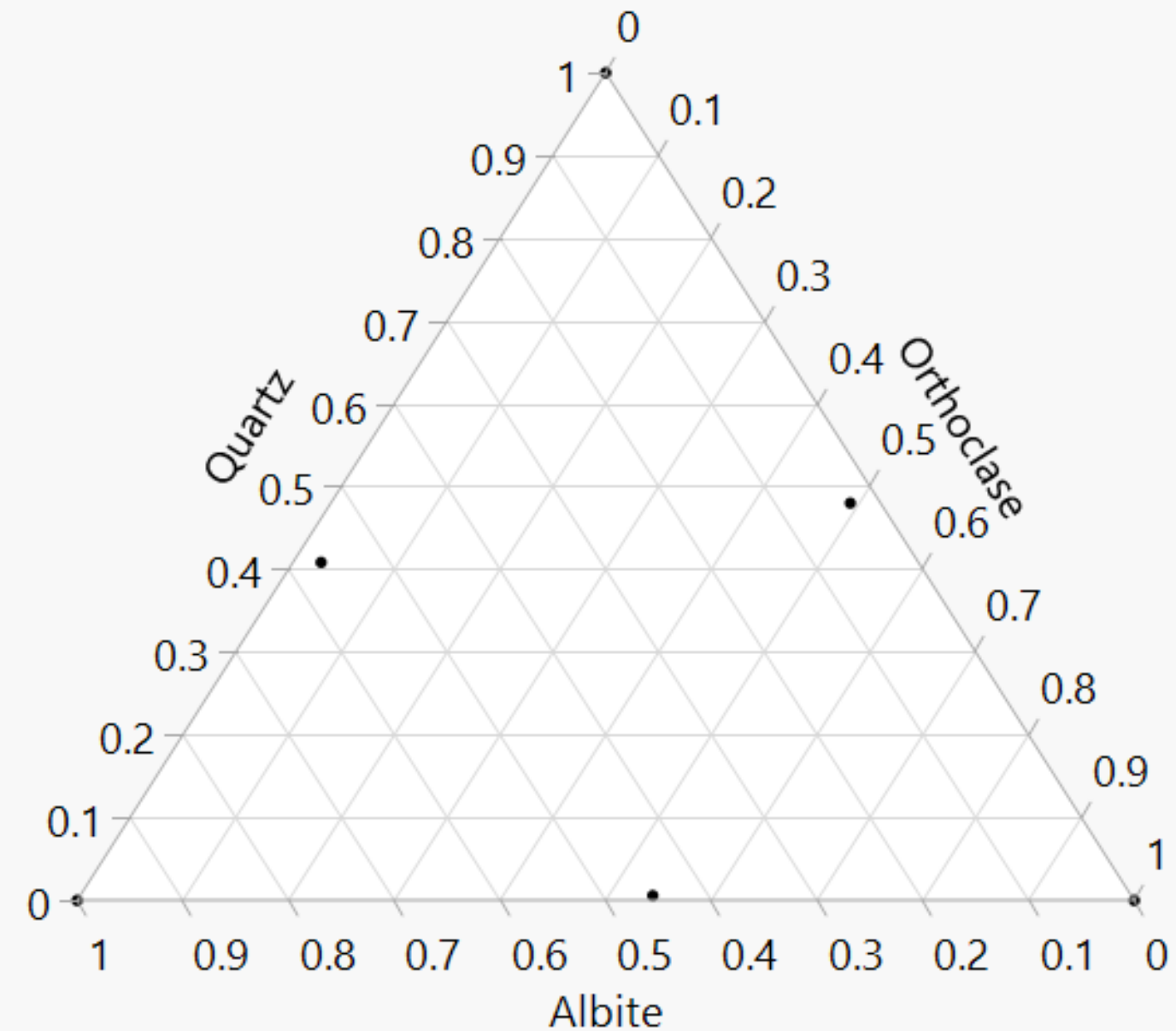
Takeaway #5

- Use Custom DOE to choose the most informative subset of trials (blends) from existing trials used as a candidate set.

Ternary Plot with 303 Blends of 3 Minerals



Ternary Plot with 6 Custom DOE Chosen Blends

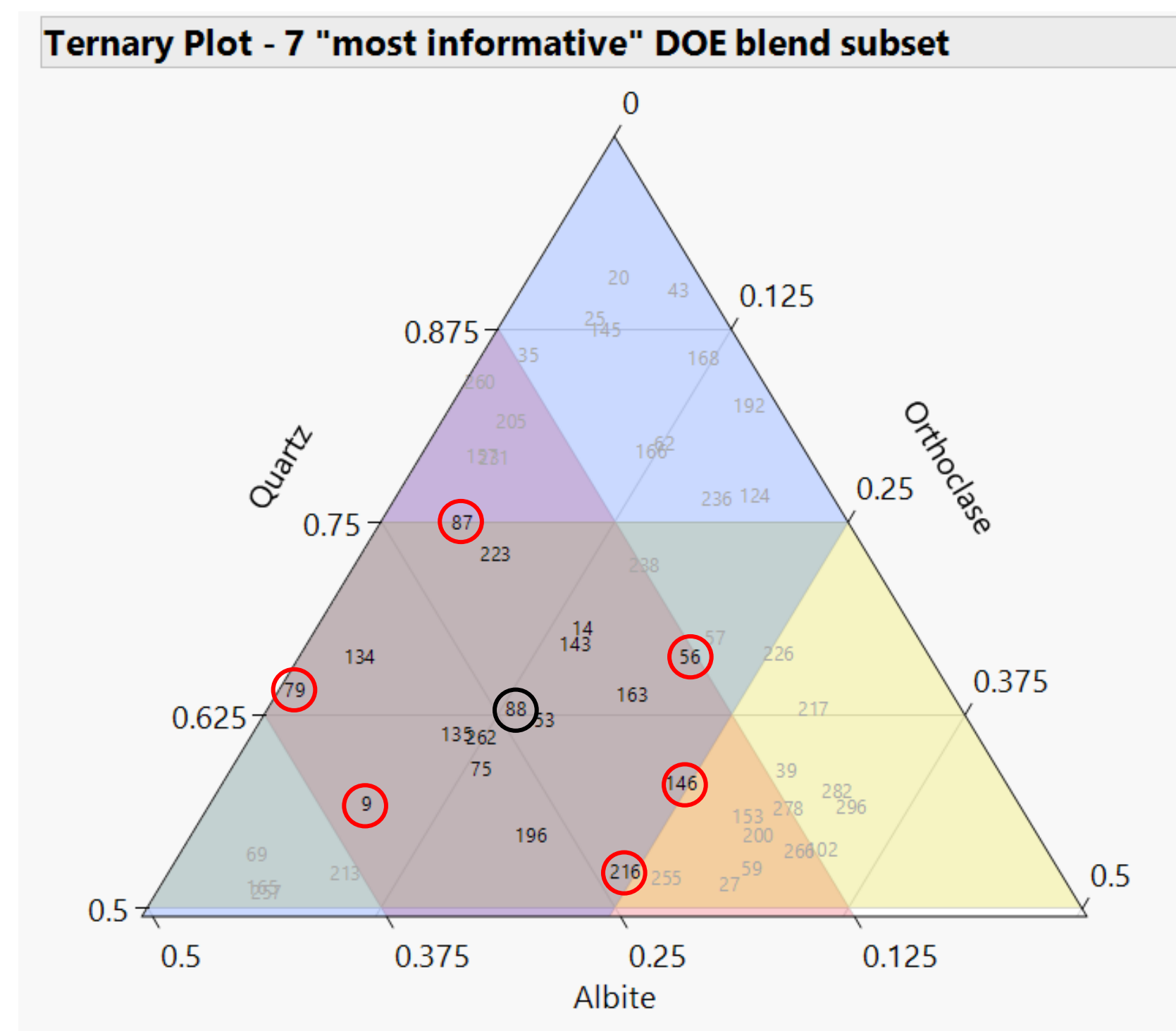
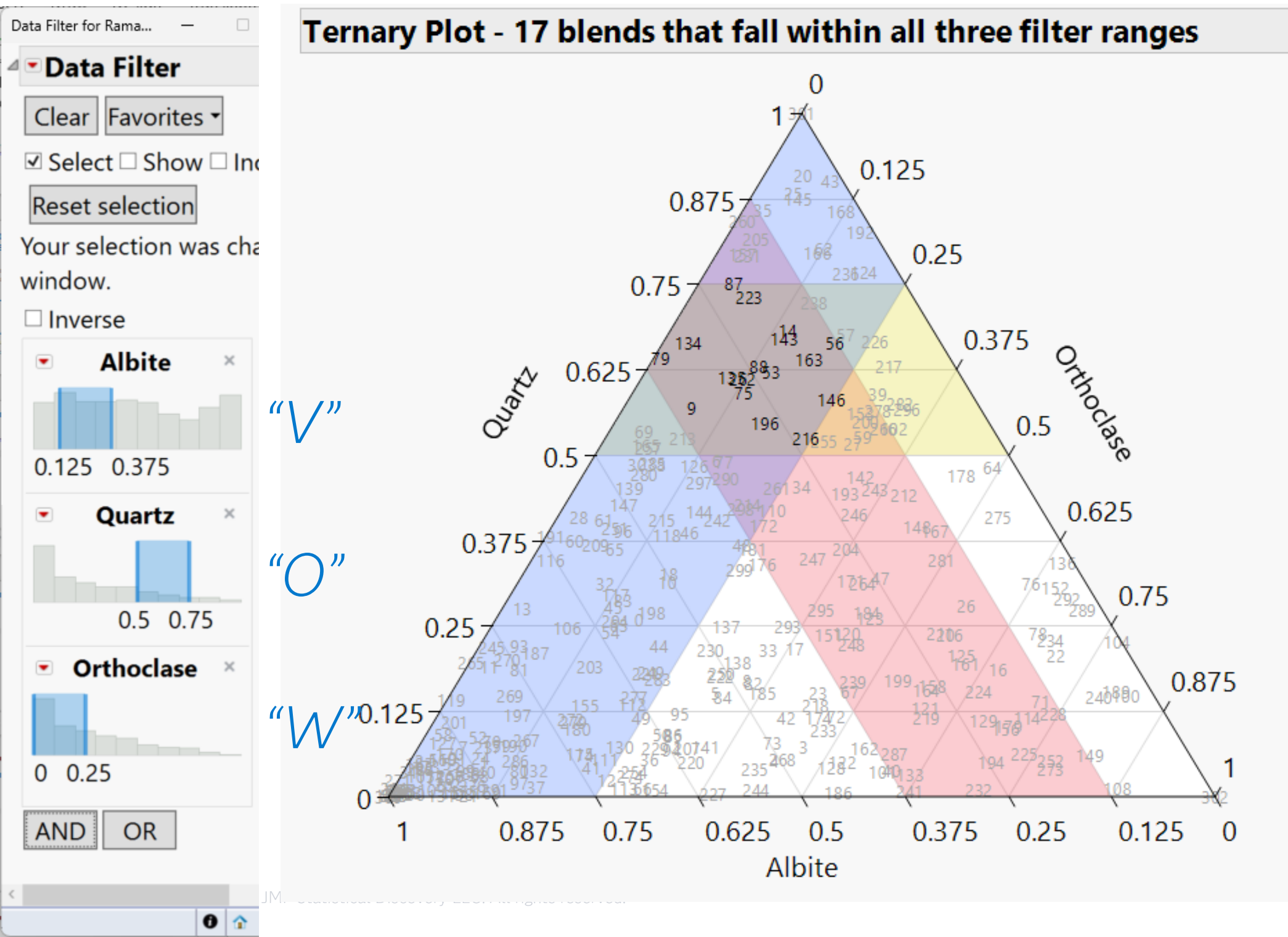


Takeaway #5 (continued)

- Use Custom DOE on a constrained region of design space

17 *filtered* blends used as candidate trials

7 circled trials are DOE subset



Case 1: Reanalysis of NMR Spectral Data for 3-Alcohol Mixture DOE using Functional Data Analysis



Available online at www.sciencedirect.com



Journal of Magnetic Resonance 190 (2008) 26–32



www.elsevier.com/locate/jmr

Quantitative analysis of NMR spectra with chemometrics

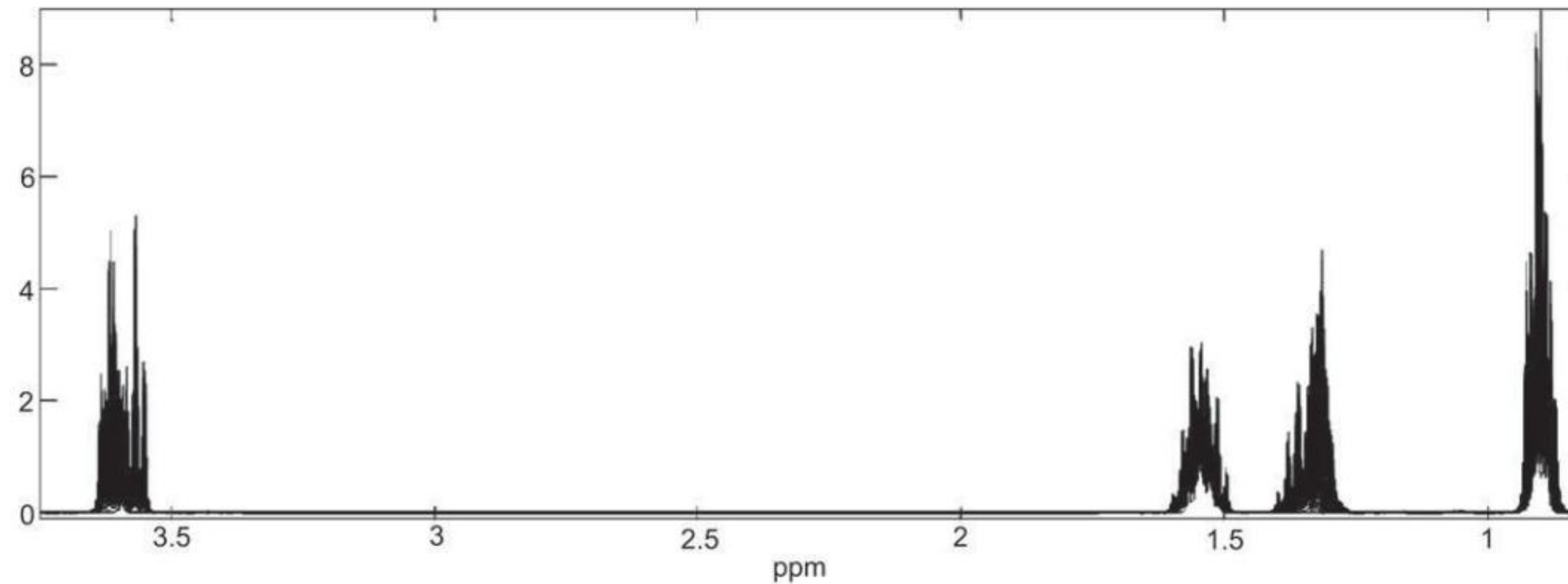
H. Winning *, F.H. Larsen, R. Bro, S.B. Engelsen

*Quality and Technology, Department of Food Science, Faculty of Life Sciences, University of Copenhagen, Rolighedsvej 30,
DK-1958 Frederiksberg C, Denmark*

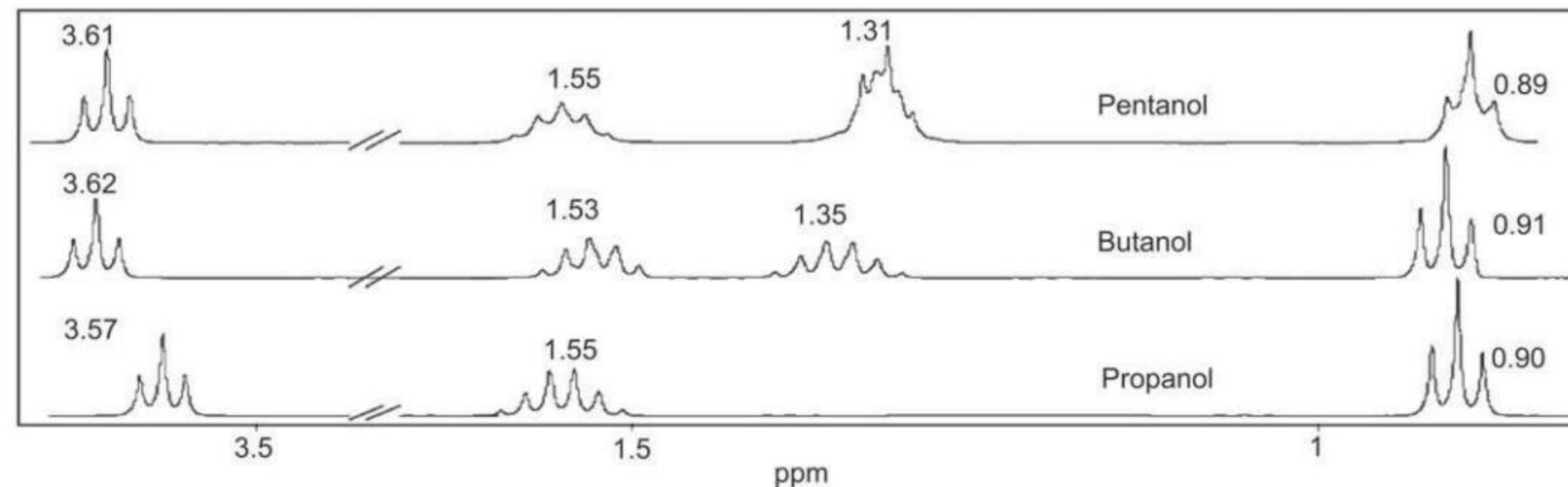
Received 11 April 2007; revised 8 October 2007

Available online 14 October 2007

Quantitative analysis of NMR spectra with chemometrics



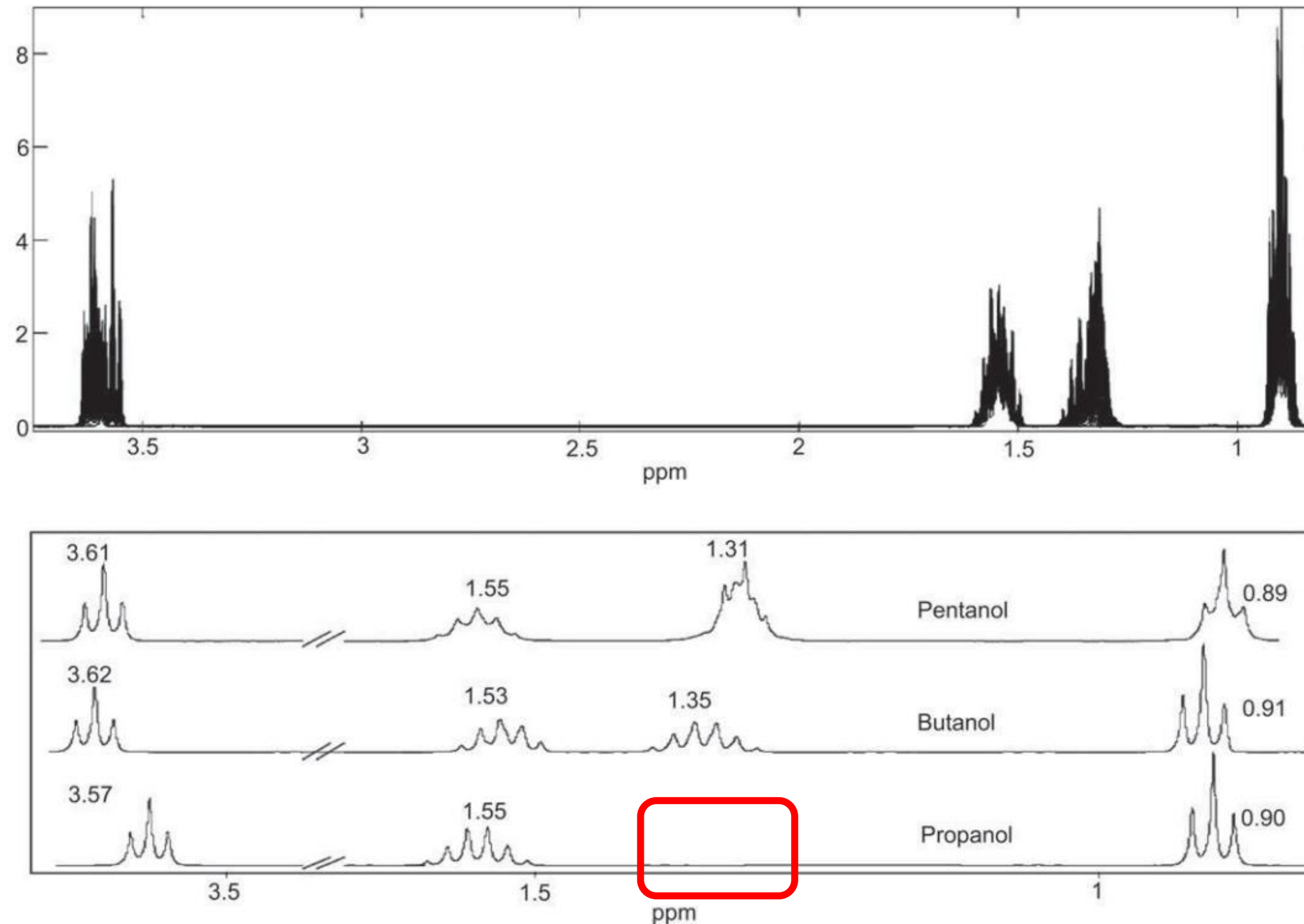
Overlay
of 231
alcohol-
blend
spectra



Spectra
for 3
pure
alcohols

Fig. 2. (Top) NMR spectra of the 231 alcohol mixtures from 3.85 to 0.65 ppm. The NMR spectra of mixtures show highly overlapping signals. (Bottom) The ^1H NMR spectra of the pure alcohol samples of propanol, butanol and pentanol.

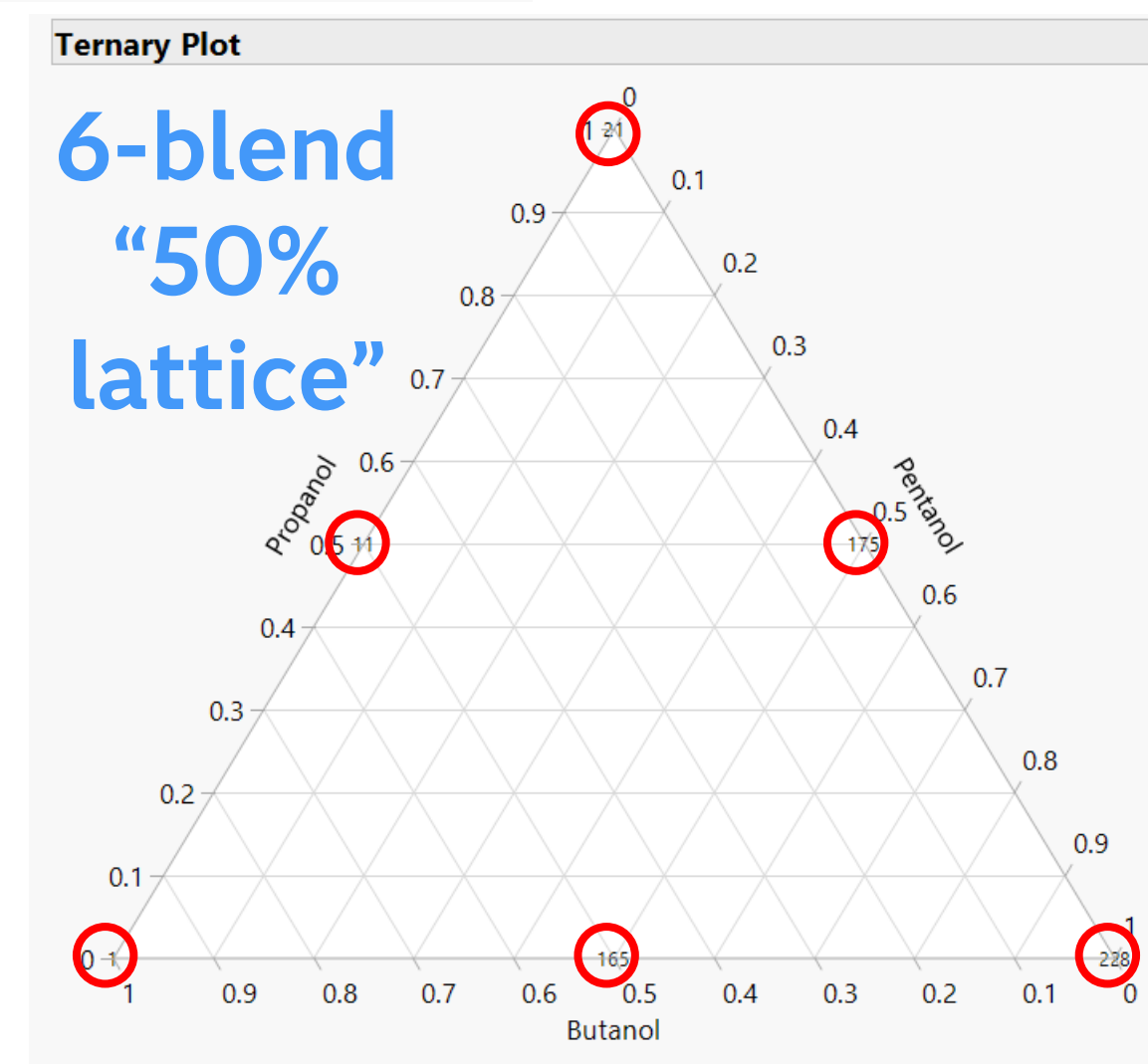
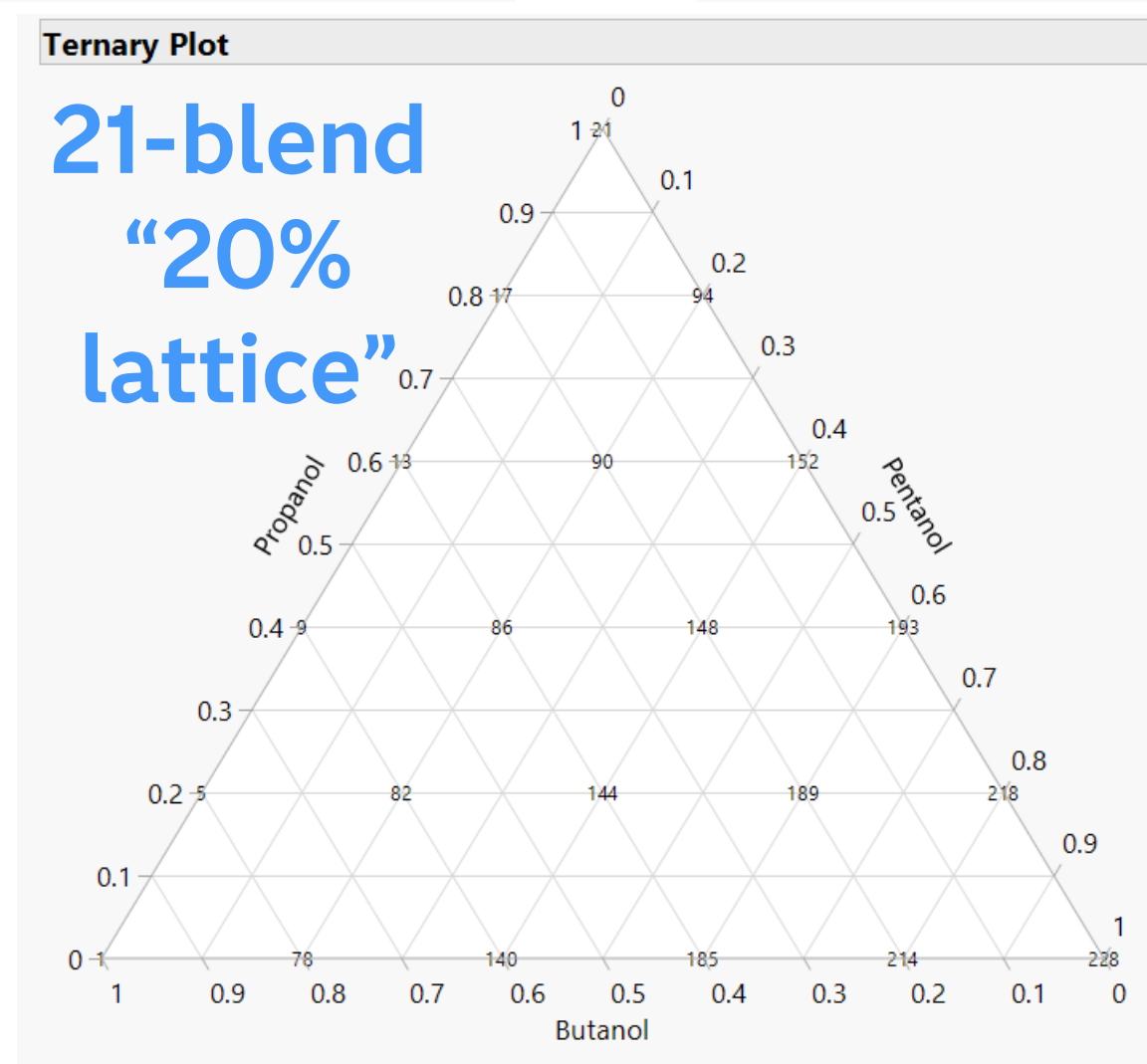
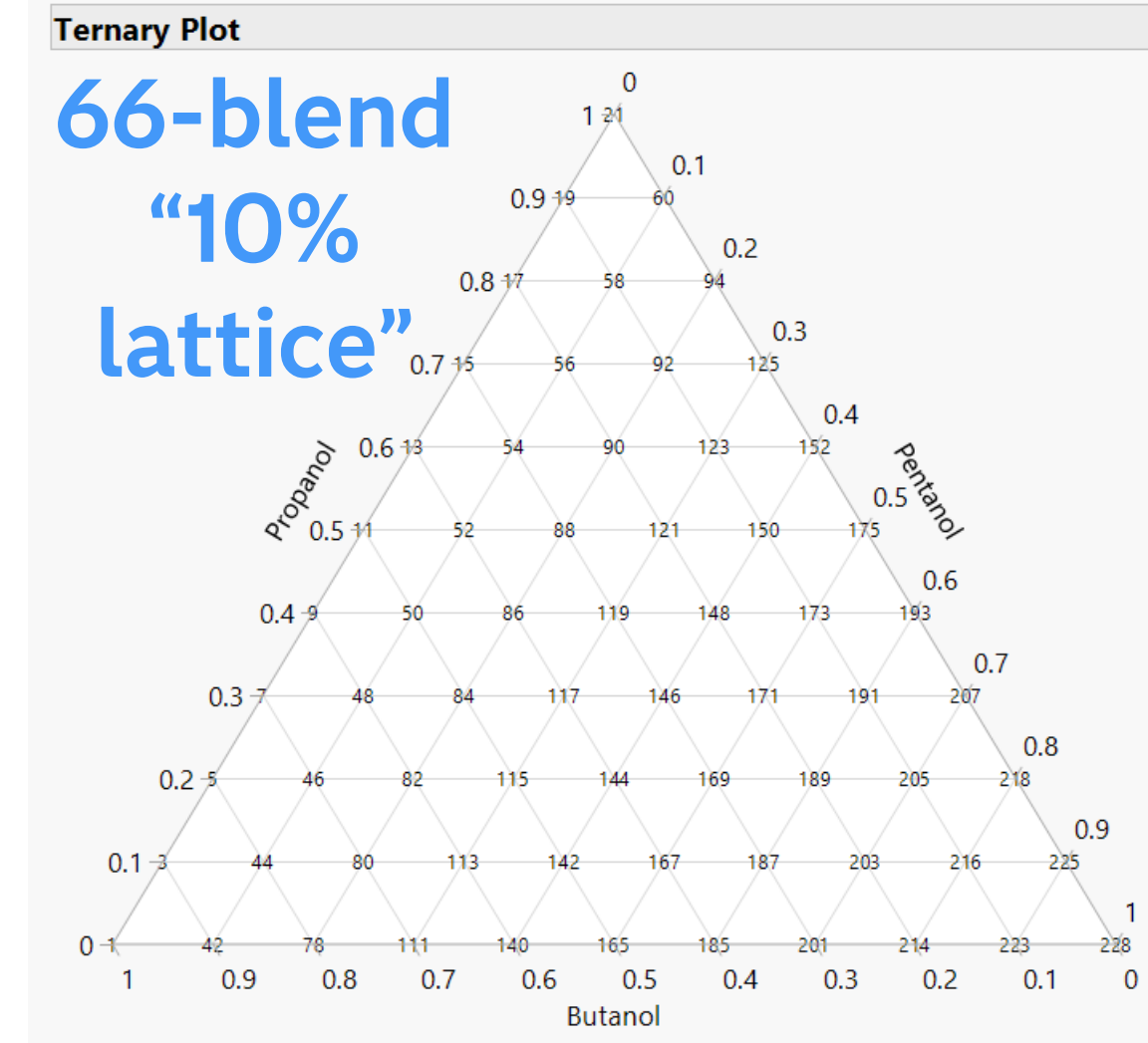
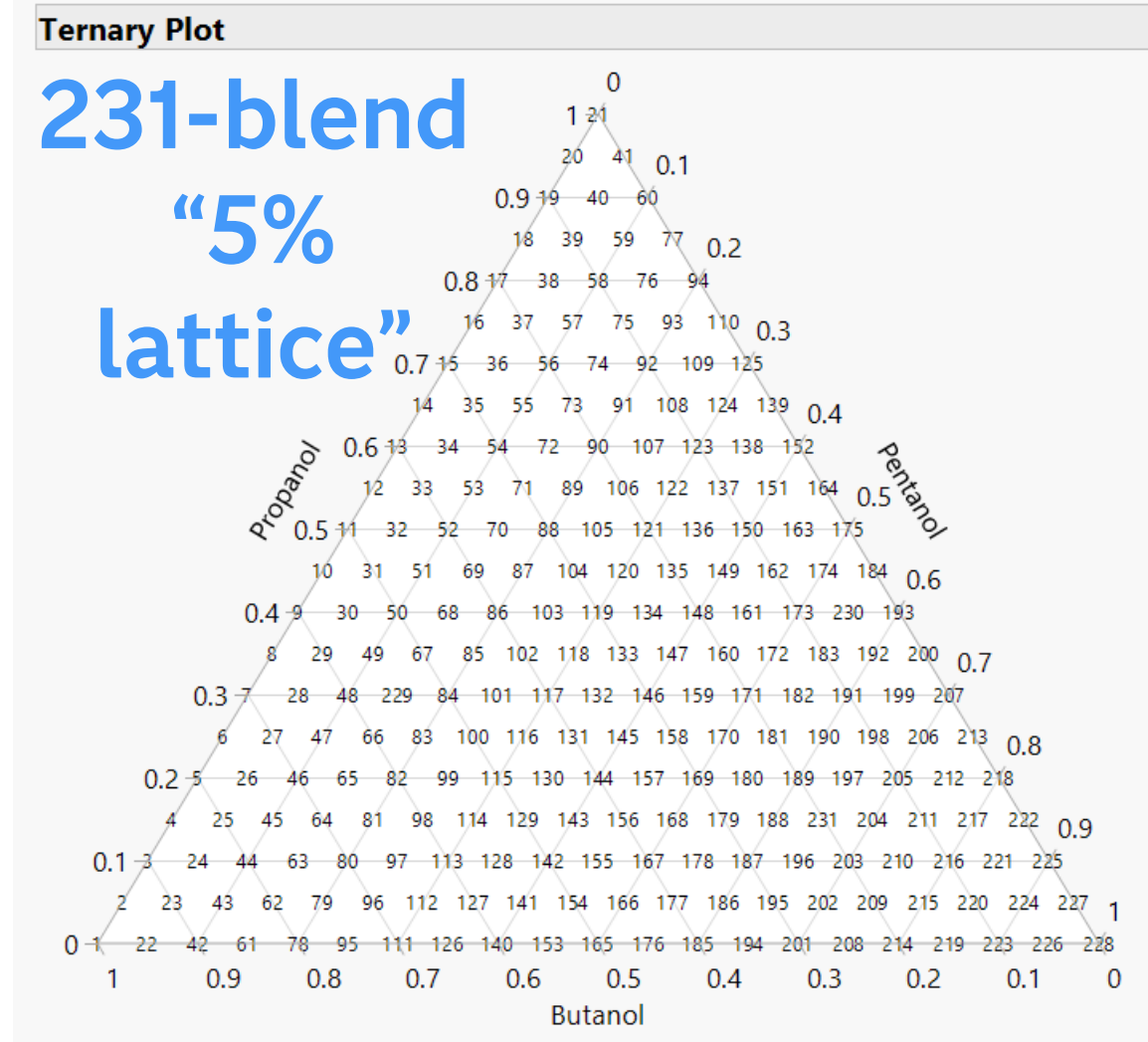
Quantitative analysis of NMR spectra with chemometrics



**Note the
absence of
spectral
group in
Propanol**

Fig. 2. (Top) NMR spectra of the 231 alcohol mixtures from 3.85 to 0.65 ppm. The NMR spectra of mixtures show highly overlapping signals. (Bottom) The ^1H NMR spectra of the pure alcohol samples of propanol, butanol and pentanol.

Various size “lattice” subset mixture designs



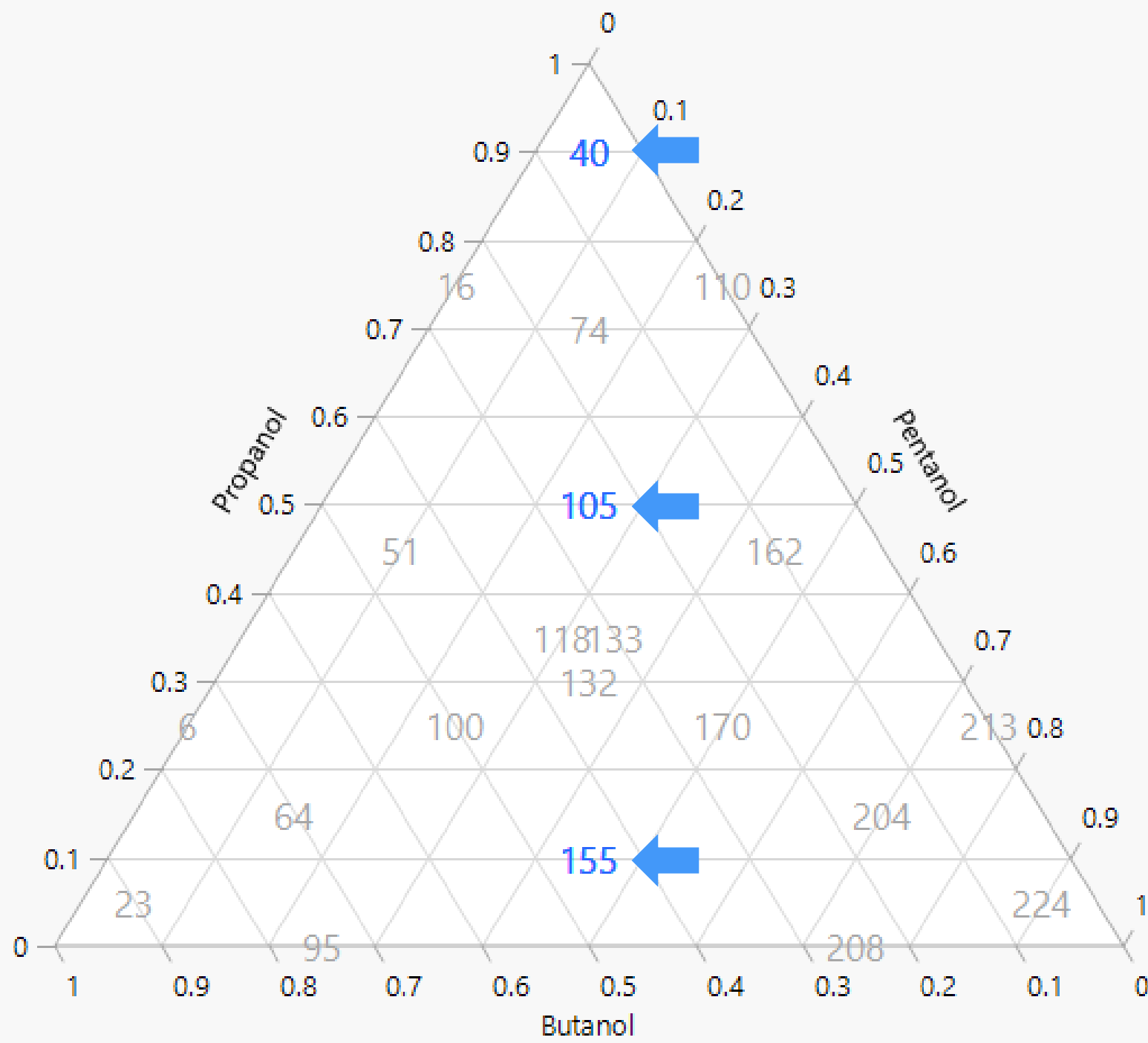
Given proportions of each component in a formulation
- *that was not used in the functional data analysis* -

How well can the spectral shape be predicted?

Counts & Counts Functional Prediction Formula vs. X



Ternary Plot



NMR ID

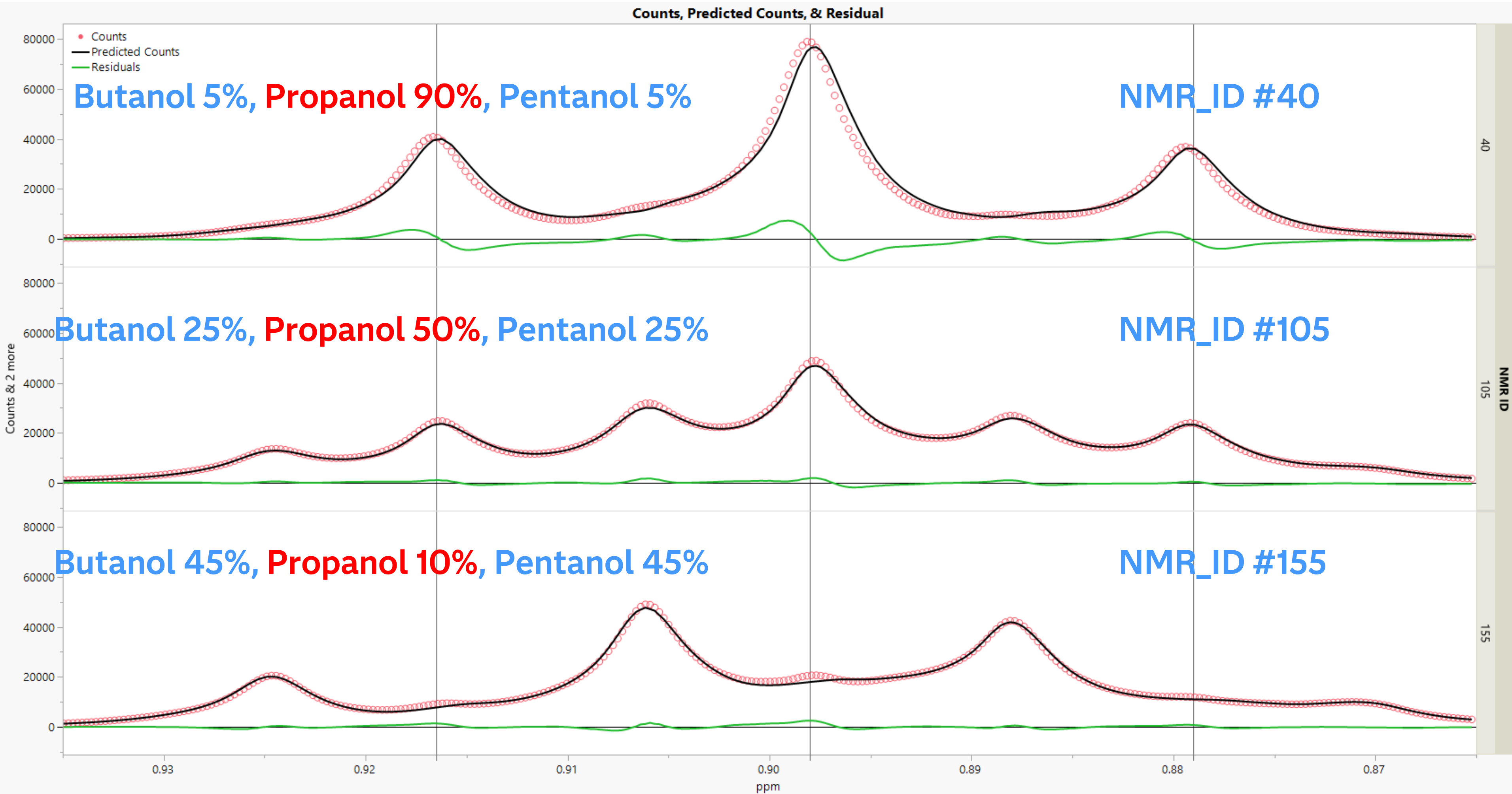
40

105

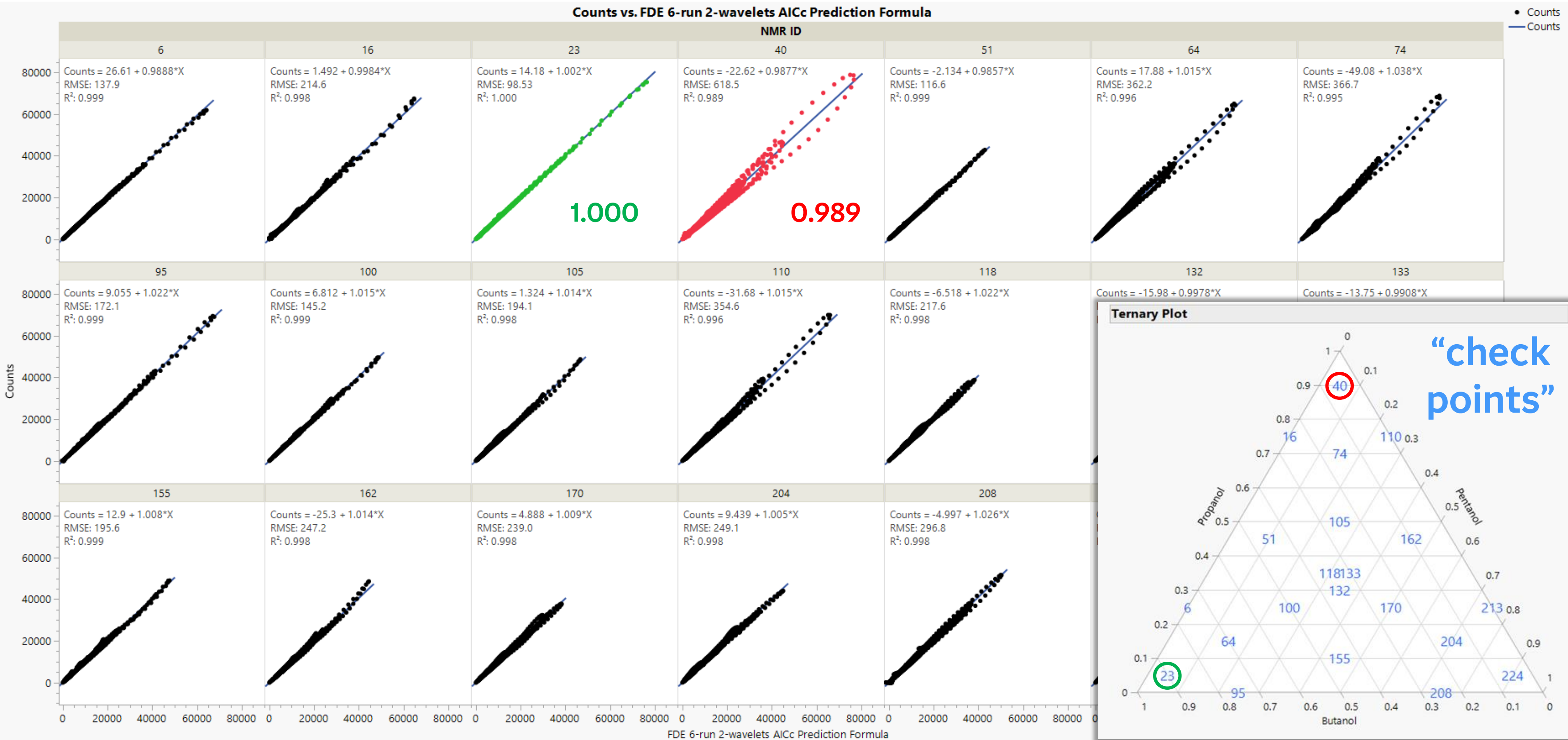
155

Where(NMR ID = 40, 105, 155)

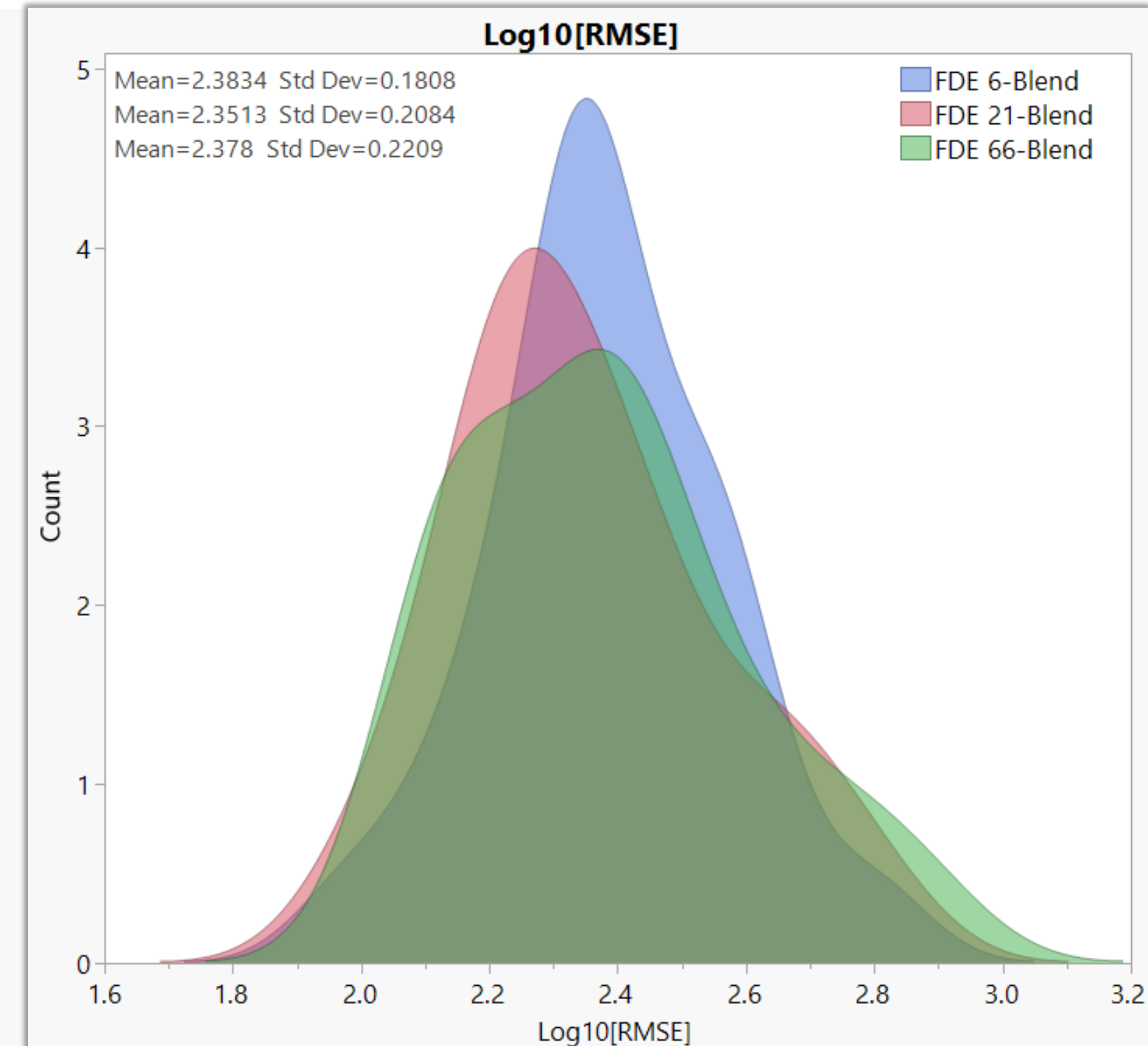
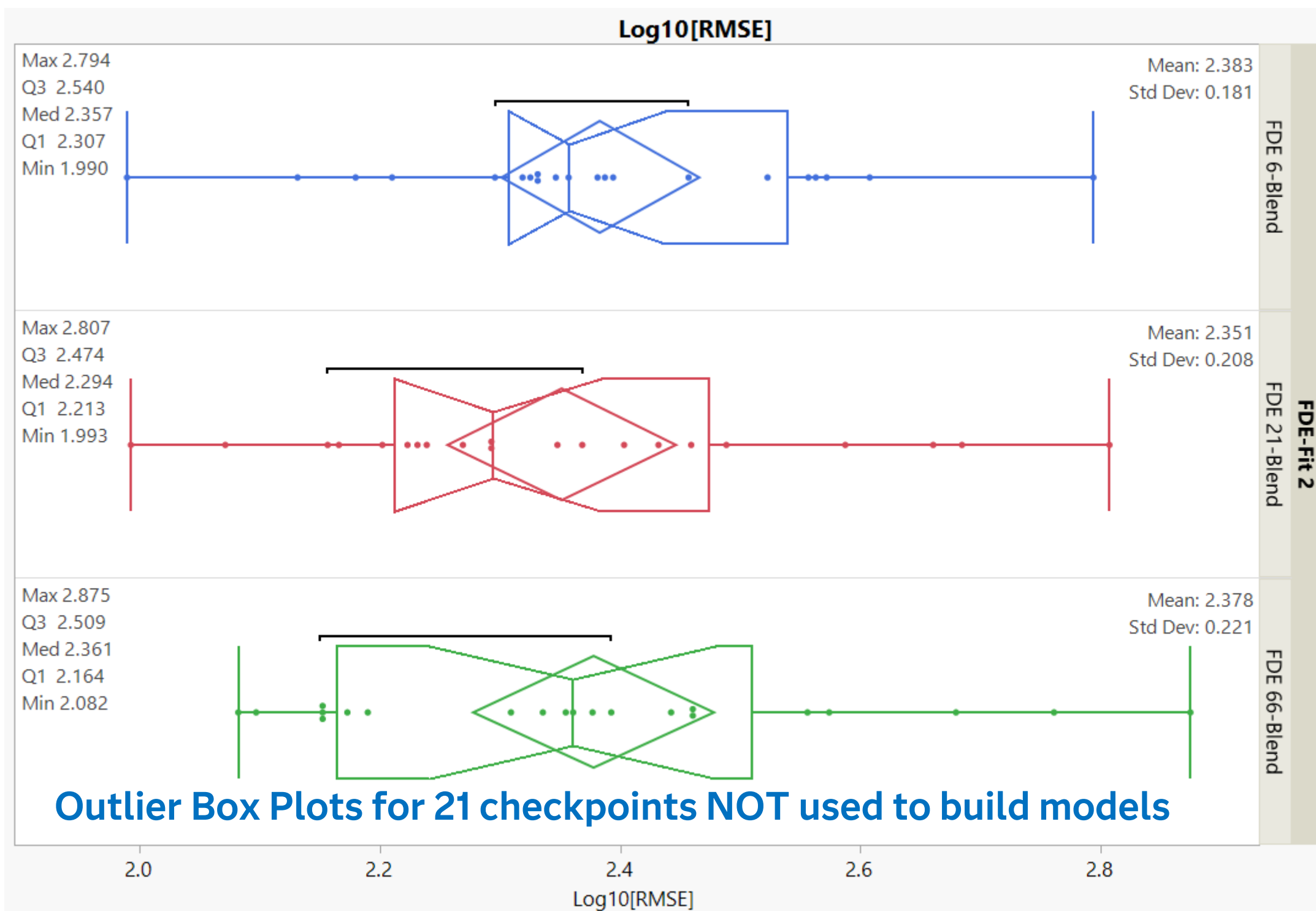
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Actual vs. Predicted Plots for 21 Test Blends



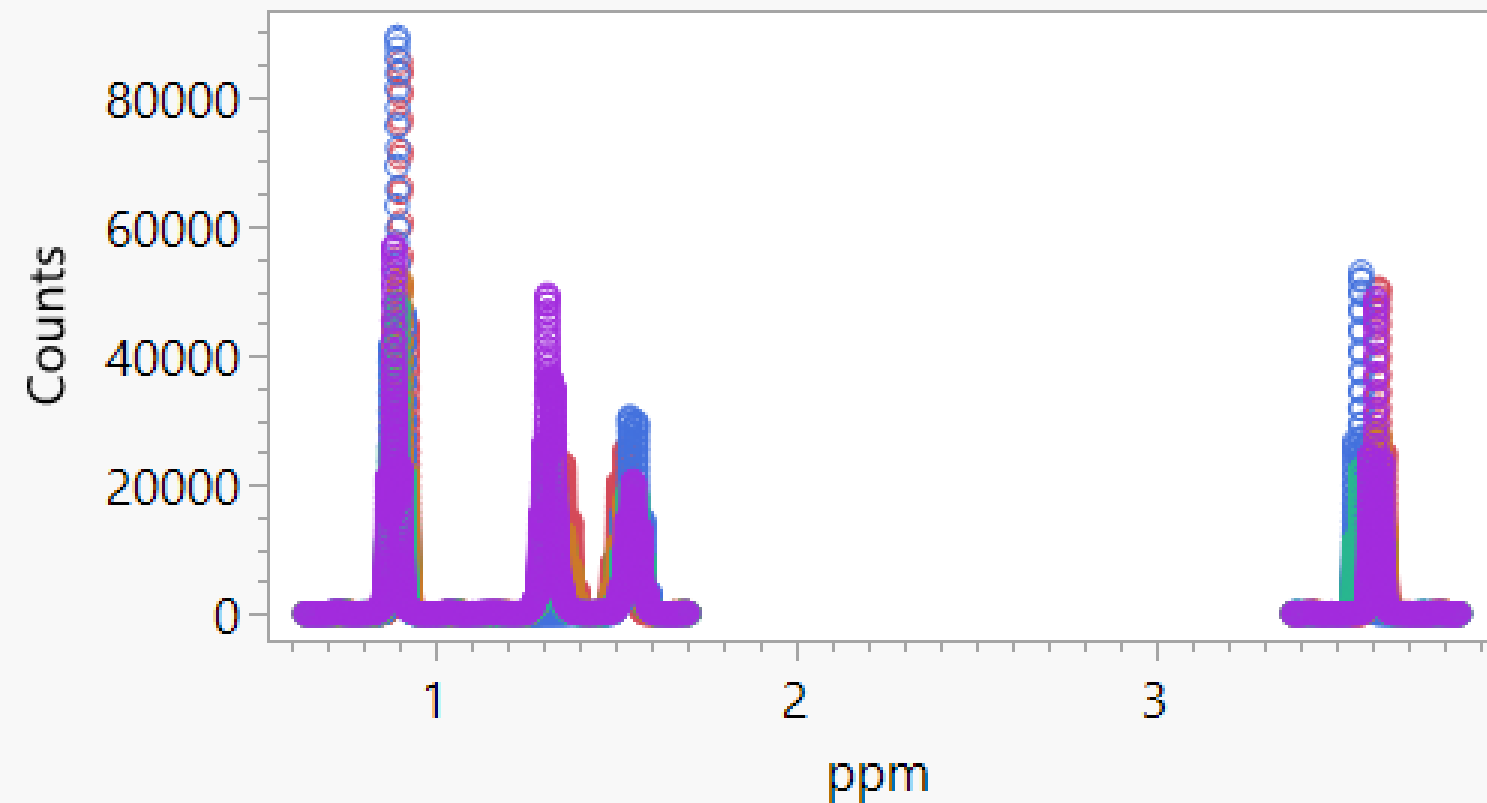
No Statistical or Practical Improvement Observed when Increasing from 6 to 21 or 66 Blends to Train FDA Model



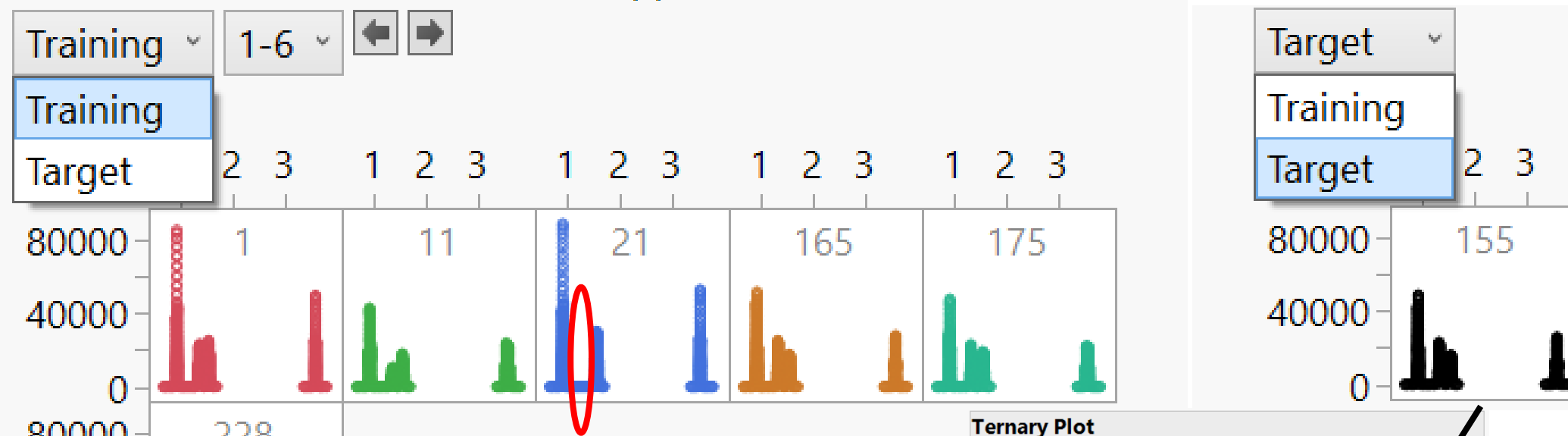
Given the spectral shape of a formulation
– *that was not used in the functional data analysis* –

**How well can the proportion of each component
be predicted? Can we *Reverse Engineer* it?**

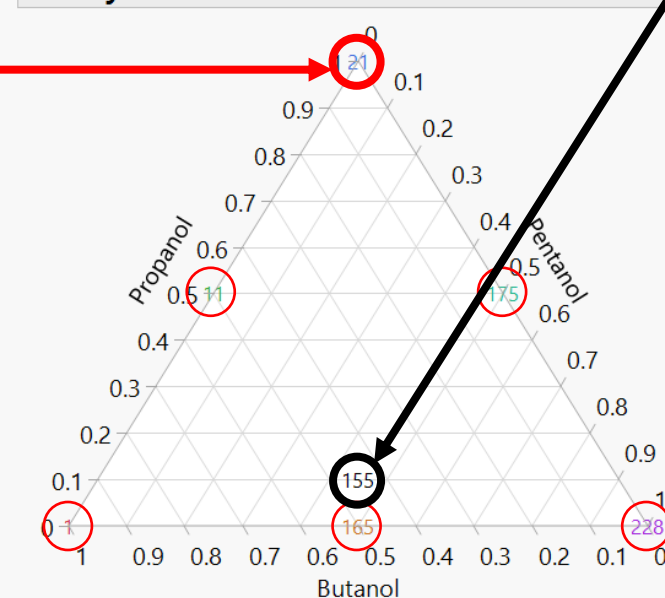
Load Targets Plot



Functional Data Explorer:
After loading 6 *Training* spectra
and 1 *Target* spectra to predict
composition of NMR ID #155



Pure
Propanol
Missing
Spectral
Group



Commands

Cleanup Transform Align Spectral Target Functions

Load



Select target functions

- 1
- 11
- 21
- 155
- 165
- 175
- 228

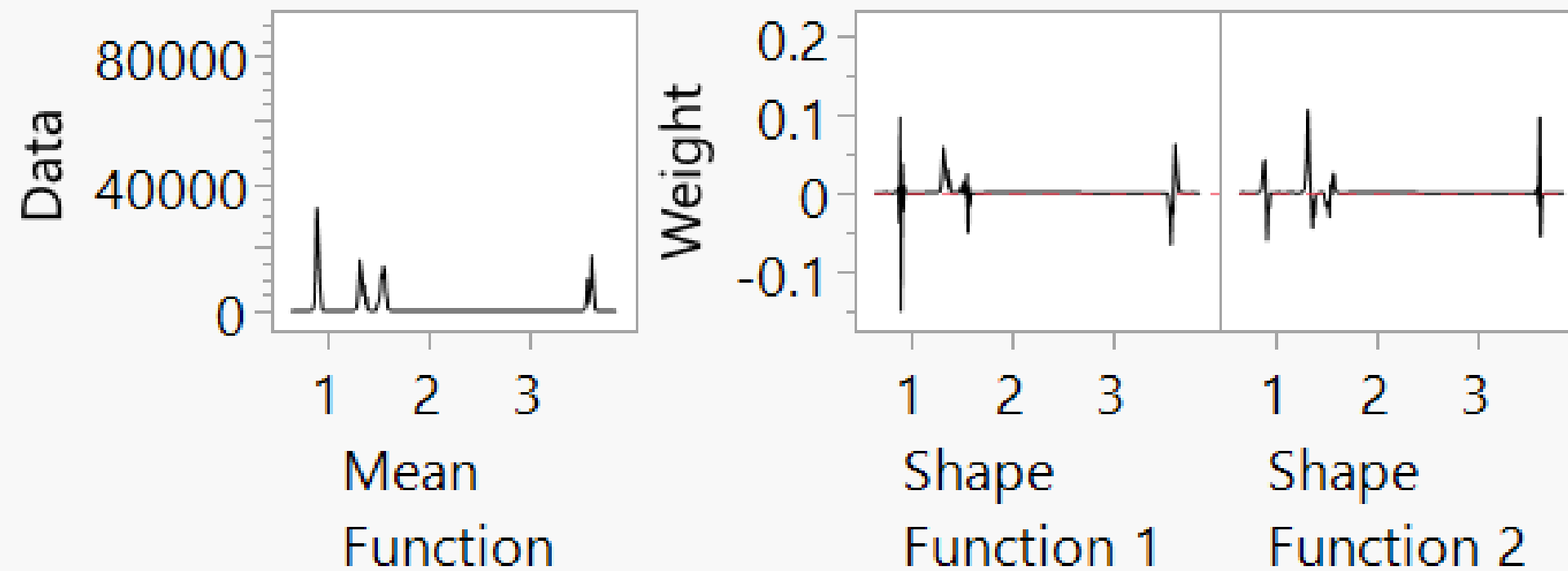
OK Cancel

FUNCTIONAL DATA ANALYSIS

Component Strength

FPC	Eigenvalue	20406080	Percent	Cumulative
1	2.978e+10		56.8%	56.8%
2	2.213e+10		42.2%	99.1%

Shape Functions



longitudinal variation

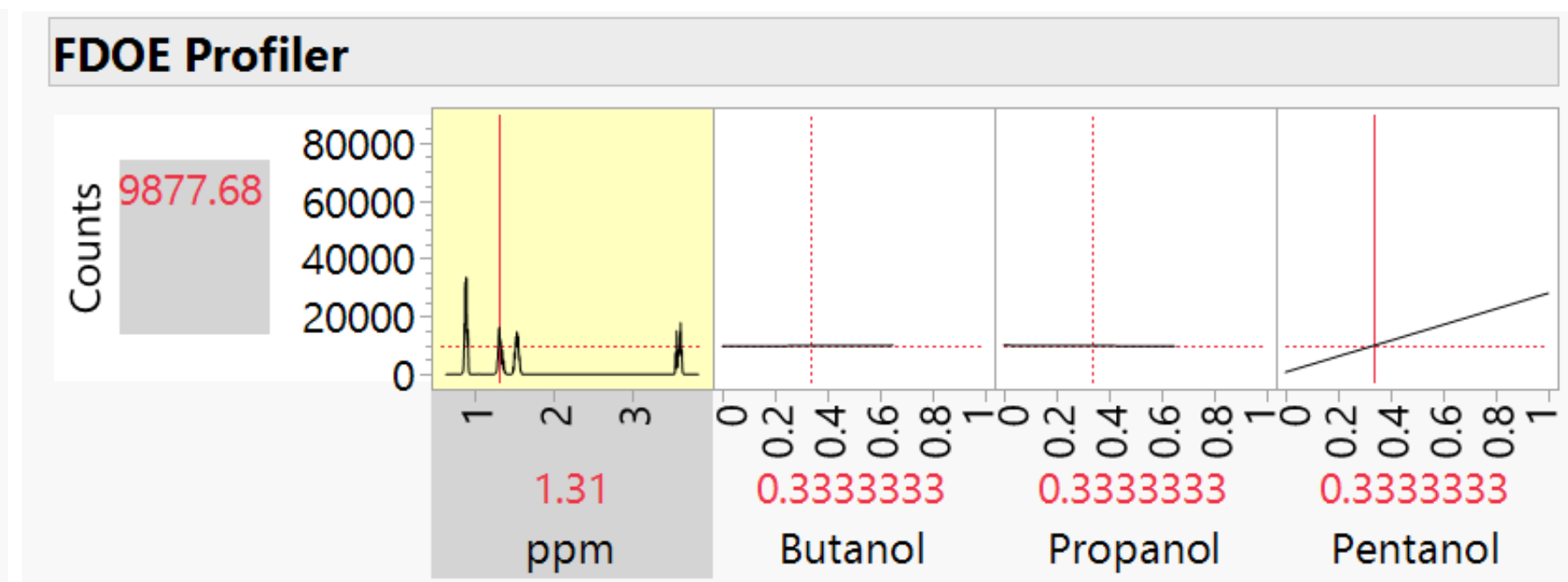
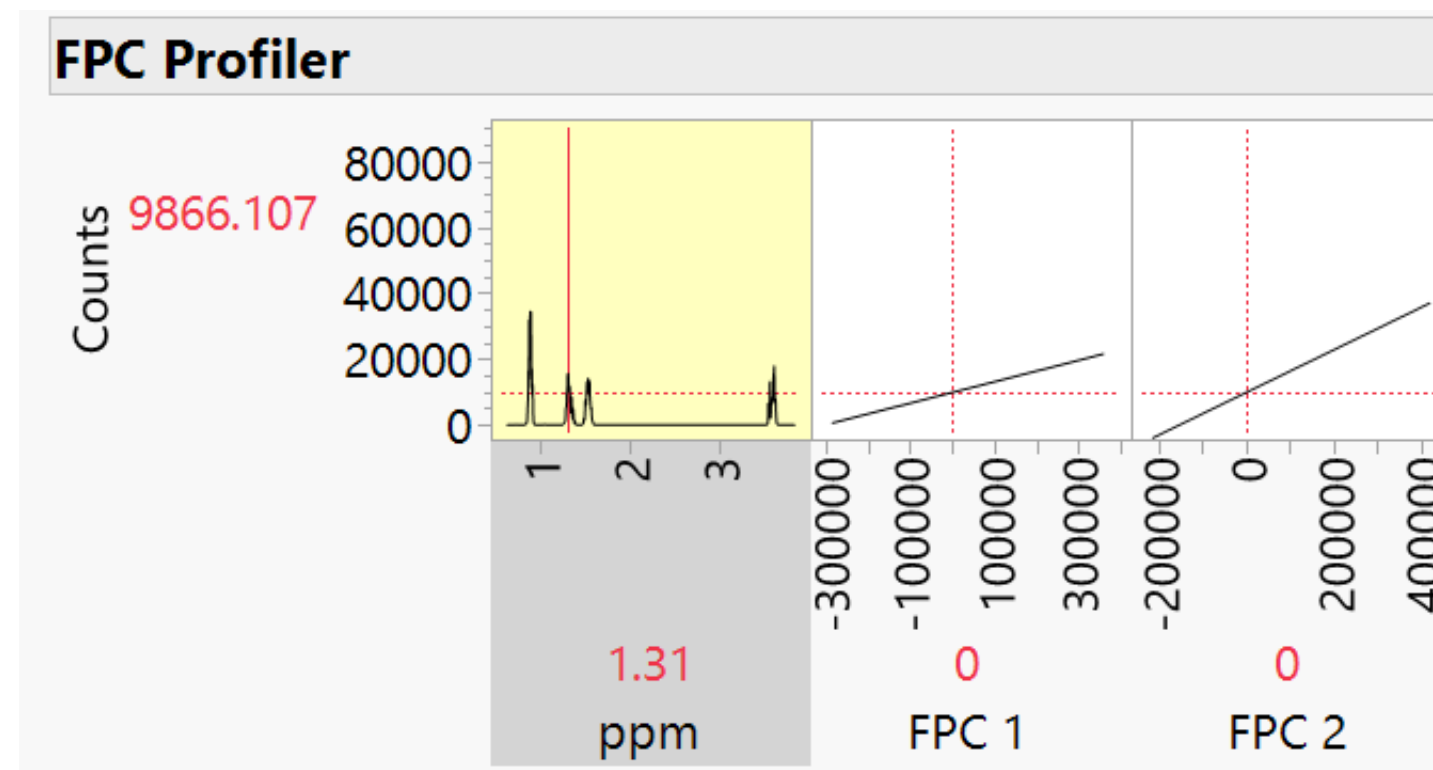
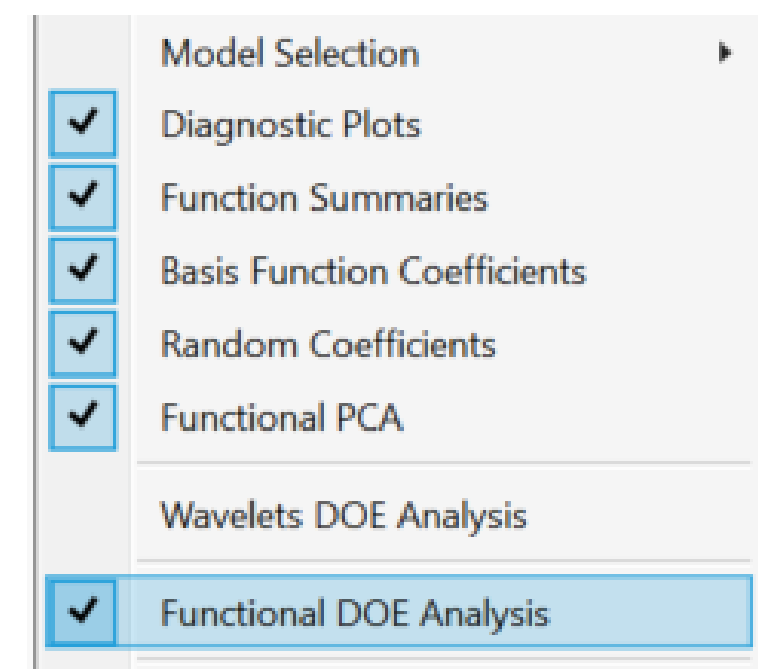
Function Summaries

NMR ID	FPC 1	FPC 2
1	145028.69	-213039.7
11	-73207.5	-101250.7
21	-283858.6	-5560.768
165	140129.43	3883.9851
175	-63377.54	107639.32
228	135285.5	208327.83

function-to-function variation

FUNCTIONAL DOE

- One Problem!! We don't blend FPCs. We blend alcohols!
- That is why Functional DOE Analysis option is so powerful
- Automatically models the FPC scores as functions of the DOE factors

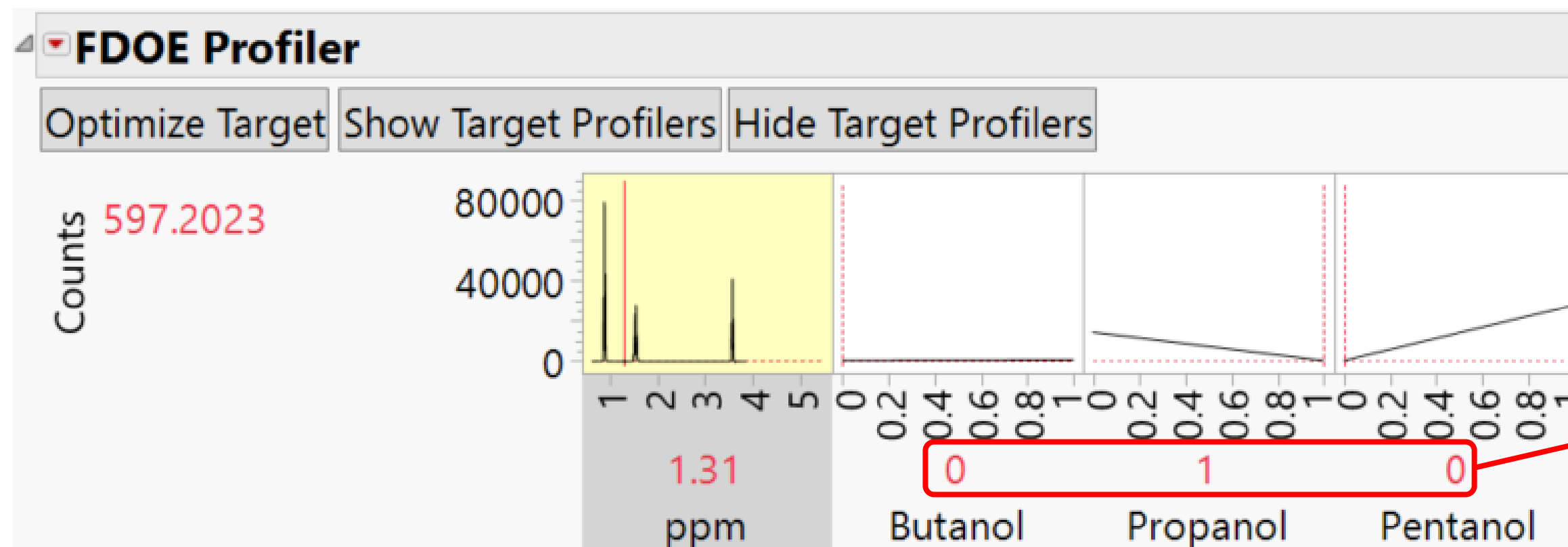


$$FPC\ 1 = f(\text{Butanol}, \text{Propanol}, \text{Pentanol})$$

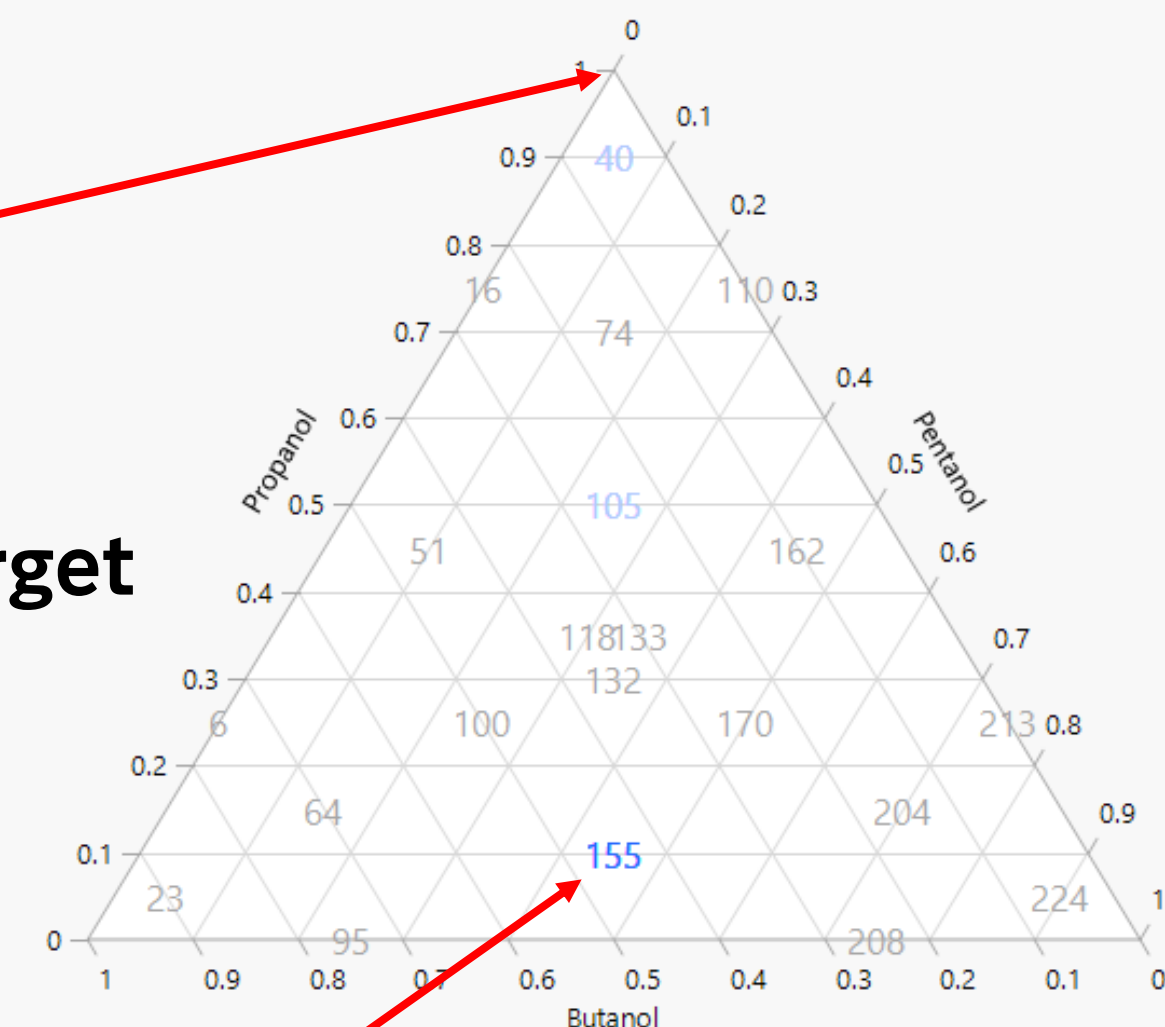
$$FPC\ 2 = f(\text{Butanol}, \text{Propanol}, \text{Pentanol})$$

- FDOE Profiler model can readily be used - *in a practical manner* - to *predict* component/factor impact on spectra

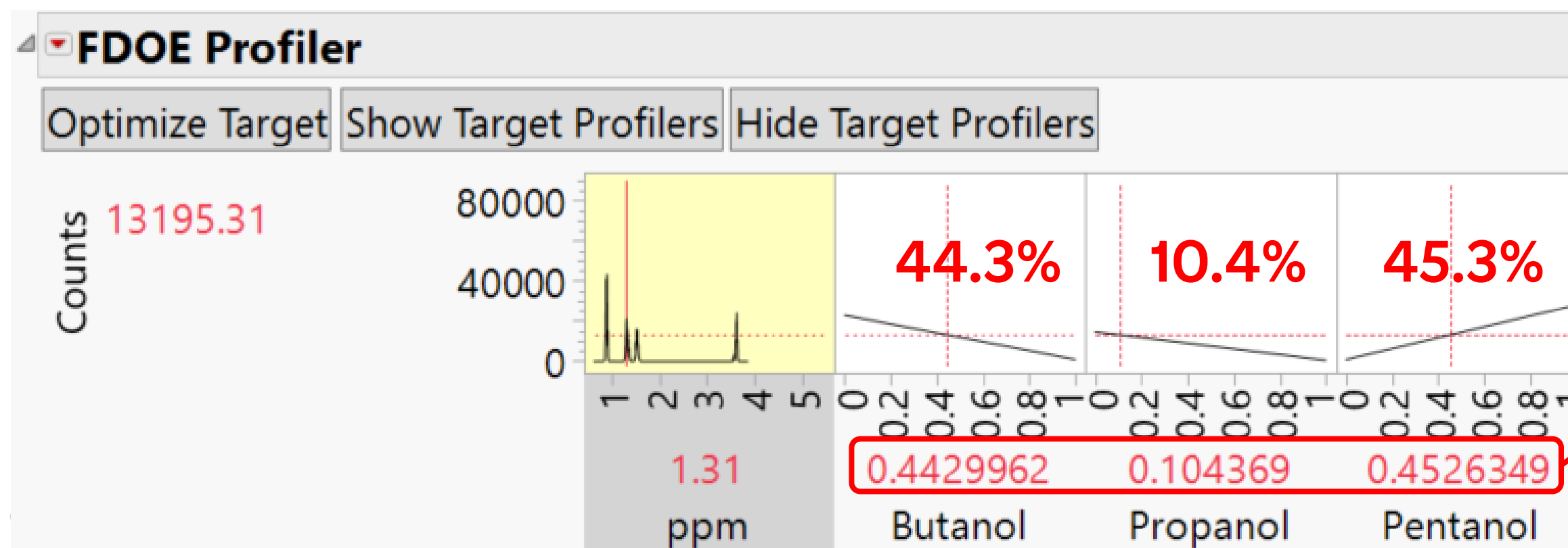
Settings for pure Propanol (0% 100% 0%) – before Optimize Target



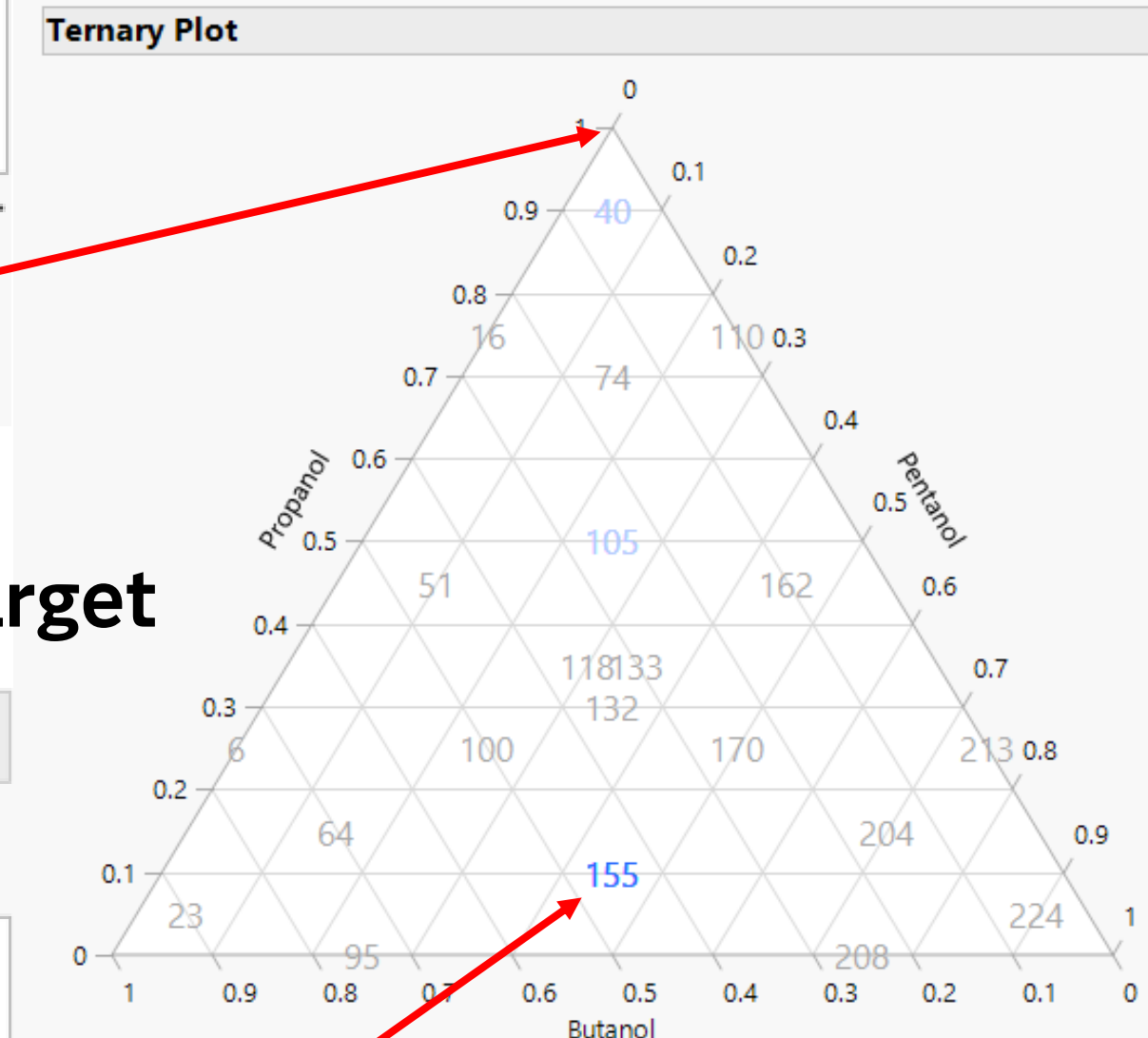
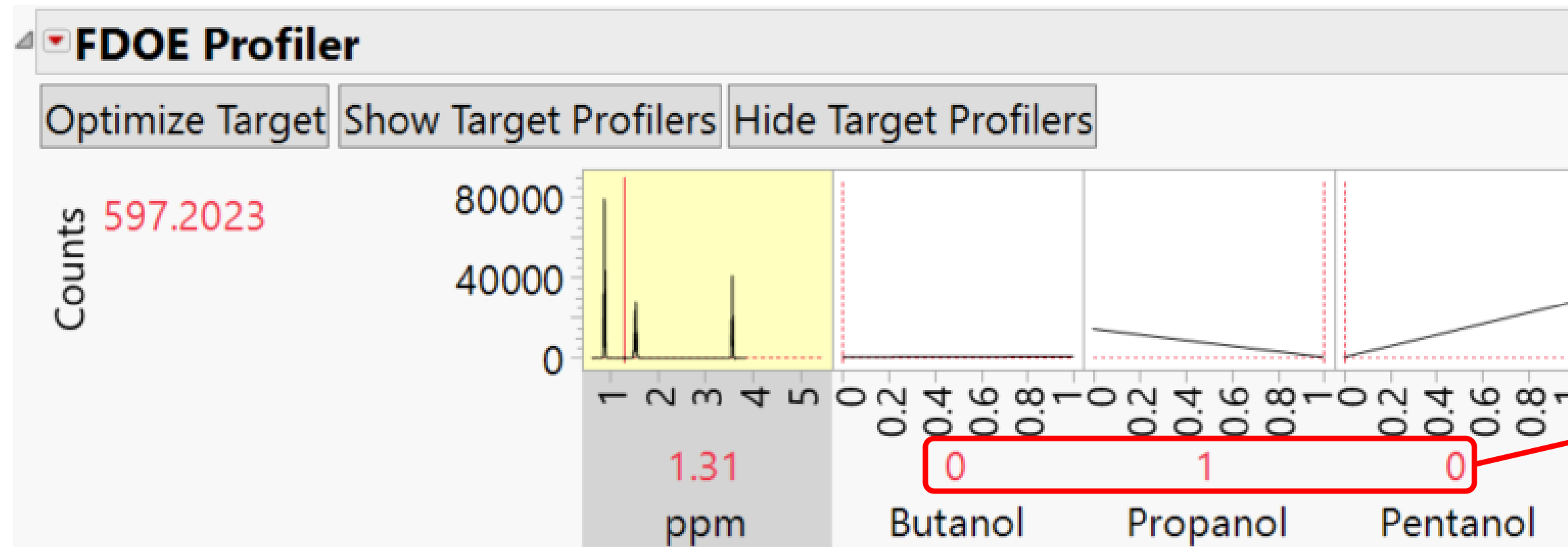
Ternary Plot



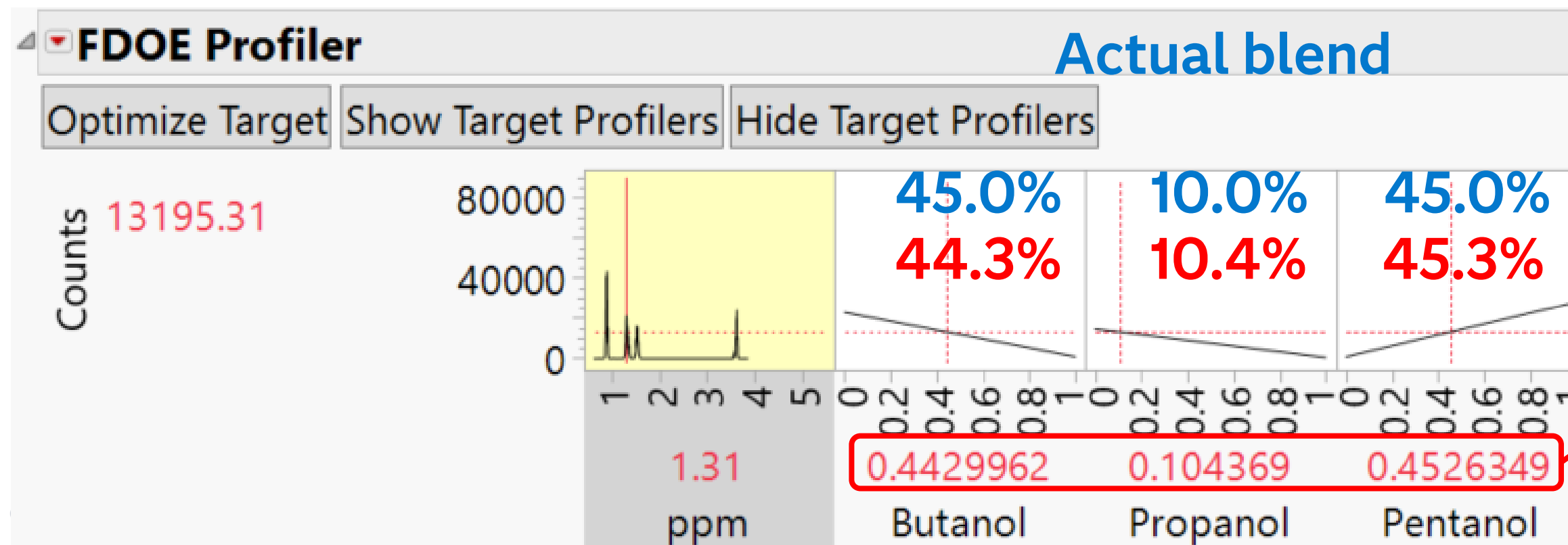
Predicted settings for target NMR #155 – after Optimize Target



Settings for pure Propanol (0% 100% 0%) – before Optimize Target



Predicted settings for target NMR #155 – after Optimize Target



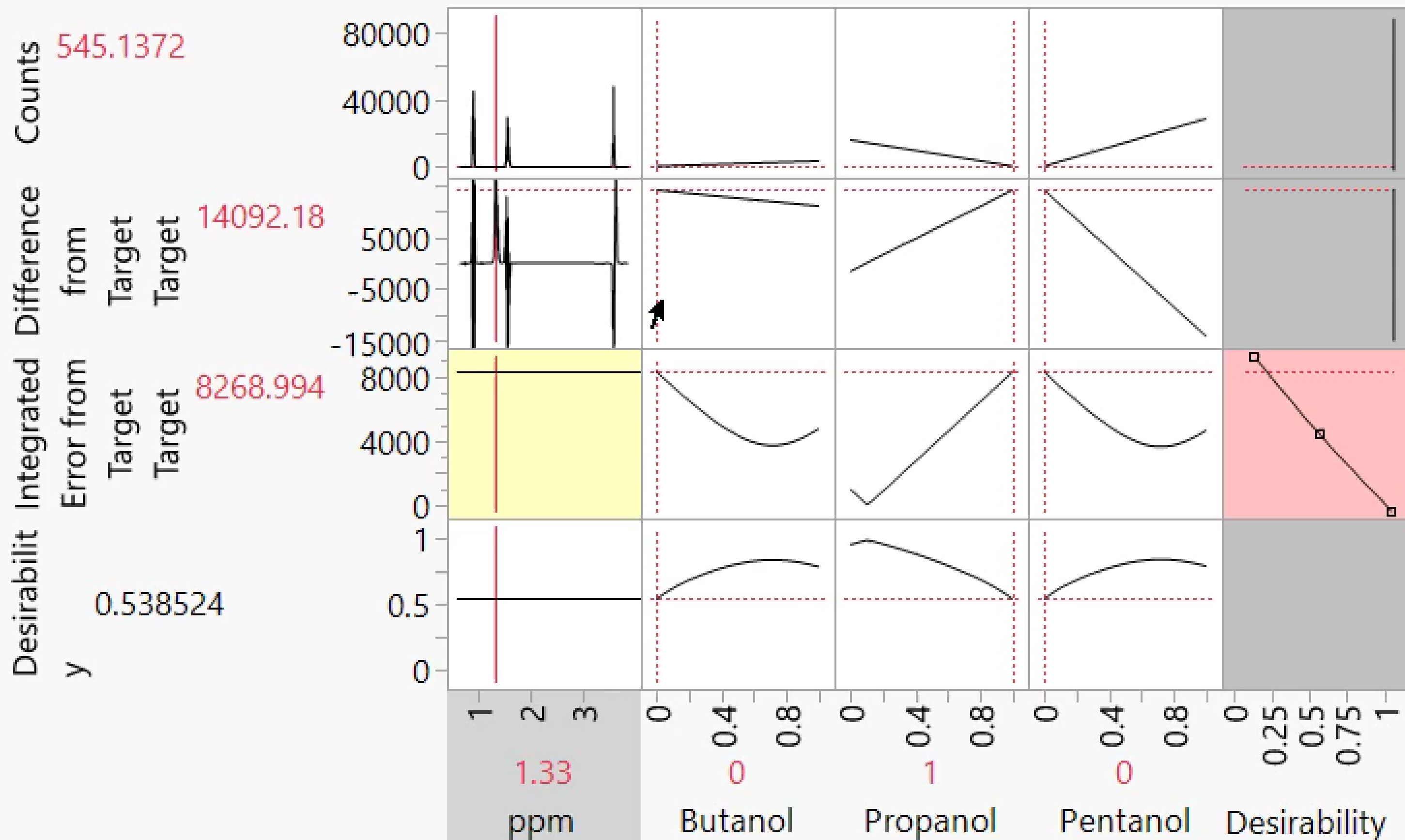
FDOE Profiler

NMR_ID #155 is the Target Curve (45% 10% 45%)

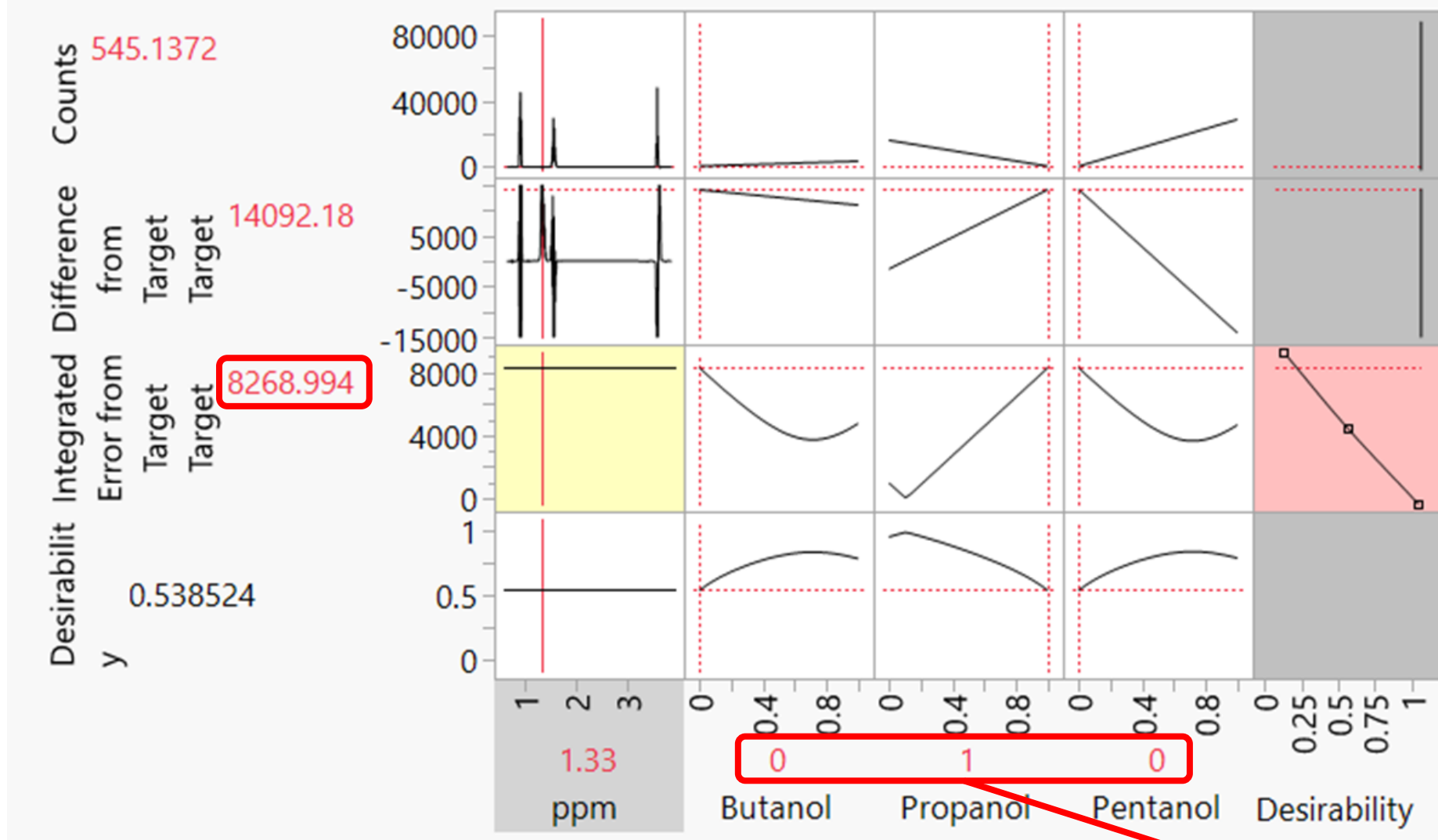
Optimize Target

Show Target Profilers

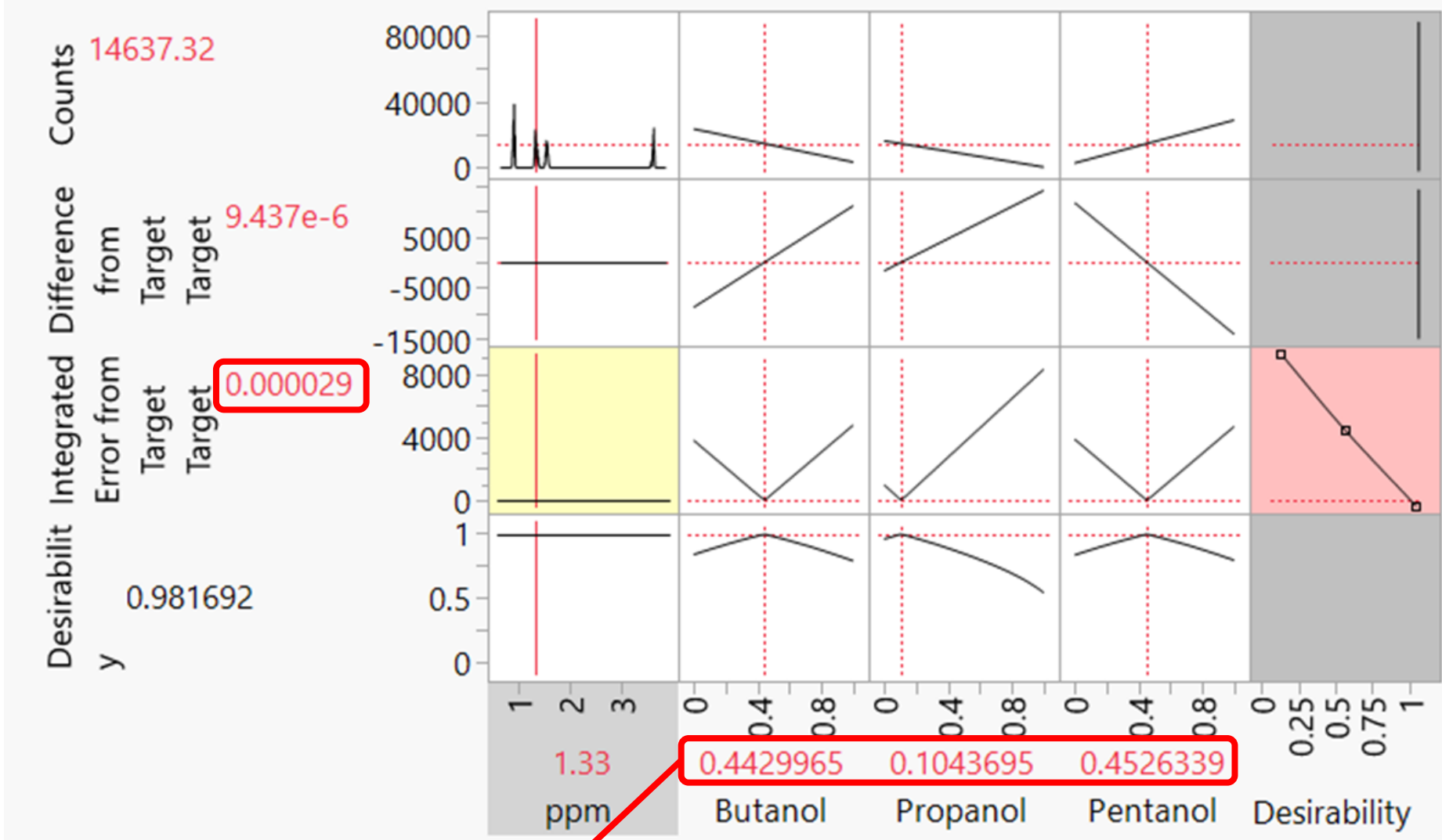
Hide Target Profilers



FDOE Profiler Before Optimization Pure Propanol

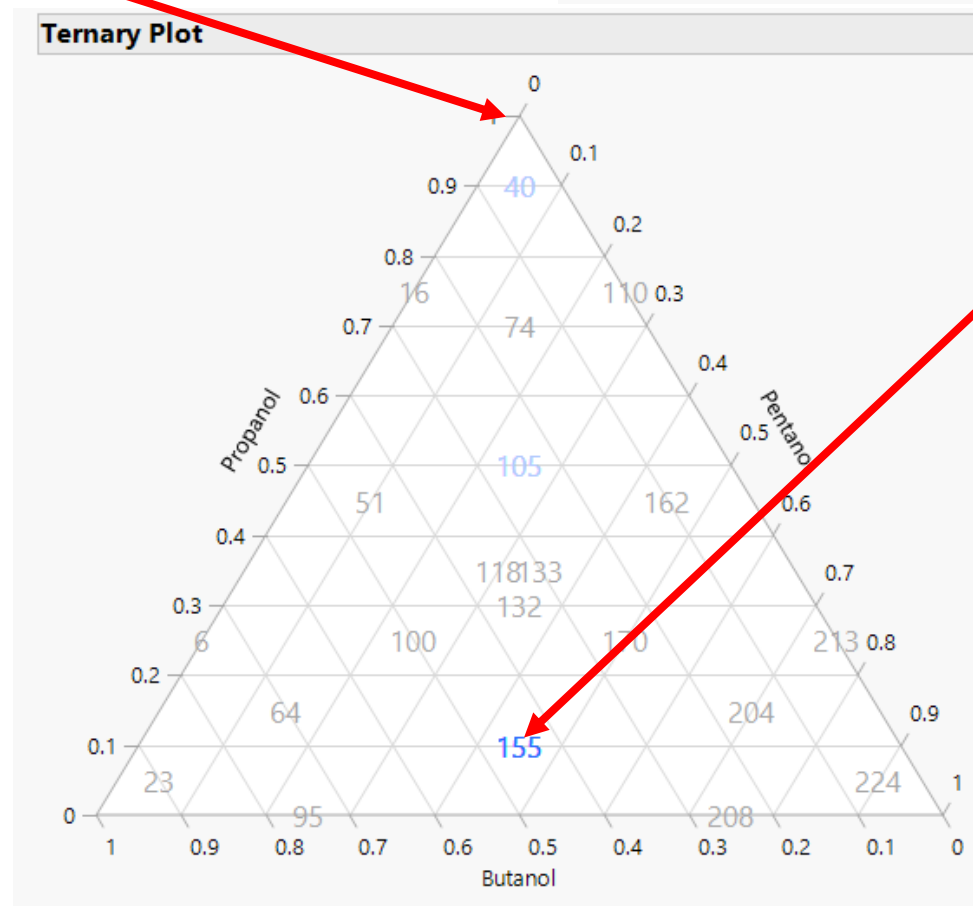


FDOE Profiler After Optimization "NMR_ID #155"

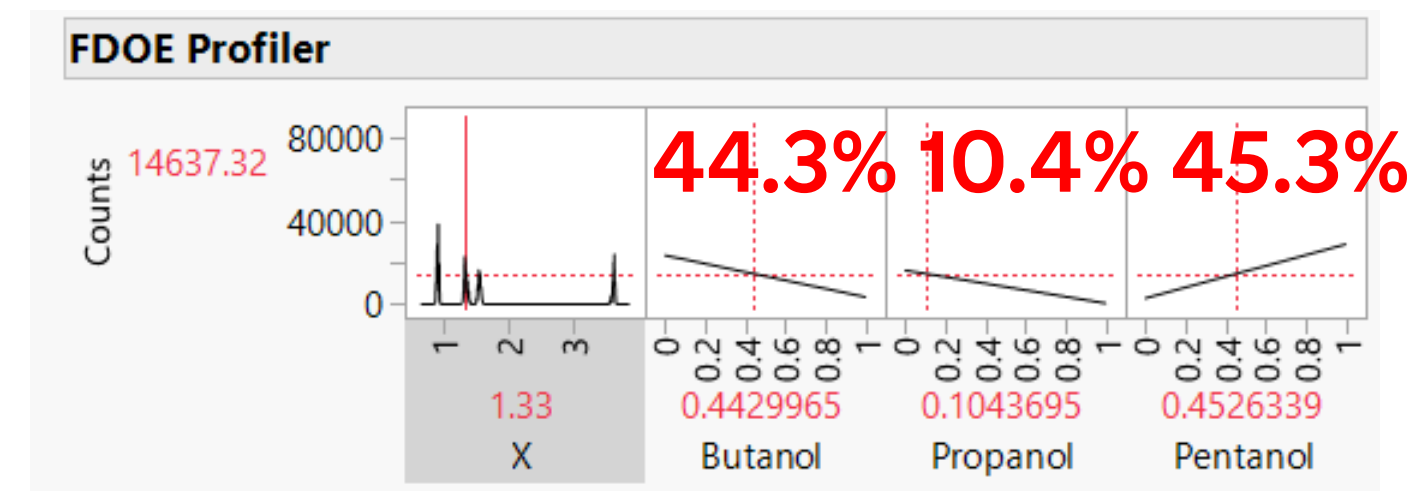


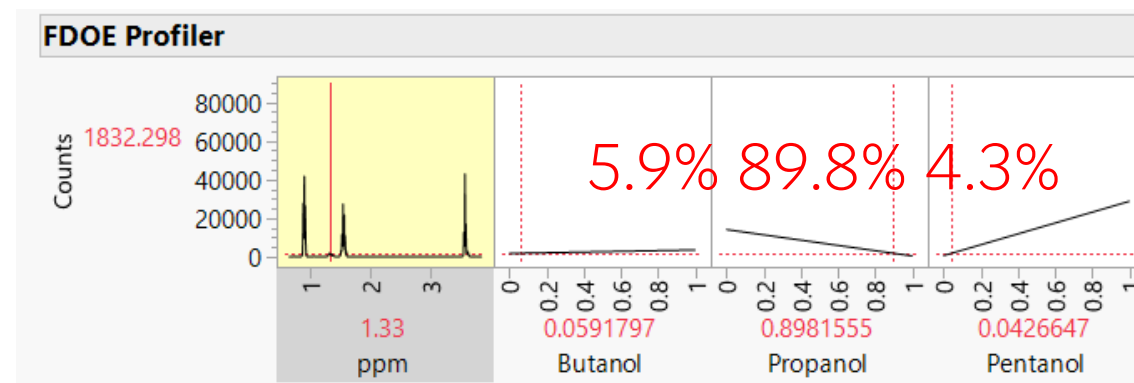
Using **NMR_ID #155** as the target curve

Minimize Integrated Error from Target yields composition

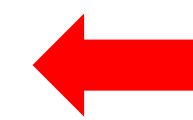


Actual 45.0%, 10.0%, 45.0%

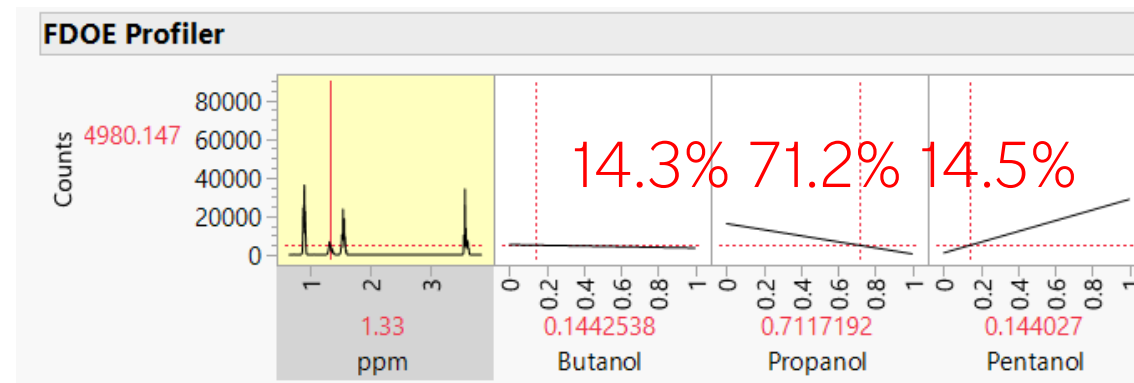




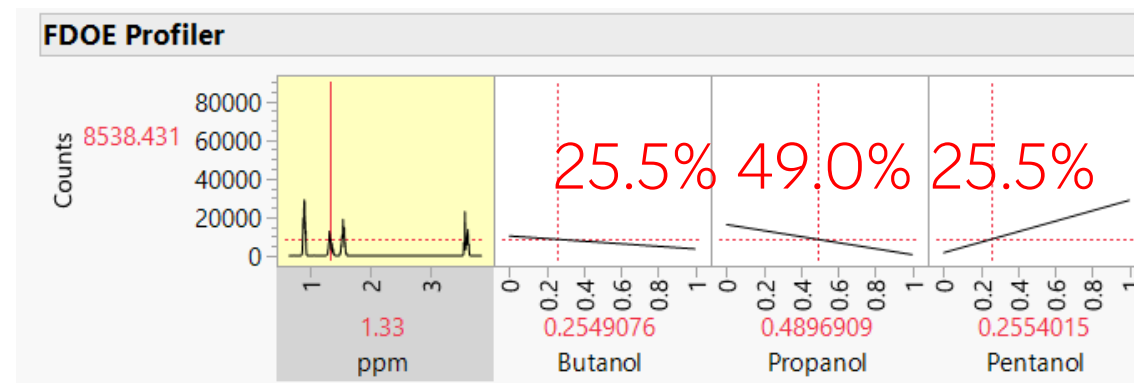
RMSE
0.67%



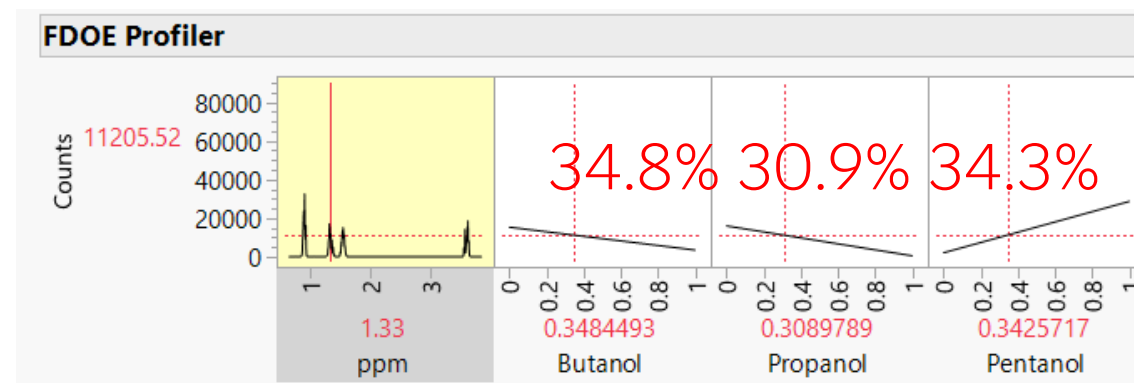
Predicted Proportions for Check Point Spectra from 6-Blend FDA Model



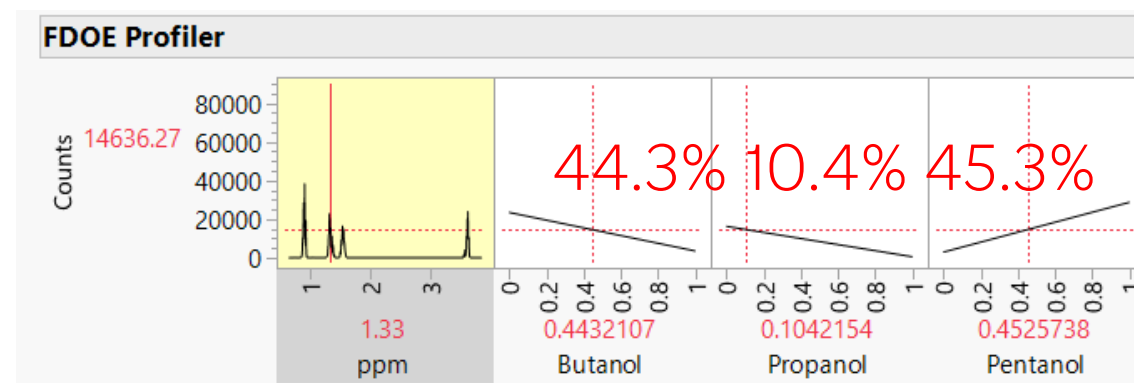
0.85%



0.71%

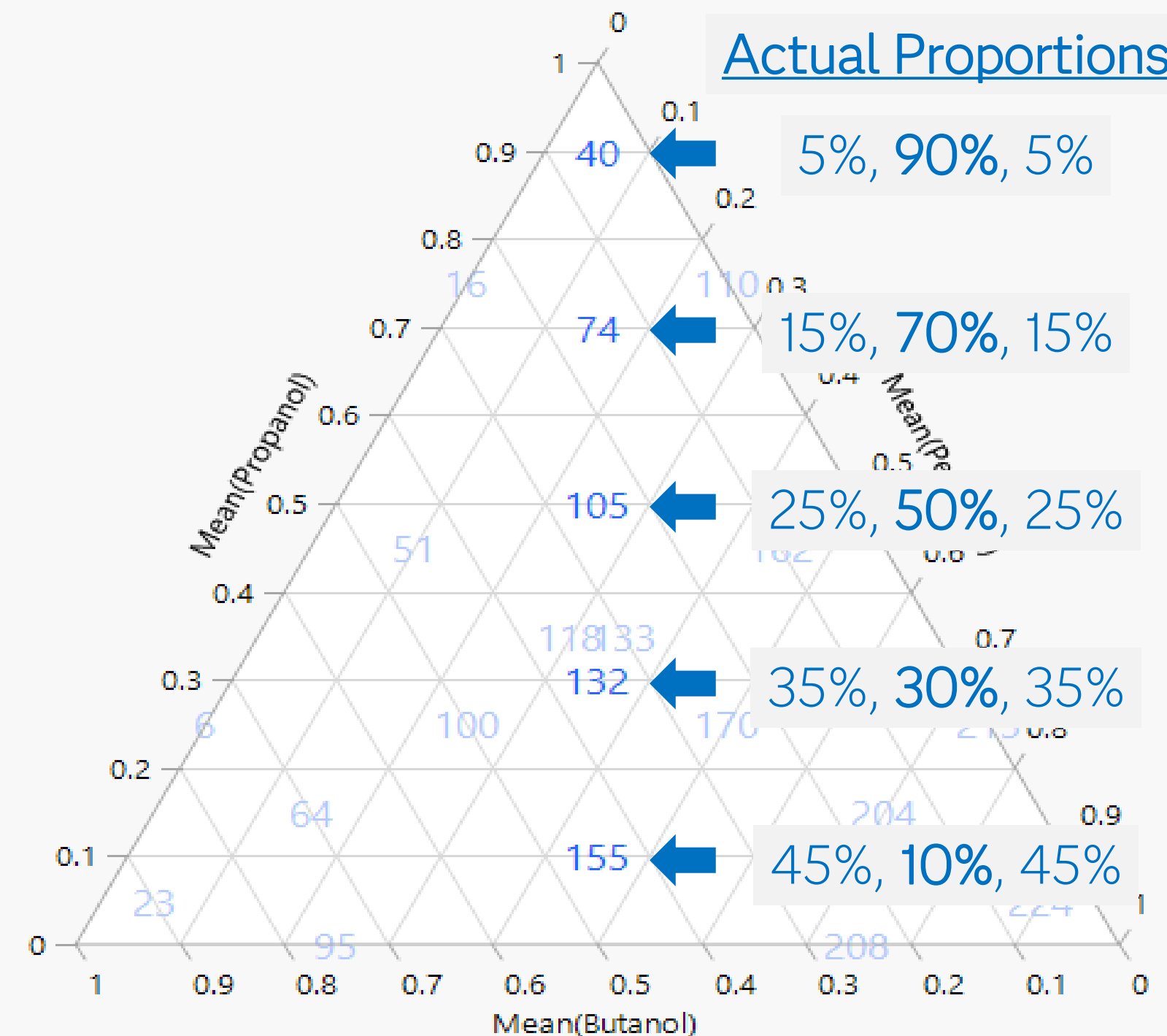


0.67%



0.50%

Ternary Plot




Let's go to JMP...

- Perform FDA on the NMR spectra of 6 alcohol blends and identify the composition of the 7th *target* blend

How might this be used in industries like chemical, biopharma, food, & consumer products

1. Run a DOE with component and factor ranges you believe encompass the unknown competitor formulation settings
2. Use FDA to model the spectra of the DOE blends & conditions
3. Use FDA-DOE model and the target spectra of competitor's product to closely determine the actual formulation

How might this be used in industries like defense and aerospace?

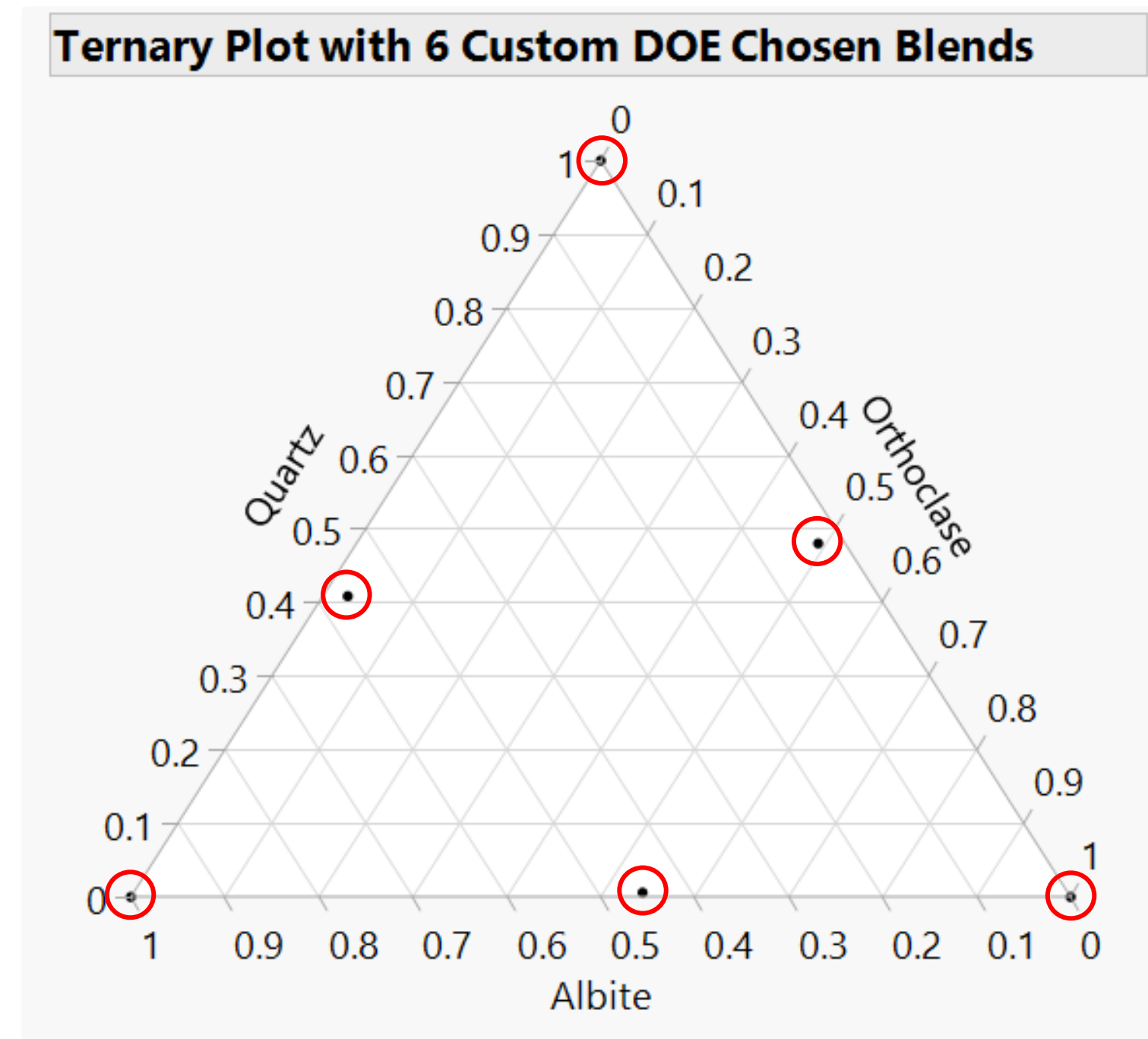
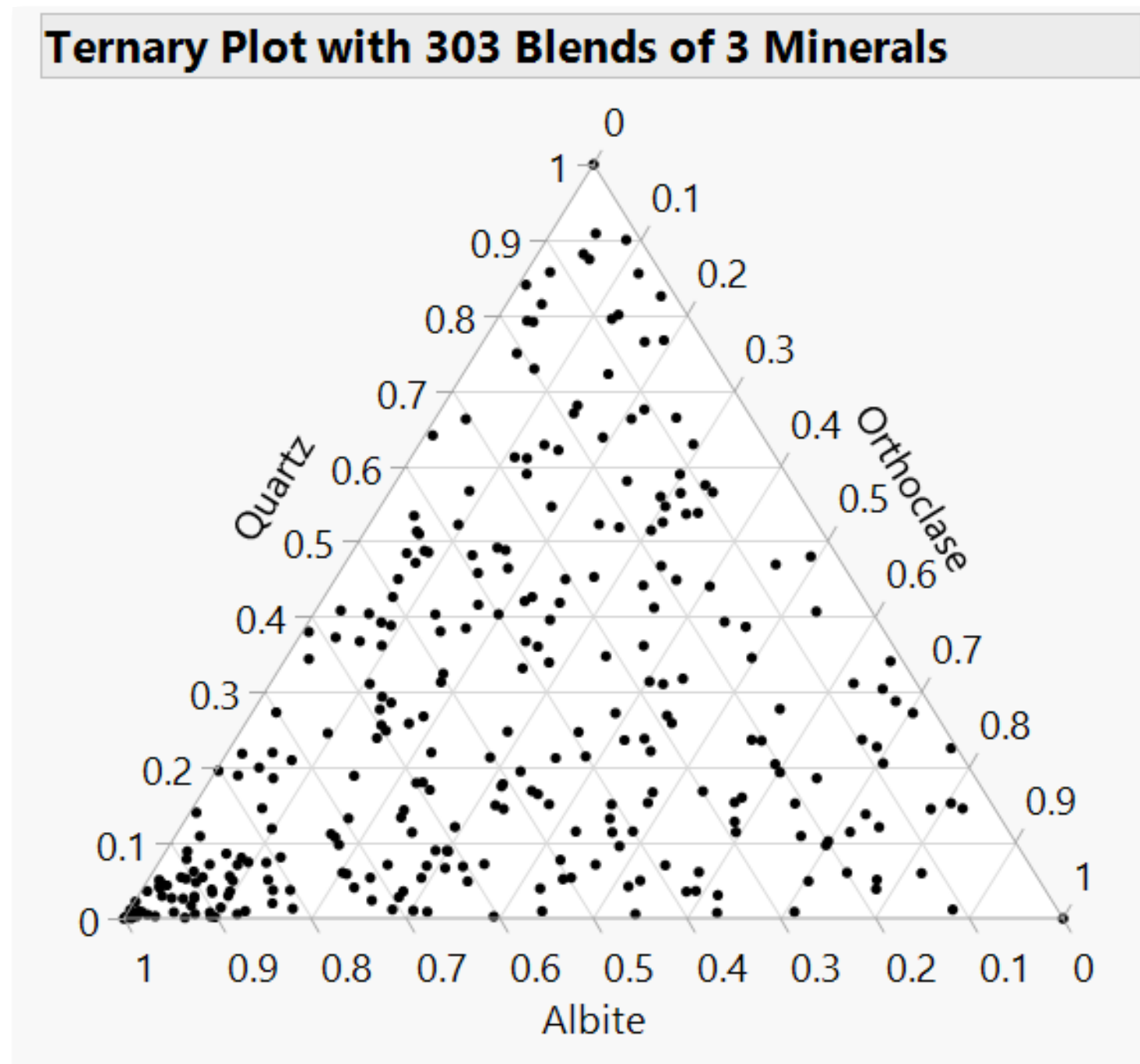
1. Help formulate chemical composition of a decoy flare, so its spectra matches that of a particular aircraft engine
2. By analyzing
 - spectra of sensors
 - sonar signatures
 - radar signatures

All as functions of factors like shape, speed, angle, distance, vibration, etc.

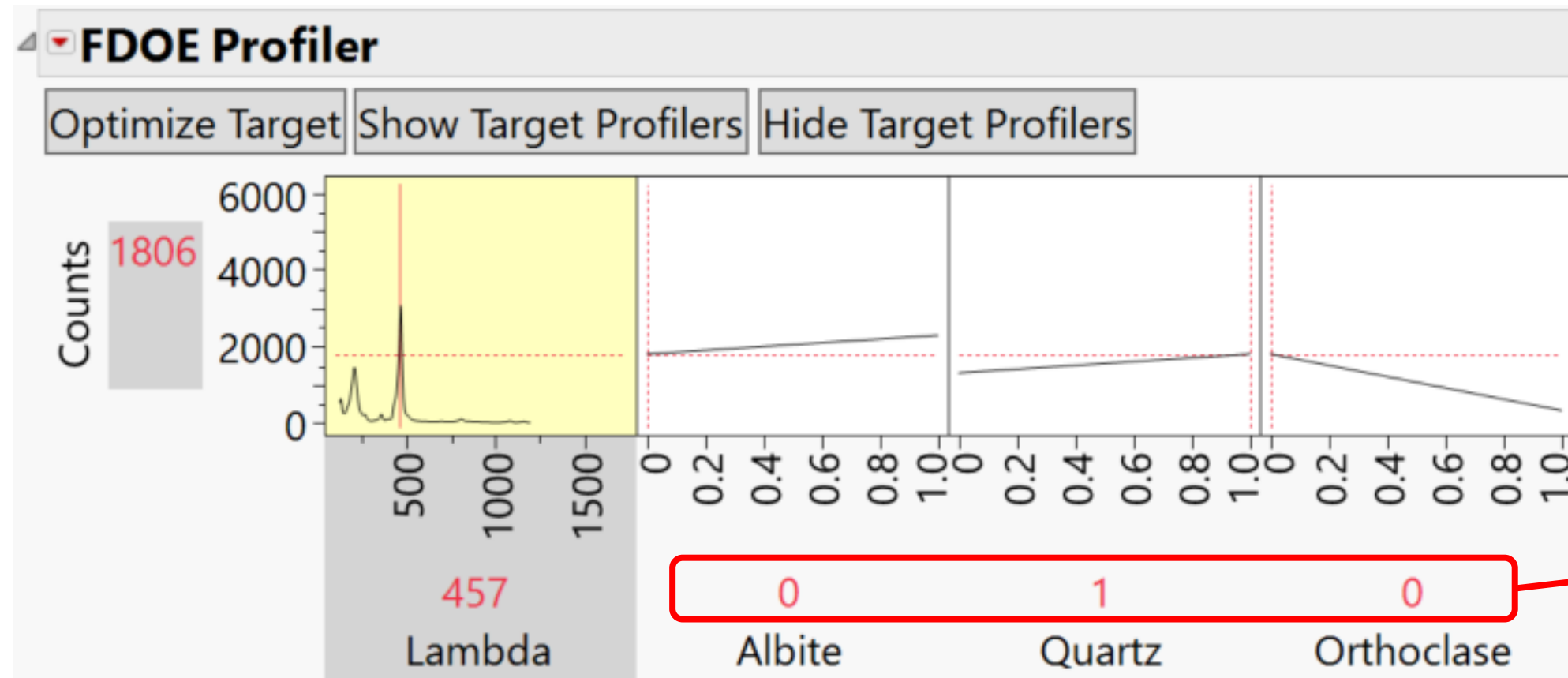
Better predict remaining useful life of engines and
improve identification of detected submersibles and aircraft

Case 2 - Reanalysis of Raman Spectral Data for 3-Mineral Mixture DOE using FDA

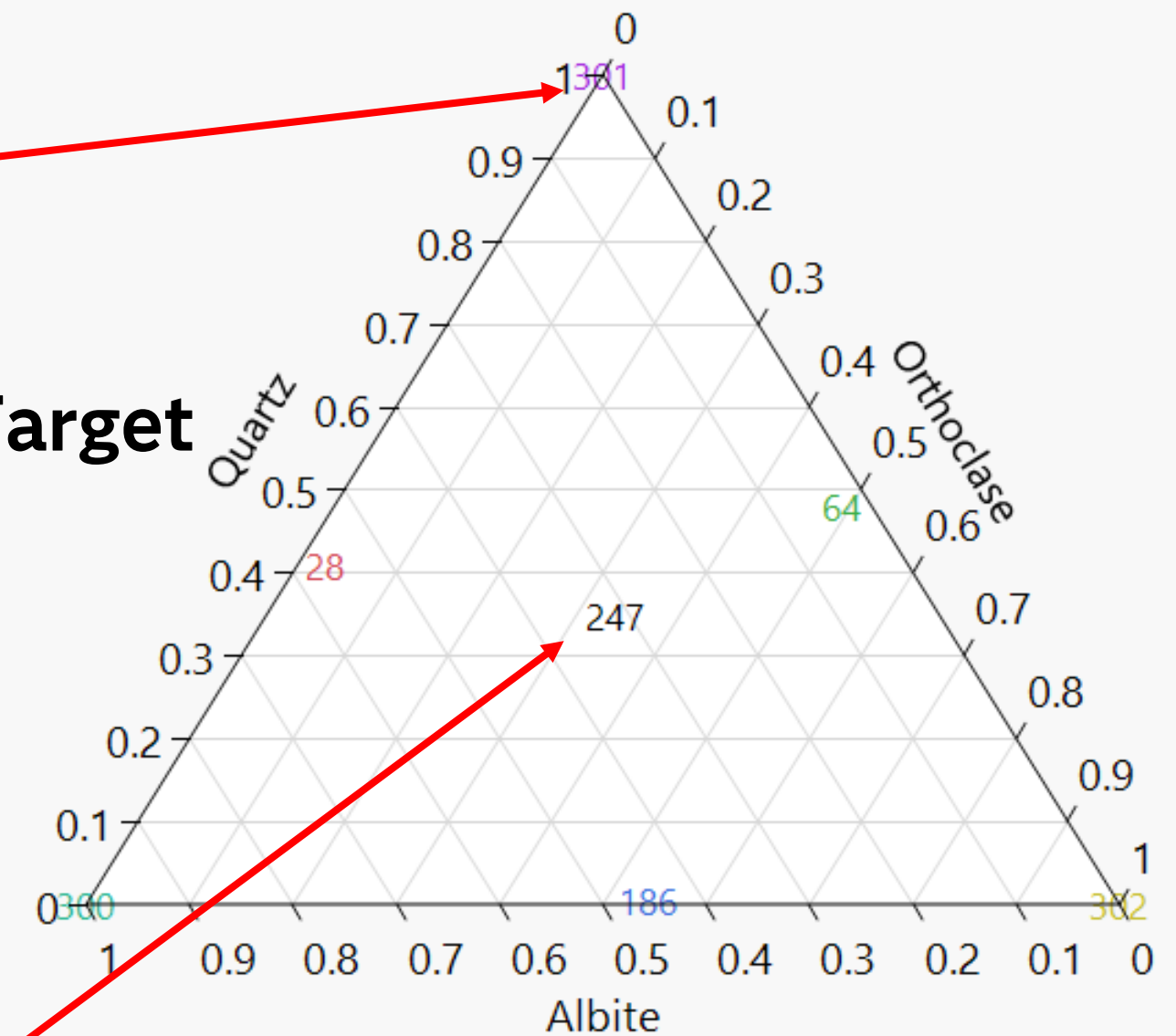
All 303 blends used as candidate trials 6 on right are resulting subset DOE



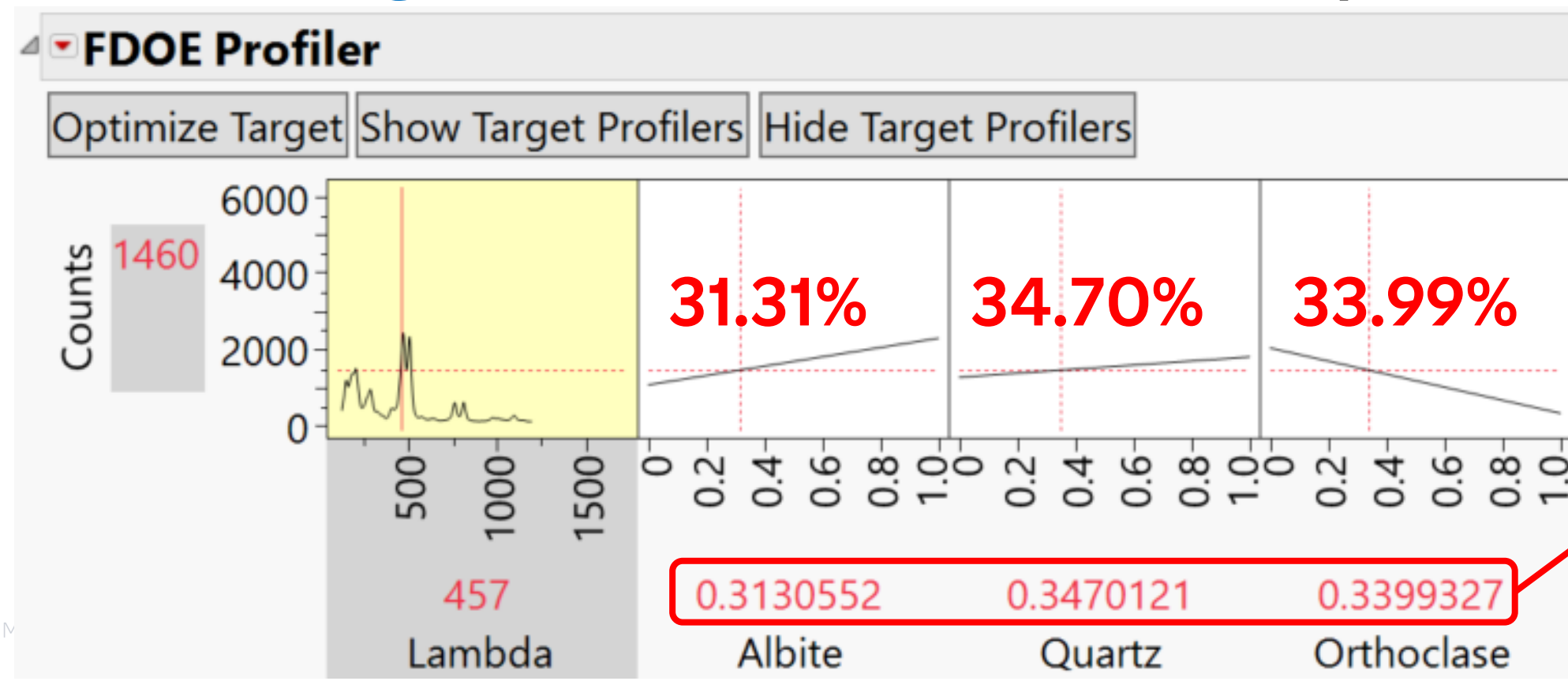
Settings for Raman ID# 301 (0%, 100%, 0%) – before Optimize Target



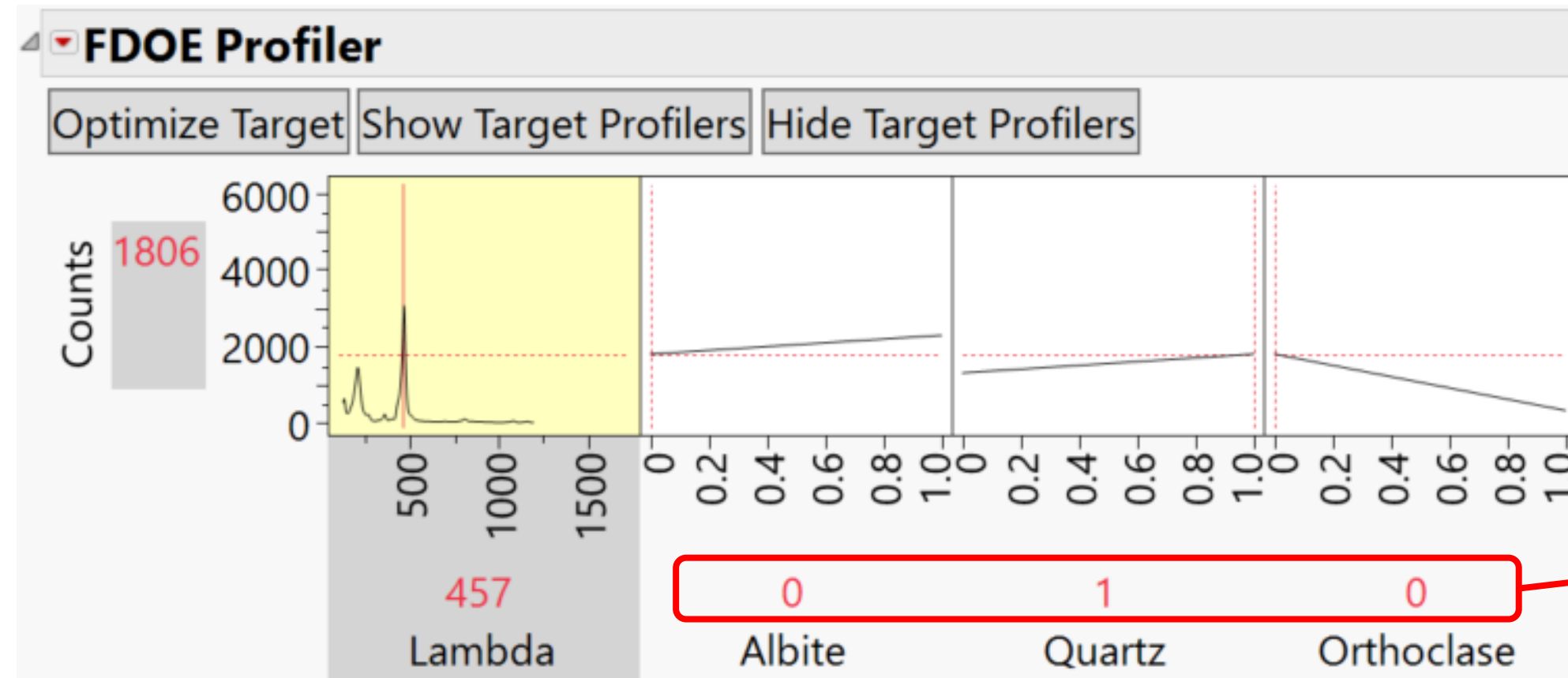
Ternary Plot



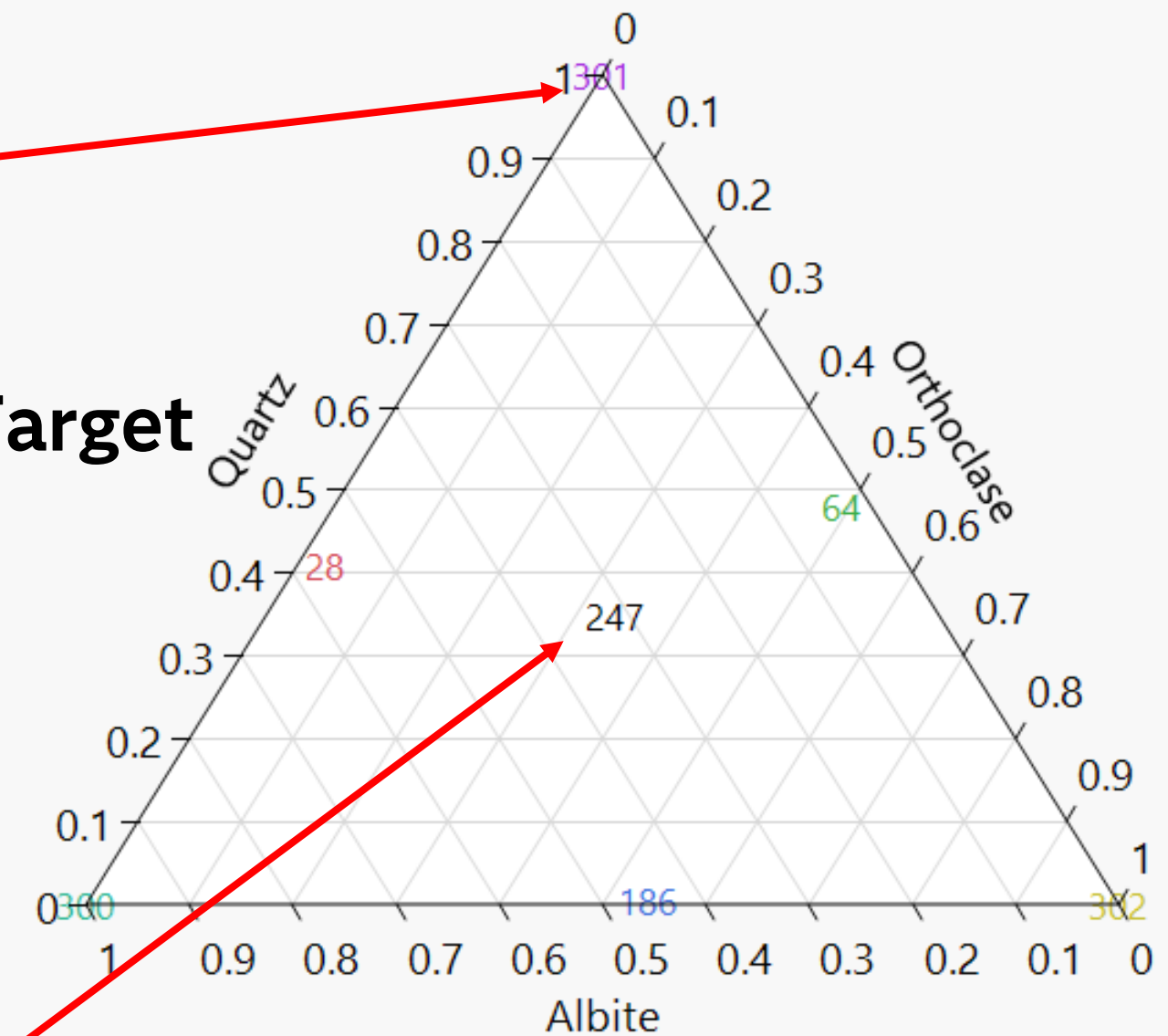
Predicted settings for Raman ID #247 – after Optimize Target



Settings for Raman ID# 301 (0%, 100%, 0%) – before Optimize Target

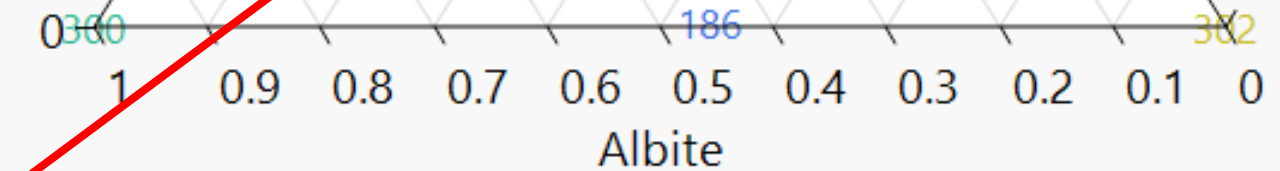
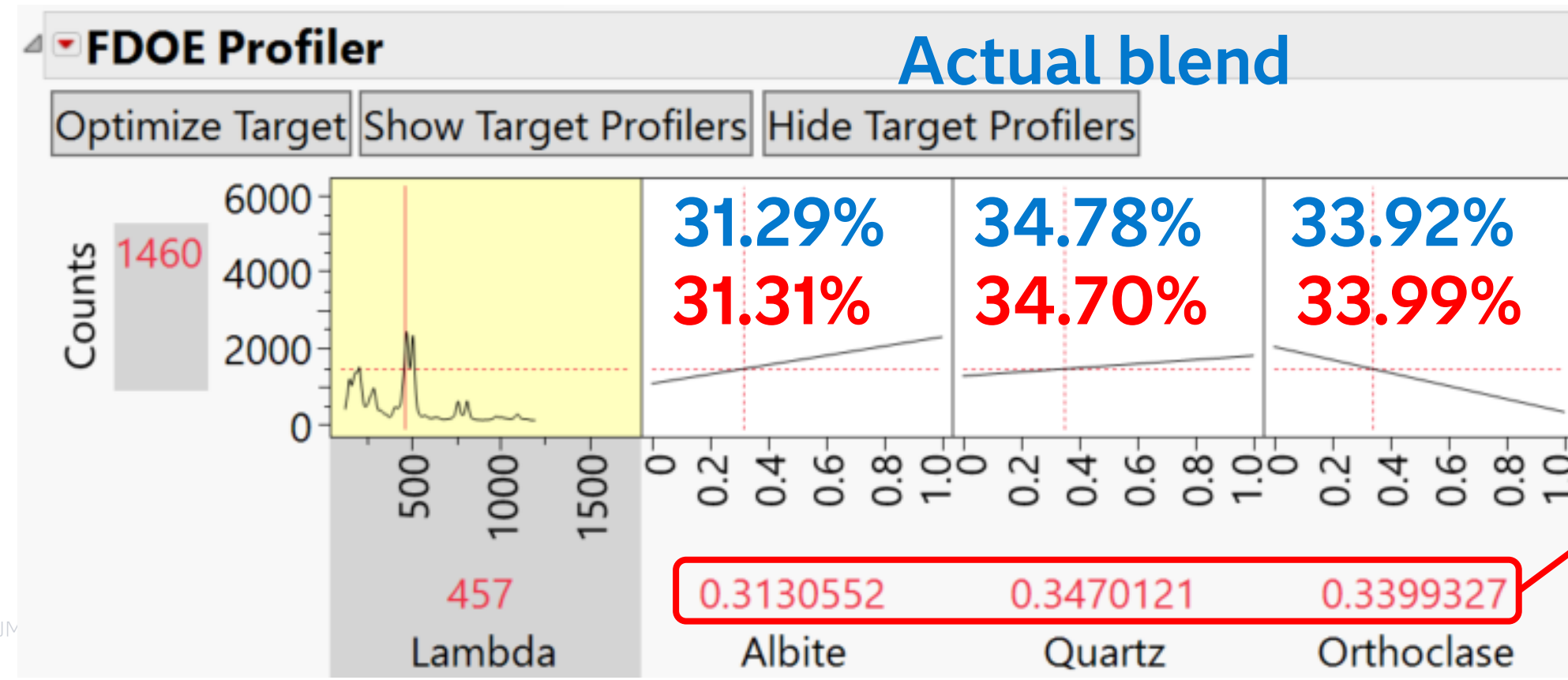


Ternary Plot



Predicted settings for Raman ID #247 – after Optimize Target

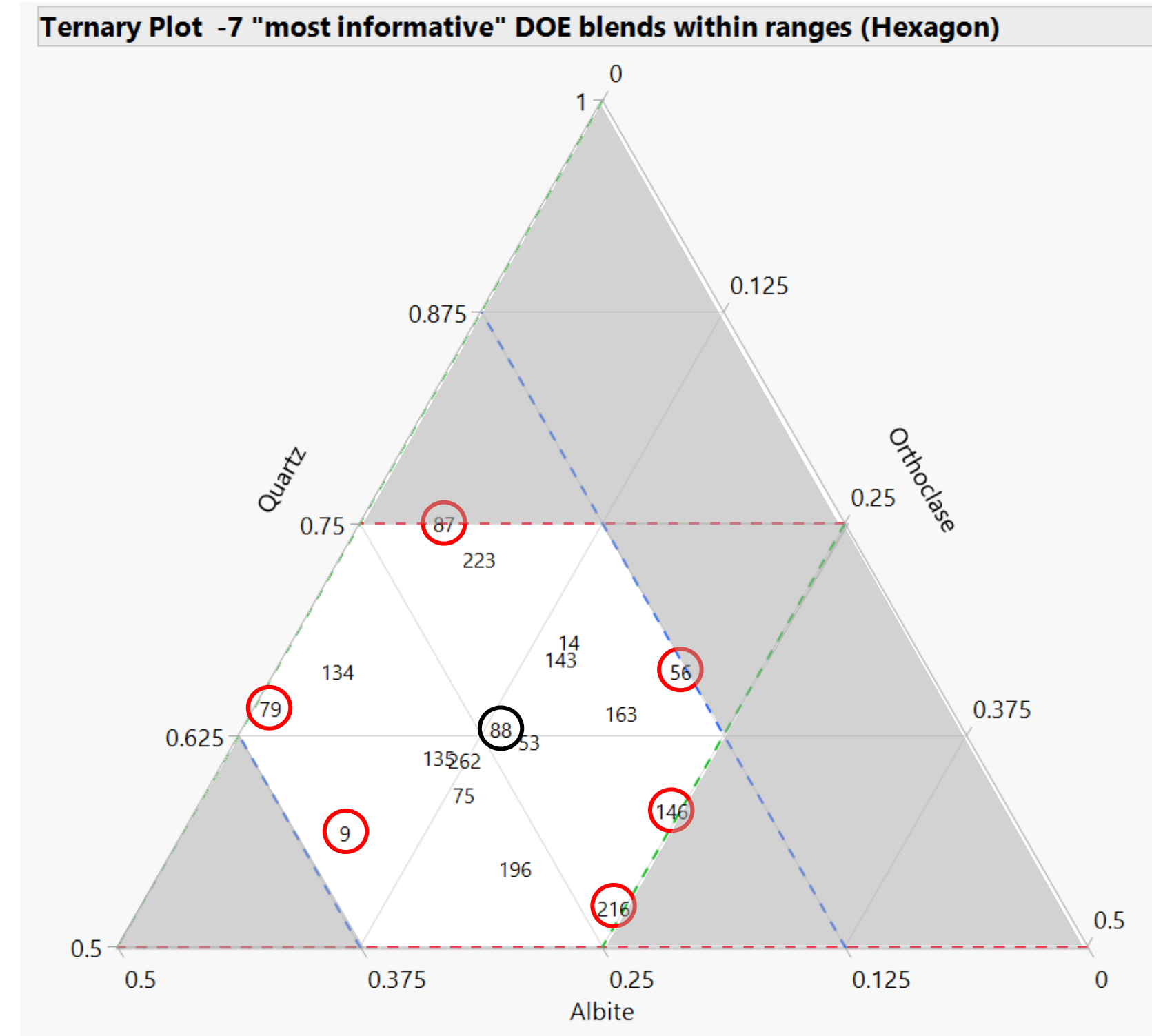
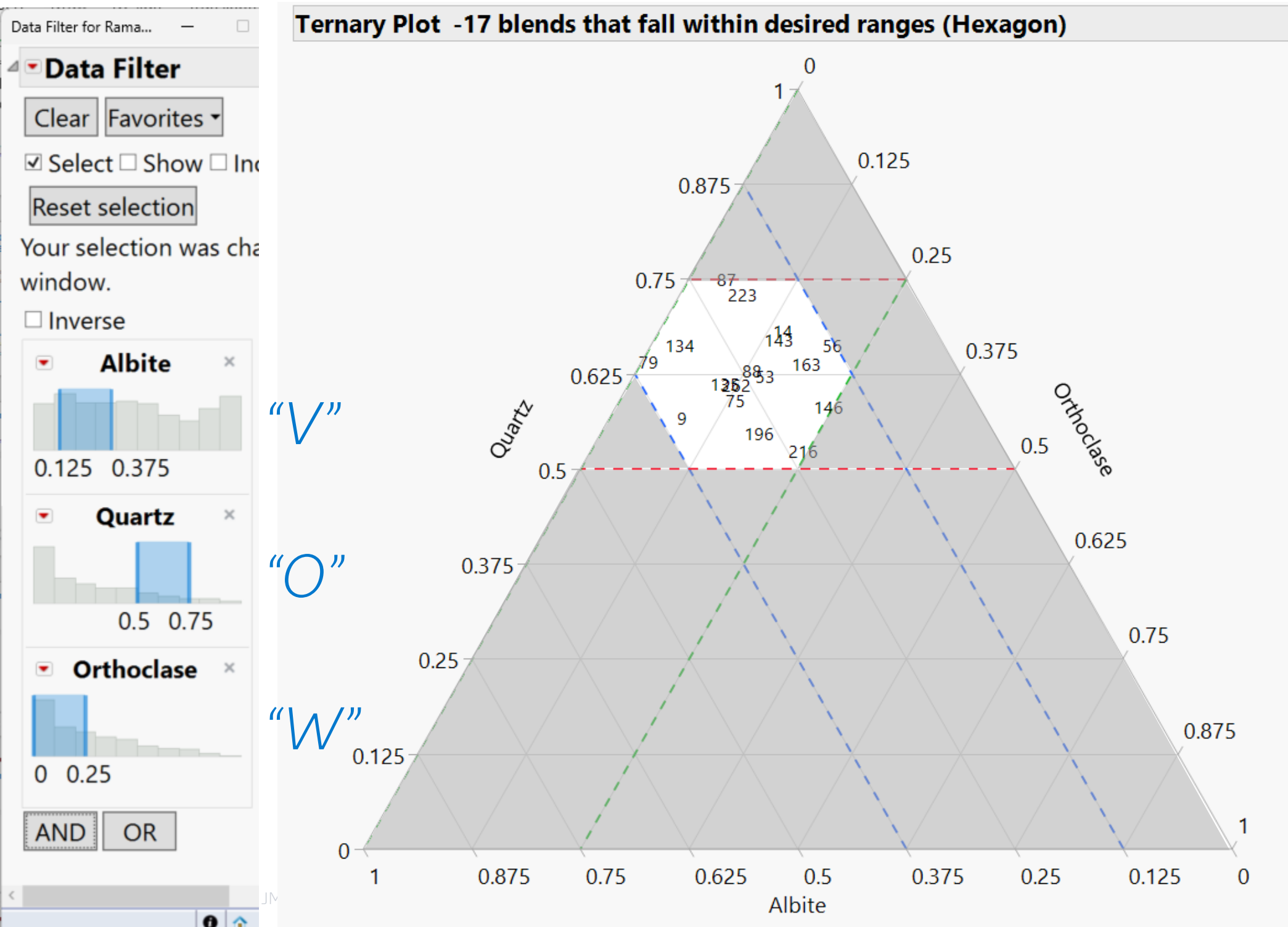
Actual blend



Case 2 - Reanalysis of Raman Spectral Data for 3-Mineral Mixture DOE using FDA

17 *filtered* blends used as candidate trials

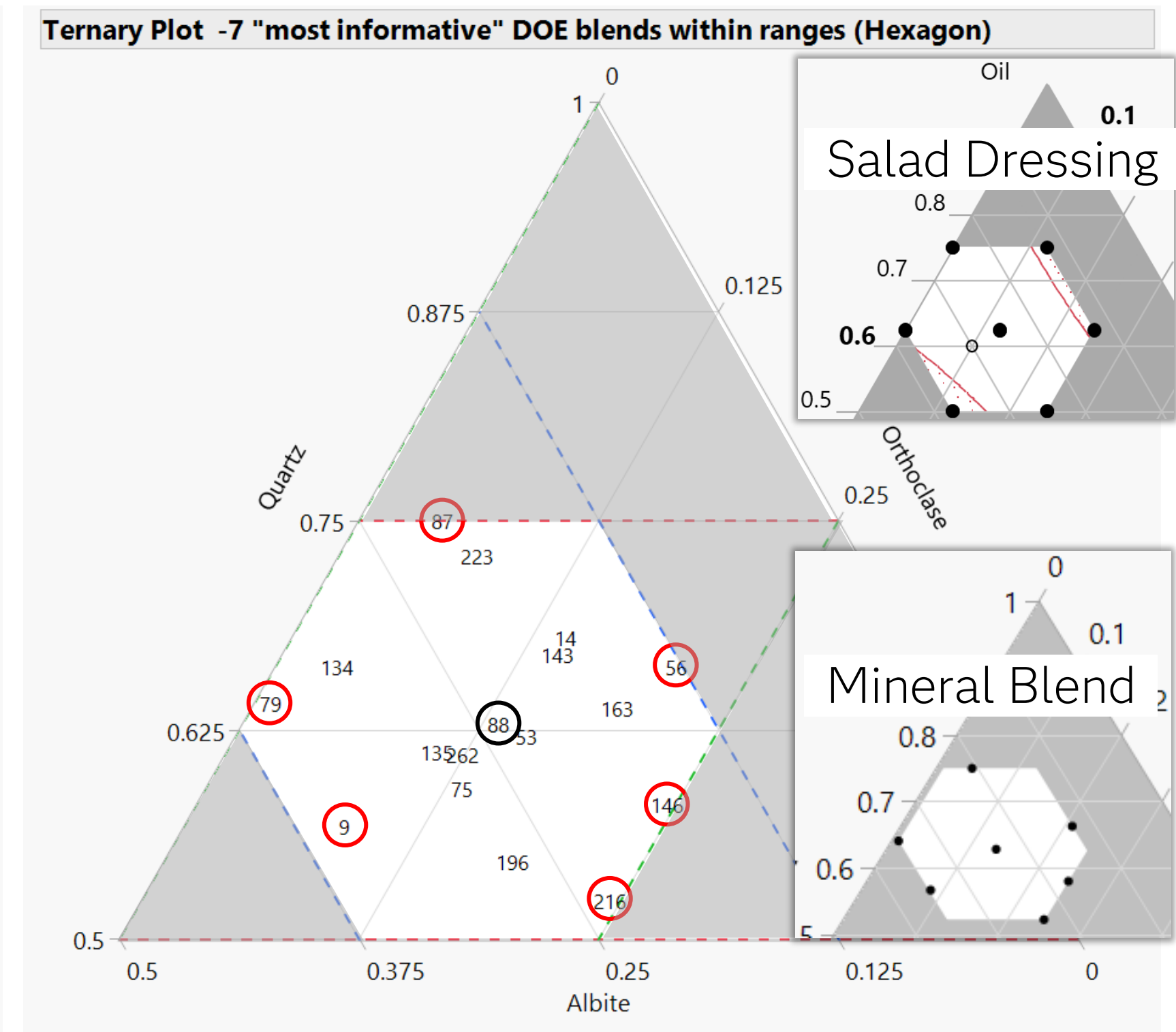
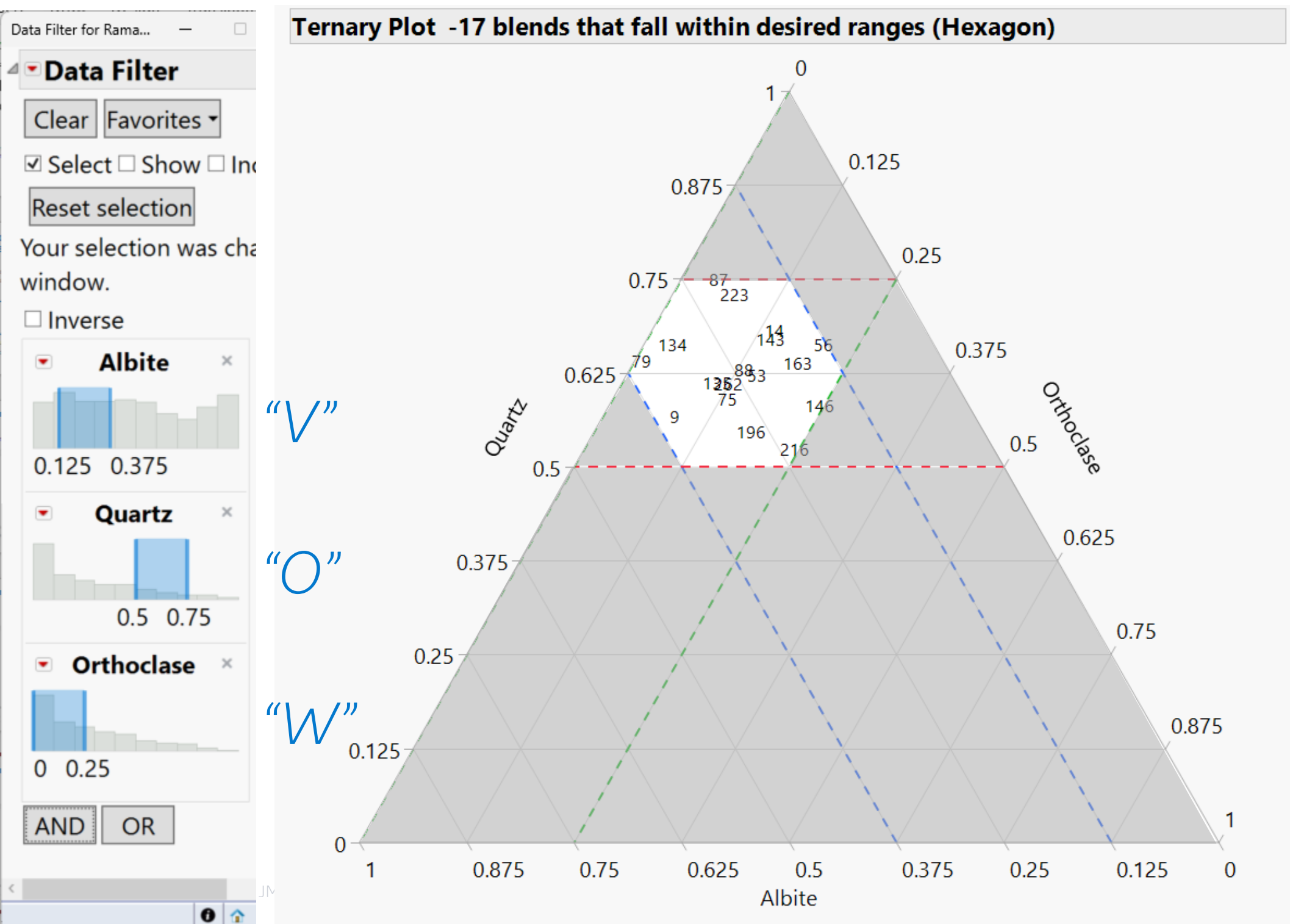
7 circled trials are DOE subset



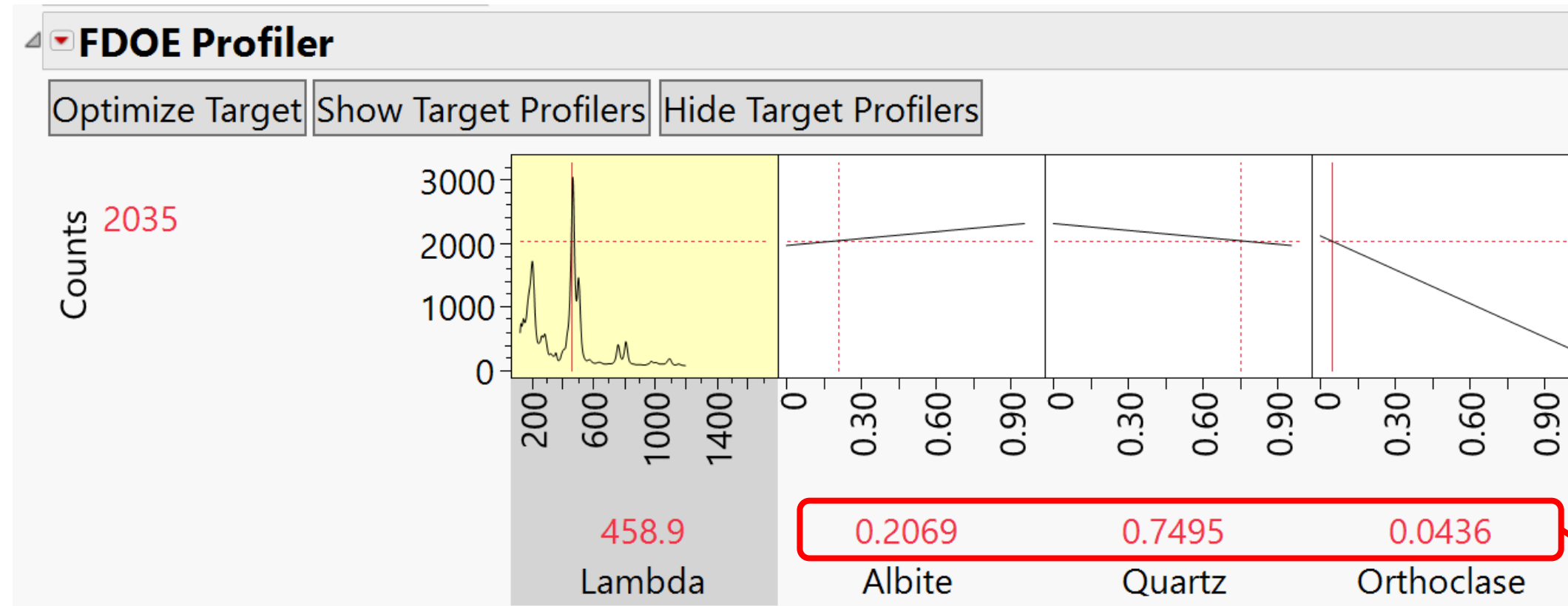
Case 2 - Reanalysis of Raman Spectral Data for 3-Mineral Mixture DOE using FDA

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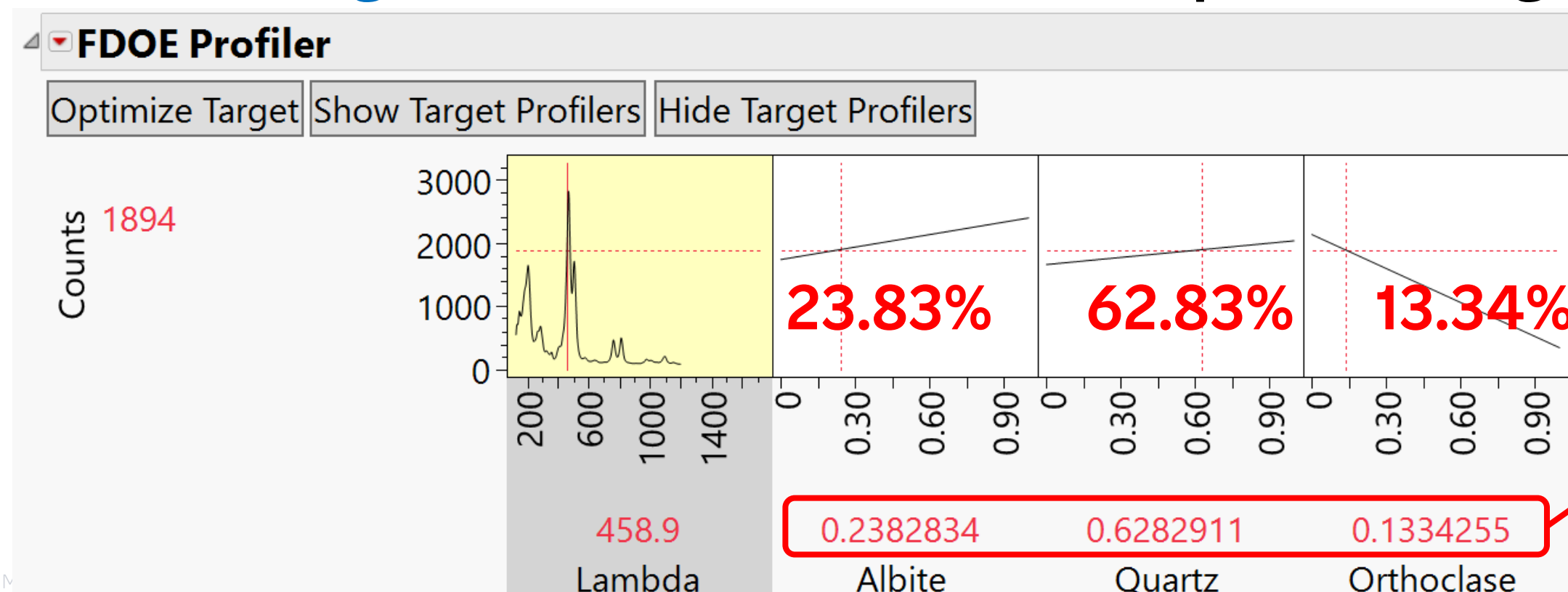


Settings for Raman ID# 87 (20.69%, 74.95%, 4.36%) – before Optimize Target

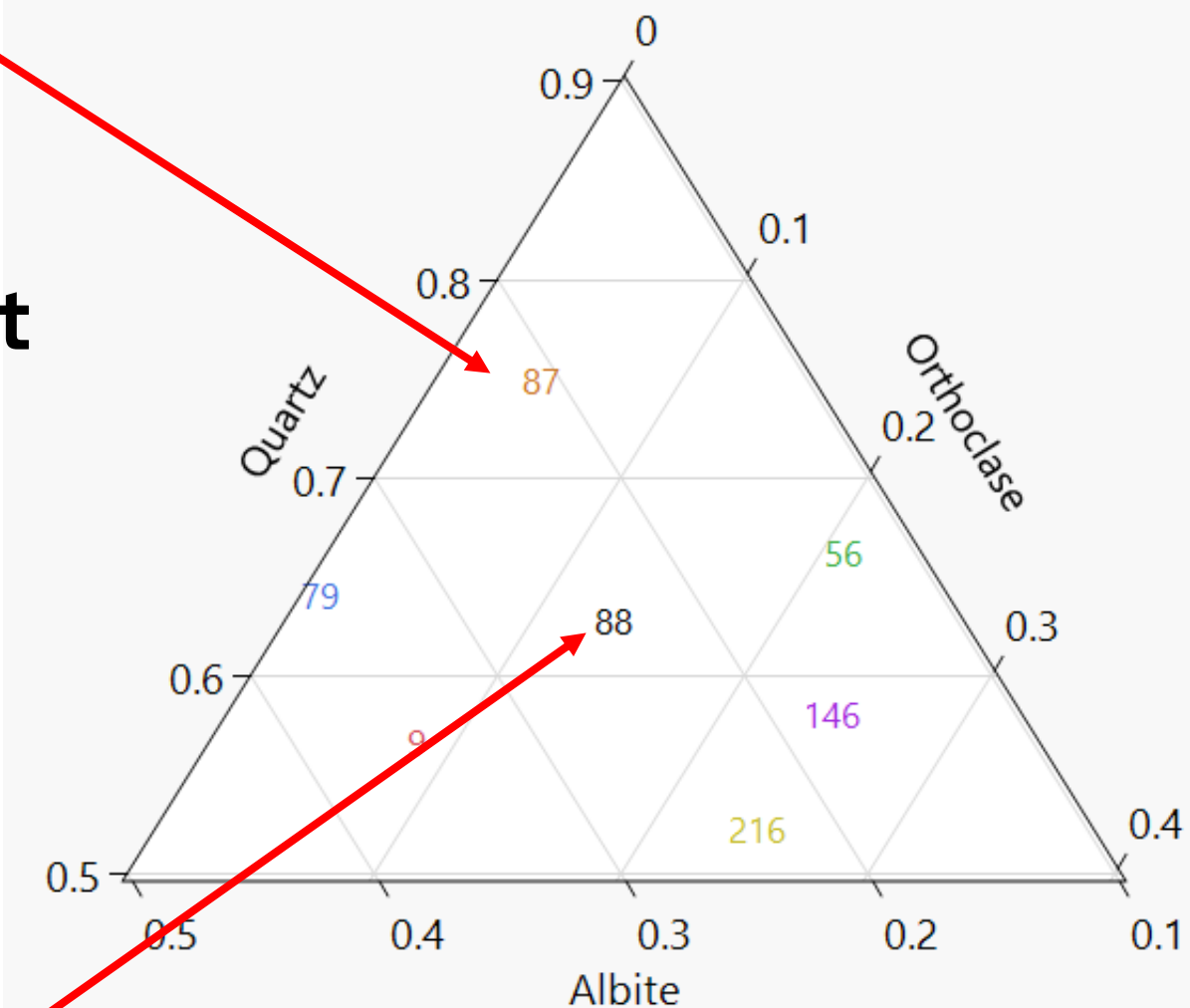


NOTE: Outer 6 points used to Train Model
Raman ID# 88 used as Target spectra

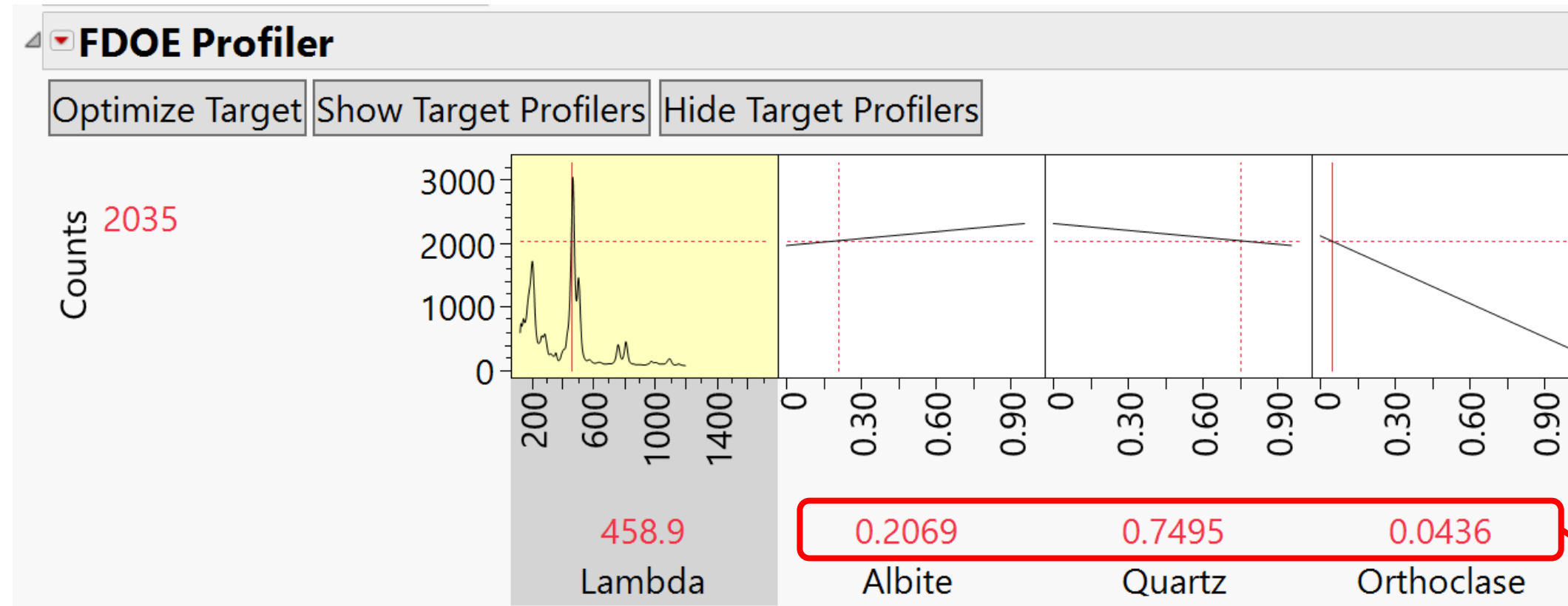
Predicted settings for Raman ID #88 – after Optimize Target



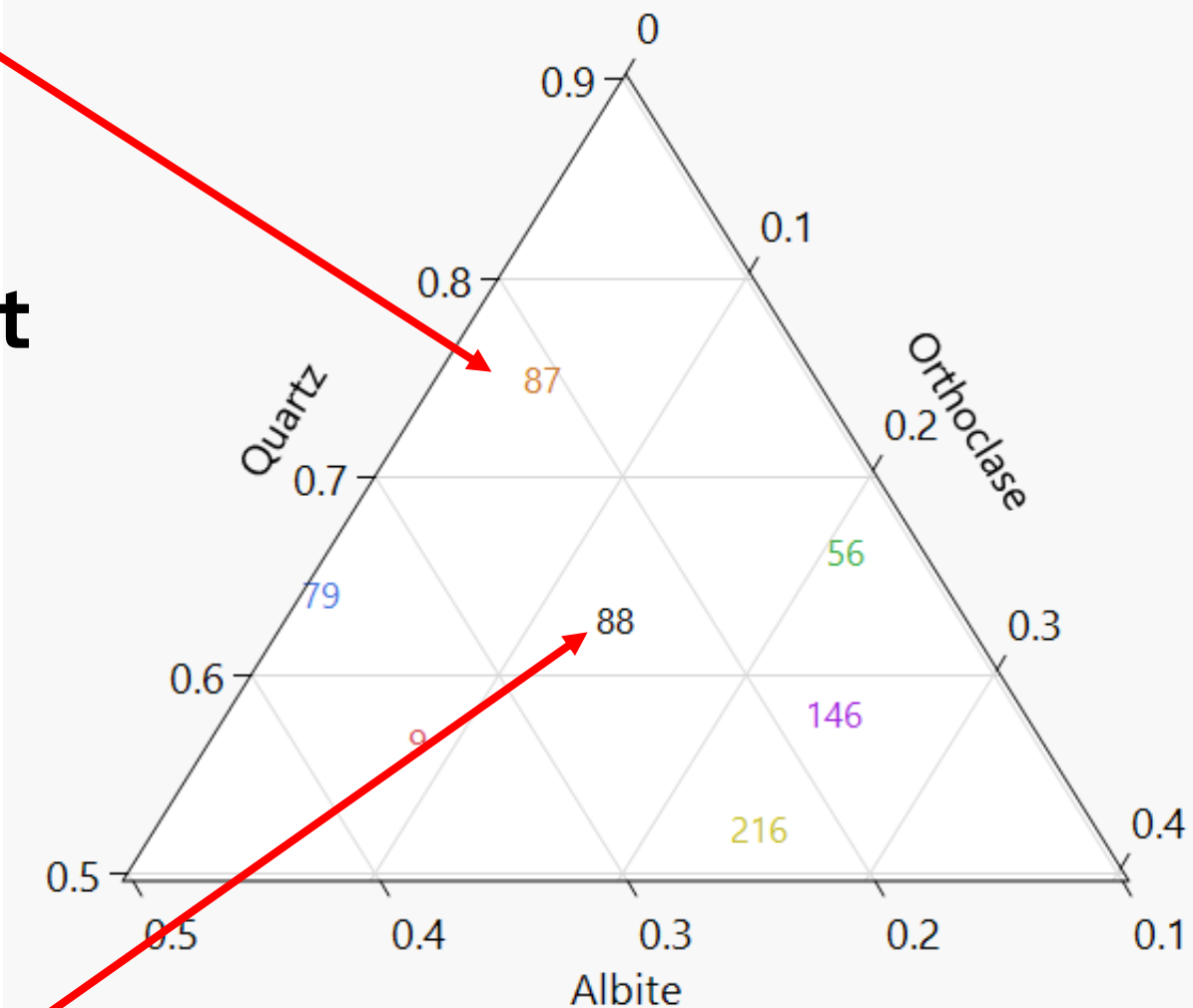
Ternary Plot



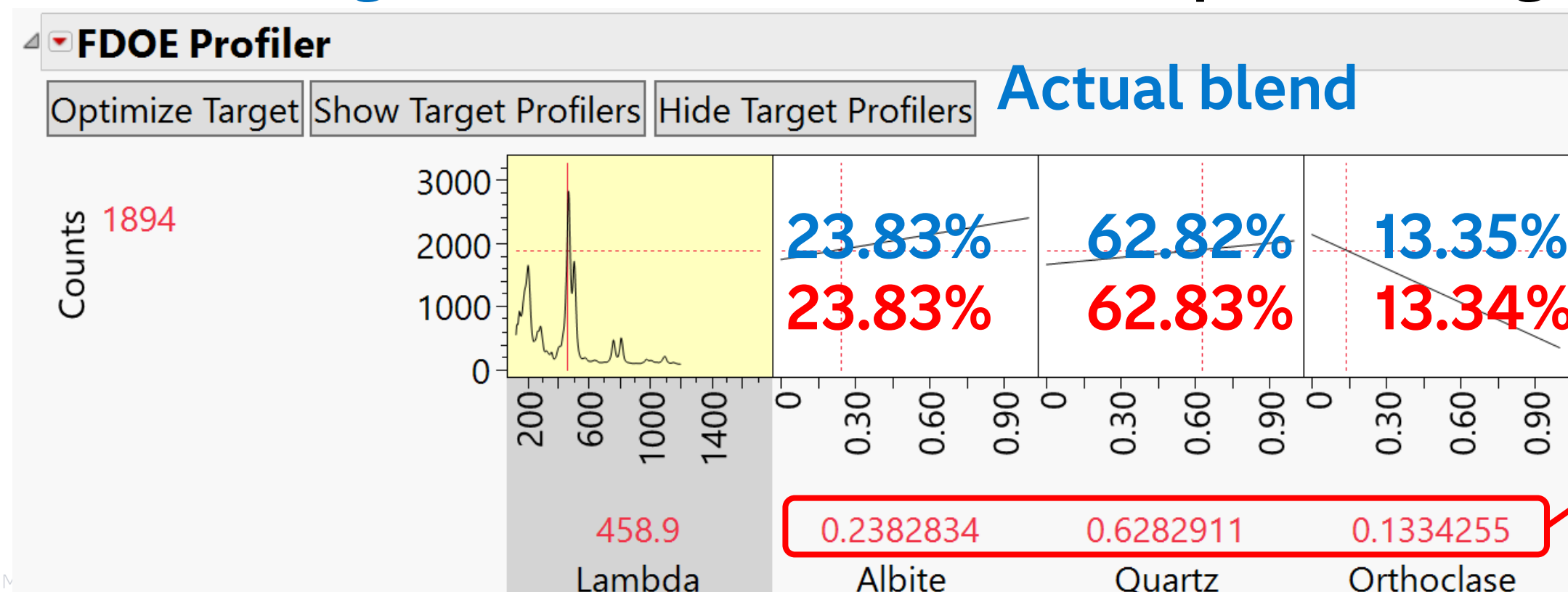
Settings for Raman ID# 87 (20.69%, 74.95%, 4.36%) – before Optimize Target



Ternary Plot



Predicted settings for Raman ID #88 – after Optimize Target



Let's go to JMP...

- Filter out candidates in an interesting subregion of the full mixture space
- Use Custom DOE to find the most informative subset of 7 trials

Takeaways

1. Use DOE to get most information from fewest trials
2. Use FDA to better model curves and spectra
3. Combine DOE with FDA to predict spectra
4. Combine DOE with FDA to predict formulation (factor settings)
5. Create a DOE by choosing informative subset of trials from candidates

Questions?

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Thanks to my JMP colleagues

Chris Gotwalt, Chief Data Scientist

Ryan Parker, Sr Research Statistician Developer

[Developer Tutorial Video on Spectral Data](#)

